Dynamic Relationship Between Gross Domestic Product and Domestic Investments in Rwanda

Bruno Ocaya\(^1\), Charles Ruranga\(^2\) and William Kaberuka\(^3\)

Abstract

This study uses a VAR model to analyse the dynamic relationship between gross domestic product (GDP) and domestic investment (DI) in Rwanda for the period 1970 to 2011. Several selection lag criteria chose a maximum lag of one and a bivariate VAR(1) model specification in levels was adopted. Unit root tests show that both GDP and DI series are nonstationary in levels but stationary in first differences, implying that both are integrated of order one I(1). Tests of cointegration established that GDP and DI are CI(1,1), suggesting there is a long-run equilibrium relationship between the two series. The error correction model indicates that DI adjusts to GDP with a lag whereby 0.2 percent of the discrepancy between long-term and short-term DI is corrected within the year. Granger causality tests show that there is unidirectional causality where GDP causes DI. The bivariate VAR (1) was unstable when estimated at levels, but was stable in first differences. Finally it was found out that GDP almost perfectly predicts DI in the estimated VAR (1) model. The forecasted value of DI in 2011 was 22.6% of GDP while the actual value was 22.7% of GDP. The small discrepancy may be attributed to the appropriate policy measures the Rwandan government and the private sector federation have thus far taken to facilitate investors in their businesses.

Keywords: Gross Domestic Product (GDP); Domestic Investment (DI); Granger Causality; Cointegration; Vector Autoregression (VAR) and Vector Error Correction Model (VECM)

1.0 Introduction

Investment is a powerful channel for innovation, economic growth and therefore poverty reduction. Recent empirical studies have established linkages between investment and economic growth, Baro (1991); Baro et al (1993), Ben- David (1998), Collier et al (1999), Ghura and Hadjimichael (1996), Hernandez-Cata (2000), Khan et al (1990) and Ndikumana (2000). Analysis of causality between economic growth and domestic investment conducted in different countries are marred with ambiguities and inconclusive results. For example, several researchers have found bi-directional relationship, Tang et al (2008), Tan and Lean (2010). Others found the direction of causality to be from economic growth to domestic investment, Choe (2003) and Qin et al (2006) while some found the
direction of causality to be from domestic investment to economic growth, Villa (2008). Also in other studies, private investment was shown to be super-exogenous, meaning investment was the primary determinant of economic growth, Montek (2002).

Rwanda has made significant progress in poverty reduction and has improved the conditions of doing business, World Bank (2011). Different policies have been adopted in order to increase gross domestic product and promote domestic investment but there has been no empirical study which has attempted to establish the relationship between the growth of GDP and investment. In other words, the question about the forecasting power of investment growth and economic growth remains a moot point. The few and sketchy studies that exist are mainly descriptive in nature and offer limited understanding of the relationship for policy prescription in Rwanda.

Rwanda is a land-locked country located in east and central Africa. It borders Uganda to the north, Tanzania to the east, the Democratic Republic of Congo to the west, and Burundi to the south. Rwanda covers 26,338 square kilometres of land. The current population is about 10.7 million, exhibiting a very high population density of 407 inhabitants per square kilometre, African Development Bank (2011). Agriculture and Services are the principal sectors contributing to more than 80% of GDP. Coffee and tea are the main primary products exported and they constitute 40% of export earnings. Due to limited diversification of its economy, Rwanda’s balance of payments has continued to be unfavourable with current account balance always in the negative.

After the 1994 genocide, Rwandan embarked on a new development path. The new government ushered in peace, political stability, good governance and minimal corruption among others. As a result, Rwanda’s economy has since 2002 been experiencing robust, resilient and sustained GDP growth in the East African region averaging over eight percent annually, World Bank (2012). The Rwandan government has also made significant efforts to promote private sector led growth to spur domestic investment currently at 22% of GDP, World Bank (2012). Extreme poverty has fallen from 40% in 2000 to 24% in 2011. Though still high, the percentage of the population living below poverty line has significantly reduced from 77.8% to 44.9% between 1994 and 2011 respectively, National Institute of Statistics of Rwanda (2011)

The objective of this paper is to analyse and establish the unknown feedback mechanism between GDP and DI for shaping the development policy in Rwanda. A bivariate VAR model was used to analyse the dynamic relationship between gross domestic product and domestic investment in Rwanda for the period 1970 to 2011.

2.0 Data and Methodology
2.1 Data
The data used for our analysis consists of 42 observations, collected from World Bank publications for the period 1970-2011, World Bank (2012). The variables analysed are GDP (at 2000 US$ prices) and gross fixed capital formation as percent of GDP, proxies of economic growth and domestic investment respectively. Economic growth represents the
increase in the amount of the goods and services produced by an economy over time. It is conventionally measured as percentage rate of increase in real gross domestic product. Domestic investment represents gross fixed capital formation or gross domestic fixed investment. It includes land improvements, plant, machinery, equipment purchases, commercial and industrial buildings; and construction of roads, railways, schools, offices, hospitals and private residential dwellings. In order to have a feel of the data used, we first plotted the time series for GDP and DI as defined in Figure 1 and Figure 2 below.

Figure 1: GDP and DI, Rwanda, 1970-2011

Except for the brief period of conflict and genocide in Rwanda in 1994, Figure 1 shows there has been an upward trend increase in the time series for both GDP and DI. Between 1970 and 2011, Rwanda’s DI increased more than seventy times, from US$15.8 million to US$1.4 billion. Figure 2 shows that the annual growth rate of GDP plummeted to -50% (genocide period) and theafter fluctuating around 8%. However, DI as a share of GDP exhibited an upward trend increasing from 7% in 1970 to 22.7% in 2011. Both graphical representations in Figure 1 and Figure 2 indicate general trending and fluctuation of GDP and DI series, implying their nonstationarity.
2.2 Model Specification

The general form of bivariate vector autoregressive (VAR model used to analyse the
dynamic relationship between GDP and DI is expressed as

\[
GDP_t = \delta + \sum_{i=1}^{p} \alpha_i GDP_{t-i} + \sum_{j=1}^{p} \beta_j DI_{t-j} + u_{1t}, \quad (1)
\]

\[
DI_t = \theta + \sum_{i=1}^{p} \alpha_i GDP_{t-i} + \sum_{j=1}^{p} \beta_j DI_{t-j} + u_{2t}, \quad (2)
\]

where \( \delta \) and \( \theta \) are intercepts, \( \alpha_i, \alpha_i, \beta_i, \beta_i \) represent coefficients, \( GDP \) is gross
domestic product (constant 2000 in US$), \( DI \) is domestic investment as percent of GDP,
\( t(t=1,2,...,T) \) is time period and \( p \) represents equal lags for GDP and DI. The \( u_{1t}, u_{2t} \) are
the stochastic error terms, also known as shocks, innovations or impulses with the assumptions:

(i) \( E(u_{1t}) = E(u_{2t}) = 0 \)

(ii) \( E(u_{it}u_{jt}) = \sum_{\tau} \begin{pmatrix} \text{var}(u_{it}) & \text{cov}(u_{it}, u_{jt}) \\ \text{cov}(u_{jt}, u_{it}) & \text{var}(u_{jt}) \end{pmatrix} \)

with

\( E(u_{it}u_{jt}) = \sigma_i^2 \) for \( i = 1, 2 \)

\( E(u_{it}u_{jt}) = 0 \) for \( t \neq \tau \).

3.0 Results and Discussion

The following sections present empirical time series analysis on the relationship between GDP and DI:

3.1 Lag Order Selection

Determination of maximum lag \( p \) was carried out using Akaike information criteria, Schwarz information criteria and others. The lower the values of Akaike and Schwarz statistics, the better is the model. All criteria chose lag one, suggesting a bivariate VAR (1) model as the appropriate model to be adopted for analysing the dynamic relationship between GDP and DI. The results are shown in Table 1 below.

### Table 1: VAR Lag Order selection

<table>
<thead>
<tr>
<th>Lag</th>
<th>LogL</th>
<th>LR</th>
<th>FPE</th>
<th>AIC</th>
<th>SC</th>
<th>HQ</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>-385.7850</td>
<td>NA</td>
<td>1484637.</td>
<td>19.88641</td>
<td>19.97172</td>
<td>19.91702</td>
</tr>
<tr>
<td>1</td>
<td>-318.9473</td>
<td>123.3928*</td>
<td>59208.31*</td>
<td>16.66396*</td>
<td>16.91989*</td>
<td>16.75579*</td>
</tr>
<tr>
<td>2</td>
<td>-317.6407</td>
<td>2.278132</td>
<td>68129.82</td>
<td>16.80209</td>
<td>17.22864</td>
<td>16.95513</td>
</tr>
<tr>
<td>3</td>
<td>-317.4289</td>
<td>0.347633</td>
<td>83154.82</td>
<td>16.99635</td>
<td>17.59353</td>
<td>17.21061</td>
</tr>
</tbody>
</table>

* indicates lag order selected by the criterion

LR: sequential modified LR test statistic (each test at 5% level)

FPE: Final prediction error

AIC: Akaike information criterion

SC: Schwarz information criterion

HQ: Hannan-Quinn information criterion

* Most of the results were obtained using EViews 7.0 and Stata 11.0 software packages.
The VAR model after lag determination becomes

\[ GDP_t = \alpha_{10} + \alpha_{11} GDP_{t-1} + \alpha_{12} DI_{t-1} + u_{1t}, \]

(3)

\[ DI_t = \alpha_{20} + \alpha_{21} GDP_{t-1} + \alpha_{22} DI_{t-1} + u_{2t}, \]

(4)

or

\[
\begin{bmatrix}
GDP_t \\
DI_t
\end{bmatrix} = \begin{bmatrix}
\alpha_{10} \\
\alpha_{20}
\end{bmatrix} + \begin{bmatrix}
\alpha_{11} & \alpha_{12} \\
\alpha_{21} & \alpha_{22}
\end{bmatrix} \begin{bmatrix}
GDP_{t-1} \\
DI_{t-1}
\end{bmatrix} + \begin{bmatrix}
u_{1t} \\
u_{2t}
\end{bmatrix}
\]

### 3.2 Unit Root Tests

Tests for unit roots were undertaken in order to determine the stationarity of the series for GDP and DI. The Augmented Dickey-Fuller (ADF) tests provided in Table 2 show that GDP and DI are not stationary at levels. Instead, their first differences were found to be stationary, in Table 3, implying that both GDP and DI are integrated of order one \([I(1)]\).

#### Table 2: The results of unit root test in levels

<table>
<thead>
<tr>
<th>Included in test equation</th>
<th>GDP</th>
<th>DI</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>ADF Test Statistic</td>
<td>Critical Value at different levels of significance</td>
</tr>
<tr>
<td></td>
<td>1%</td>
<td>5%</td>
</tr>
<tr>
<td>Constant &amp; trend</td>
<td>0.254149</td>
<td>-4.198503</td>
</tr>
<tr>
<td>Constant</td>
<td>1.929356</td>
<td>-3.600987</td>
</tr>
</tbody>
</table>

The null hypothesis of existence of unit root is not rejected since the Augmented Dickey-Fuller (ADF) test statistics are lower than the absolute critical values at 1% and 5% significant levels. These results establish that GDP and DI are non stationary in levels. However Table 3 rejects the null hypothesis of unit roots for both GDP and DI in their first differences because the absolute values of the ADF are less than the stipulated absolute critical values at 1% and 5% significant levels. Results using Phillips-Perron tests for unit roots arrive at similar conclusions.

#### Table 3: The results of unit root tests in first differences

<table>
<thead>
<tr>
<th>Included in test equation</th>
<th>GDP</th>
<th>DI</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>ADF Test Statistic</td>
<td>Critical Value at different levels of significance</td>
</tr>
<tr>
<td></td>
<td>1%</td>
<td>5%</td>
</tr>
<tr>
<td>Constant &amp; trend</td>
<td>-5.587328***</td>
<td>-4.205004</td>
</tr>
<tr>
<td>Constant</td>
<td>-5.103964***</td>
<td>-3.605593</td>
</tr>
</tbody>
</table>

*** denote the significance at 1 percent.
3.3 Tests of Cointegration

Cointegration tests were used to determine the existence of long-run equilibrium relationship between GDP and DI. The Augmented Engle-Granger test for cointegration was adopted for this purpose. This test involves unit root tests on residuals obtained from the estimation of the following models:

\[ \begin{align*}
\text{GDP}_t &= \beta_0 + \beta_1 \text{DI}_t + \epsilon_{1t} \\
\text{DI}_t &= \alpha_0 + \alpha_1 \text{GDP}_t + \epsilon_{2t}
\end{align*} \]

The ADF was applied on \( \hat{\epsilon}_{1t} \) and \( \hat{\epsilon}_{2t} \) to test for unit roots. The tests were based on testing the significance of \( \phi \) and \( \theta \) for the following residual models:

\[ \begin{align*}
\Delta \hat{\epsilon}_{1t} &= \phi \hat{\epsilon}_{1t-1} + \epsilon_{1t} \\
\Delta \hat{\epsilon}_{2t} &= \theta \hat{\epsilon}_{2t-1} + \epsilon_{2t}
\end{align*} \]

The results of the estimation of equations (7) and (8) are presented in Table 4(a) and 4(b) respectively:

**Table 4(a): Augmented Dickey-Fuller Test**

Augmented Dickey-Fuller Test Equation

Dependent Variable: \( \Delta \hat{\epsilon}_{1t} \)

Method: Least Squares
Sample (adjusted): 1971 2011
Included observations: 41 after adjustments

<table>
<thead>
<tr>
<th>Variable</th>
<th>Coefficient</th>
<th>Std. Error</th>
<th>t-Statistic</th>
<th>Prob.</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \hat{\epsilon}_{1t-1} )</td>
<td>-0.300829</td>
<td>0.115390</td>
<td>-2.607060</td>
<td>0.0128</td>
</tr>
</tbody>
</table>

R-squared 0.145191 Mean dependent var 2.205344
Adjusted R-squared 0.145191 S.D. dependent var 293.3920
S.E. of regression 271.2583 Akaike info criterion 14.06811
Sum squared resid 2943242. Schwarz criterion 14.10990
Log likelihood -287.3962 Hannan-Quinn criter. 14.08333
Durbin-Watson stat 1.847711
### Table 4(b): Augmented Dickey-Fuller Test

Augmented Dickey-Fuller Test Equation  
Dependent Variable $\Delta \hat{\epsilon}_{t-1}$  
Method: Least Squares  
Sample (adjusted): 1971 2011  
Included observations: 41 after adjustments

<table>
<thead>
<tr>
<th>Variable</th>
<th>Coefficient</th>
<th>Std. Error</th>
<th>t-Statistic</th>
<th>Prob.</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\Delta \hat{\epsilon}_{t-1}$</td>
<td>-0.467489</td>
<td>0.119829</td>
<td>-3.901300</td>
<td>0.0004</td>
</tr>
</tbody>
</table>

- R-squared 0.273575  
- Mean dependent var 0.081744  
- Adjusted R-squared 0.2755  
- S.D. dependent var 1.554870  
- S.E. of regression 1.325225  
- Akaike info criterion 3.425129  
- Schwarz criterion 3.466924  
- Log likelihood -69.21515  
- Hannan-Quinn criter. 3.440349  
- Durbin-Watson stat 1.929877

The null hypotheses of no-cointegration or unit root are rejected in both models, implying that GDP and DI are cointegrated of order 1, 1 [i.e., GDP, DI $\subset CI(1,1)$]. This verifies there is a long-run equilibrium relationship between GDP and DI in Rwanda. Similar conclusions were also obtained using the Johansen cointegration test.

#### 3.4 Vector Error Correction Model (VECM)

We have found that GDP and DI are each I(1) and co-integrated of order 1,1. With cointegration present, there exists a dynamic interrelationship between the two variables with a disequilibrium correction error term given by the following VECM

\[
\Delta GDP_t = \alpha_{10} + \beta EC_{t-1} + \alpha_{11}\Delta GDP_{t-1} + \alpha_{12}\Delta DI_{t-1} + \varepsilon_{1t} \tag{9}
\]

\[
\Delta DI_t = \alpha_{20} + \beta EC_{t-1} + \alpha_{21}\Delta GDP_{t-1} + \alpha_{22}\Delta DI_{t-1} + \varepsilon_{2t} \tag{10}
\]

where $EC_{t-1}$ represents the error correction component of the model. The estimates of the vector error-correction model are as follows:

\[
\begin{align*}
\Delta GDP_t &= 63.46219 + 0.001022EC_{t-1} + 0.352458\Delta GDP_{t-1} - 29.93540 \Delta DI_{t-1} \\
t &= [2.13337] [0.01842] [1.78619] [-1.57162] \\
F(3,36) &= 1.264, \text{ Prob}(F\text{-statistic})=0.301
\end{align*}
\]
\[ \Delta DI_t = 0.296464 + 0.001528 EC_{t-1} + 0.001044 \Delta GDP_{t-1} - 0.074123 \Delta DI_{t-1} \]

\[ t = [1.01524] [2.80681] [0.53921] [-0.39643] \]

\[ F(3,36) = 3.259, \text{Prob}(F\text{-statistic})=0.0324 \]

The t-ratios on the coefficients of \( EC_{t-1} \), \( \Delta GDP_{t-1} \) and \( \Delta DI_{t-1} \) in the \( \Delta GDP \) equation are all individually insignificant. They are also collectively insignificant as indicated by the F-statistic. This implies that GDP does not respond to disequilibrium between itself and DI. The coefficient of \( EC_{t-1} \) in the \( \Delta DI \) equation is positive and statistically significant, suggesting that DI adjusts to GDP with a lag. Approximately 0.1528 percent of the discrepancy between long-term and short-term DI is corrected within the year. These results underscore the irrelevance of the GDP equation and the appropriateness of DI equation as was established by Granger causality tests in the next section.

### 3.5 Granger Causality

The Granger-causality tests investigate if a scalar "y" can help forecast another scalar"x". If it doesn’t, then we say that y does not Granger cause "x", Hamilton (1994). In other words, "y" does not help in predicting "x". Granger Causality test is generally sensitive to the number of lags adopted for the VAR model. Given that the assumptions in equations (1) and (2) hold, we investigated the following four possible cases of bilateral causality between GDP and DI, Gujarati and Porter (2009):

- **Unidirectional causality from DI to GDP** which is indicated if the estimated coefficients on the lagged DI in (1) are statistically different from zero as a group (i.e., \( \sum \beta_j \neq 0 \)) and the set of estimated coefficients on the lagged GDP in (2) is not statistically different from zero (i.e., \( \sum \alpha_i = 0 \)).

- Conversely, **unidirectional causality from GDP to DI** exists if the set of lagged DI coefficients in (1) is not statistically different from zero (i.e., \( \sum \beta_j = 0 \)) and the set of lagged GDP coefficients in (2) is statistically different from zero (i.e., \( \sum \alpha_i \neq 0 \)).

- **Feedback**, or **bilateral causality**, suggested when the sets of DI and GDP coefficients are statistically significantly different from zero in both regressions.

- Finally, **independence** suggested when the set of DI and GDP coefficients are not statistically significant in both the regressions.

Using OLS, the following steps were taken to test whether DI “Granger” causes GDP:

(i) Regress current GDP on lagged GDP excluding lagged DI. This gives the restricted regression which is used to obtain the restricted residual sum of squares \( RSS_k \).
Run regression (i) including lagged DI. This gives the unrestricted regression where we obtain the unrestricted residual sum of squares, \(RSS_{UR}\).

The null hypothesis is \(H_0: \sum \beta_j = 0\), that is, lagged DI terms do not belong in the regression. The null hypothesis in each case is that the variable under consideration does not “Granger cause” the other variable. In this case, DI does not “Granger cause” GDP.

The general test statistic is given by

\[
F = \frac{(RSS_R - RSS_{UR})/m}{RSS_{UR}/(n - (2m + 1))} \quad \text{or} \quad F[m, (n - (2m + 1))]
\]

where \(m\) is the number of lagged terms and \(n\) is the number of observations used to estimate the model\(^5\). If the p-value is less than 5%, we reject the null hypothesis that GDP does not Granger-cause DI. By rejecting the null hypothesis we accept that lagged DI belongs in the regression, another way of saying that DI causes GDP.

Steps (i) to (iv) can be repeated to test the model in equation (2), that is, whether GDP causes DI.

From these steps, the results of the bivariate Granger Causality test are summarized in Table 5.

<table>
<thead>
<tr>
<th>Null Hypothesis</th>
<th>Number of lags</th>
<th>(F) value</th>
<th>Prob.</th>
<th>Decision</th>
</tr>
</thead>
<tbody>
<tr>
<td>DI does not Granger Cause GDP</td>
<td>1</td>
<td>0.54720</td>
<td>0.4640</td>
<td>Do not reject</td>
</tr>
<tr>
<td>GDP does not Granger Cause DI</td>
<td>1</td>
<td>7.95147</td>
<td>0.0076</td>
<td>Reject at 5%</td>
</tr>
<tr>
<td>DI does not Granger Cause GDP</td>
<td>2</td>
<td>1.01294</td>
<td>0.3735</td>
<td>Do not reject</td>
</tr>
<tr>
<td>GDP does not Granger Cause DI</td>
<td>2</td>
<td>3.38214</td>
<td>0.0454</td>
<td>Reject at 5%</td>
</tr>
<tr>
<td>DI does not Granger Cause GDP</td>
<td>3</td>
<td>0.65607</td>
<td>0.5851</td>
<td>Do not reject</td>
</tr>
<tr>
<td>GDP does not Granger Cause DI</td>
<td>3</td>
<td>2.08297</td>
<td>0.1220</td>
<td>Do not reject</td>
</tr>
</tbody>
</table>

These results indicate a unidirectional causality from GDP to DI for the first two lags. Likewise, there is also no causality from DI to GDP for the two lags. However from lag three onwards, it was found out that there was no statistically significant causality from GDP to DI and vice versa. Since our lag selection is one, Rwanda like many other countries have been found to have a one way causality from GDP growth to DI growth,

\(^5\) Note that \((2m + 1)\) is the number of parameters estimated in the unrestricted regression. When the lags for the respective variables are different, \(m\) is divided into their components.
Choe (2003). Hence, policies towards GDP provide useful information for forecasting DI likely to be realized in Rwanda.

3.6 VAR Estimation
There is an issue of whether the variables in a VAR need to be stationary for estimation, Hamilton (1994). Some researchers recommend against differencing even if the variables contain a unit root. They argue that the goal of a VAR analysis is to determine the interrelationships among the variables, not the determination of the parameter estimates. The main argument against differencing is that it “throws away” information concerning the comovements in the data (such as the possibility of cointegrating relationships). Similarly, it is argued that the data need not be detrended. In a VAR, a trending variable will be well approximated by a unit root plus drift. However, the majority view is that the form of the variables in the VAR should mimic the true data generating process, Sims et al (1990). Taking into account these concerns our bivariate VAR (1) model was estimated in levels using equations (3) and (4) and the results are presented in table 6.

**Table 6: Vector Autoregression Estimates of GDP and DI**

<table>
<thead>
<tr>
<th>Sample (adjusted): 1971-2011</th>
<th>Included observations: 41 after adjustments</th>
</tr>
</thead>
<tbody>
<tr>
<td>Standard errors in ( ) &amp; t-statistics in [ ]</td>
<td>GDP</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>GDP(-1)</th>
<th>1.117271</th>
<th>(0.07207)</th>
<th>[15.5018]</th>
<th>0.001986</th>
<th>(0.00070)</th>
<th>[2.81983]</th>
</tr>
</thead>
<tbody>
<tr>
<td>DI(-1)</td>
<td>-11.26149</td>
<td>(15.2237)</td>
<td>[-0.73973]</td>
<td>0.492495</td>
<td>(0.14876)</td>
<td>[3.31073]</td>
</tr>
<tr>
<td>C</td>
<td>48.36127</td>
<td>(140.480)</td>
<td>[0.34426]</td>
<td>4.608133</td>
<td>(1.37268)</td>
<td>[3.35704]</td>
</tr>
</tbody>
</table>

| R-squared | 0.955859 | 0.773437 |
| Adj. R-squared | 0.953536 | 0.761513 |
| Sum sq. resid | 1075141. | 102.6545 |
| S.E equation | 168.2058 | 1.643604 |
| F-statistic | 411.4423 | 64.86199 |
| Log likelihood | -266.7515 | -76.99131 |

From the t-values the results show that lagged DI (including the constant term) in the GDP regression is insignificant (i.e., not different from zero. But all coefficients in the DI regression are individually significant at the 5% level. These results conform with those for the Granger causality tests which suggest the adoption of DI regression for forecasting.
3.7 VAR Stability

The regression equations of our estimated VAR (1) above in levels can be expressed as

\[
\begin{pmatrix}
GDP_t \\
DI_t
\end{pmatrix} = \begin{pmatrix}
48.36127 \\
4.608133
\end{pmatrix} + \begin{pmatrix}
1.117271 \\
0.001986
\end{pmatrix} \begin{pmatrix}
GDP_{t-1} \\
DI_{t-1}
\end{pmatrix}
\]

and define

\[
A = \begin{pmatrix}
1.117271 - 11.26149 \\
0.001986 0.492495
\end{pmatrix}.
\]

The estimated equations for the same model (output not shown) in first differences were found to be

\[
\begin{pmatrix}
\Delta GDP_t \\
\Delta DI_t
\end{pmatrix} = \begin{pmatrix}
63.51862 \\
0.380861
\end{pmatrix} + \begin{pmatrix}
0.352210 \\
0.000674
\end{pmatrix} \begin{pmatrix}
\Delta GDP_{t-1} \\
\Delta DI_{t-1}
\end{pmatrix}
\]

such that

\[
A_v = \begin{pmatrix}
0.352210 - 30.04025 \\
0.000674 - 0.230943
\end{pmatrix}.
\]

The stability of our VAR (1) model estimated in levels and first differences are determined using eigenvalue stability condition of matrices \(A\) and \(A_v\). By this condition, the eigenvalues of matrix \(A\) are 1.0792 and 0.53059, implying that GDP and DI estimated at levels are not stationary since at least one eigenvalue is approximately unity. However first difference estimation of the model shows that GDP and DI are stationary since all the eigenvalues of matrix \(A_v\) which are 0.315 and -0194 lie inside the unit circle.

3.7 Forecasting

For forecasting, the bivariate VAR(1) was re-estimated in levels for data covering the period 1970-2010. The data for 2011 was excluded for comparison of forecasted and actual values. Table 7 gives the results of the re-estimation of our model.
Table 7. Vector Autoregression of GDP and DI

<table>
<thead>
<tr>
<th>Included observations: 40 after adjustments</th>
</tr>
</thead>
<tbody>
<tr>
<td>Standard errors in ( ) &amp; t-statistics in [ ]</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th></th>
<th>GDP</th>
<th>DI</th>
</tr>
</thead>
<tbody>
<tr>
<td>GDP(-1)</td>
<td>1.106071</td>
<td>(0.07596)</td>
</tr>
<tr>
<td></td>
<td>[14.5616]</td>
<td>0.001978</td>
</tr>
<tr>
<td>DI(-1)</td>
<td>-10.83555</td>
<td>(15.3952)</td>
</tr>
<tr>
<td></td>
<td>[-0.70382]</td>
<td>0.492795</td>
</tr>
<tr>
<td>C</td>
<td>58.11948</td>
<td>(143.116)</td>
</tr>
<tr>
<td></td>
<td>[0.40610]</td>
<td>4.615025</td>
</tr>
</tbody>
</table>

R-squared: 0.945363 | Adj. R-squared: 0.740036
Sum sq. resid: 1067482. | S.E. equation: 102.6506
F-statistic: 320.0969 | Log likelihood: -260.5962

The DI regression equation for forecasting now becomes

\[
\hat{\text{DI}}_{2011} = 4.615025 + 0.001978\text{GDP}_{2010} + 0.492795\text{DI}_{2010}
\]

\[
\hat{\text{DI}}_{2011} = 4.615025 + 0.001978(3593.742) + 0.492795(22.1327) = 22.6303%.
\]

The forecasted value of DI in 2011 is 22.6303% of GDP while the actual value in 2011 was 22.7% of GDP. The difference between actual and forecasted is 22.7%-22.6303%=0.0697% which represents a small underprediction. This implies that GDP almost perfectly predicts DI in our bivariate VAR (1) model. The small difference between the actual and forecasted values in DI may be explained by the appropriate policy measures the Rwandan government and the private sector federation have so far taken to facilitate investors in their businesses. The World Bank reports on doing business have shown great improvement in the ranking of Rwanda since 2008, World Bank (2012).
Dynamic relationship between gross domestic product and domestic investment was analysed using time series data of Rwanda for period 1970 to 2011. A bivariate model with lag one selected and considered appropriate for the analysis. The Augmented Dickey-Fuller (ADF) tests and Phillips-Perron tests indicate that GDP and DI are not stationary at levels but their first differences were stationary, meaning that they are integrated of order one.

The Augmented Engle-Granger and Johansen tests of cointegration show that GDP and DI series are co-integrated. While GDP does not appear to respond to disequilibrium between itself and DI, the error correction model establishes that DI adjusts to GDP with a lag. Approximately 0.1528 percent of the discrepancy between long-term and short-term DI is corrected within the year.

Our analysis indicates a unidirectional causality from GDP to DI for the first two lags with no evidence of causality from DI to GDP. The unidirectional causality suggests that policies initiated towards GDP provide important information for predicting DI in Rwanda. The results of the estimation of the bivariate VAR together with those of Granger causality tests and error correction model underscore the irrelevance of the GDP equation and the appropriateness of DI equation in our adopted model.

Our estimated bivariate VAR (1) model was found to be stable in first difference, but not in levels. The forecasted value of DI in 2011 is 22.6303% of GDP while the actual value in 2011 was 22.7% of GDP. The difference shows that GDP can predict DI with small error of 0.0697%. The small difference between the actual and forecasted values in DI may be explained by the commendable policies the Rwandan government and the private sector federation have been pursuing in promoting investment in the country.

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References


