# SPATIAL AND TEMPORAL DISTRIBUTIONS OF IONOSPHERIC CURRENTS-1. ALTITUDE-LATITUDE CROSS SECTIONS OF EQUATORIAL ELECTROJET AND WORLDWIDE PARTS OF Sq CURRENT DENSITY

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### **ABSTRACT**

The first altitude-latitude cross section of worldwide part of Sq current density is reproduced. It is set at an altitude of 120 km and its current focus occurs at 35.7° latitude from the current centre. It depicts the tendency for most upper current layers observed by rockets to extend more below than above the altitude of peak current density. It also depicts the tendency of the return current streamlines of Chapman and Bartels (1940) to be equidistant towards the poles. The first altitude-latitude cross section of the equatorial electrojet (EEJ) current density on the continuous distribution of current density model based on a single data set is presented. It is set at an altitude of 106 km. It very much resembles the EEJ altitude-latitude cross section of Anandarao and Raghavarao (1979) from numerical model calculations using observed winds. The respective landmark values of the two EEJ cross sections are: peak current density jo at the current center 10.44 Akm<sup>-2</sup> and 8 Akm<sup>-2</sup>, at the altitude of 106 km the dip latitude w of current focus of 2.73° and 3°, the peak return current density j<sub>m</sub> of -2.41 Akm<sup>-2</sup> and -2.3 Akm<sup>-2</sup> occur at dip latitude x<sub>m</sub> of 5.13° and 6° and the latitudinal extent L<sub>1</sub> of return currents of 11.63° and 12° respectively.

Key words: Altitude-latitude cross sections, worldwide part of Sq (WSq), current density, dip latitude.

# 1. INTRODUCTION

The first presentation of the altitude-latitude cross section of the equatorial electrojet (EEJ) current density was done by Onwumechili (1965). However, owing to the lack of sufficient observed data for the determination of all the parameters of his continuous distribution of current density model, his altitude and latitude were in units of the scale lengths. This was followed by Sugiura and Cain (1966) who presented the altitude-latitude cross section of EEJ effective conductivity  $\sigma_{yy}$ .

Thereafter, a number of numerical model calculations (Untiedt 1967, Sugiura and Poros 1969, Krylov et al. 1973, Richmond 1973, Takeda and Maeda 1980,1981, Stening 1985, and Singh and Cole 1987) gave altitude-latitude cross sections of EEJ current density. The winds used in these calculations are hypothetical and some adopted arbitrary electric fields. As a result, only two of them showed some indication of the westward return currents on the flanks of the dip equator. However, when Anandarao and Raghavarao (1979, 1987) and Raghavarao and Anandarao (1987) used observed winds and electron density they reproduced the westward return current on the flanks. All its features are discussed here.

Davis et al. (1967) attempted altitude-latitude cross section of EEJ current density with altitude profiles of current density measured by rockets. This would have been ideal but unfortunately there were only 9 launching stations. More regrettably, there was no

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measurement from about 240 km to 800 km dip distance. The region of westward return current and its interesting features were therefore omitted. The extrapolations into this region were therefore unrealistic.

Empirical models derived their parameters by fitting observations and then they proceed to extrapolate with the model. They are therefore anchored on observational data provided they fit observations well. Unfortunately, nearly all empirical models so far used are thin current shell models. They cannot provide altitude-latitude cross section because they take no account of the altitude distribution of the current.

However, the continuous distribution of current density model (Onwumechili 1965) provides for altitude distribution of current density and therefore has the capability to produce altitude-latitude cross section of current density. The altitude-latitude cross section of Onwumechili and Ozoemena (1989) based on this model, however derived the altitude parameters from rocket measurements and the latitudinal parameters from satellite magnetic variation measurements. Therefore the two sets of parameters do not refer to the same ionospheric current.

This paper presents altitude-latitude cross section of EEJ current density based on latitudinal and vertical parameters derived from an autonomous data set. The cross section therefore refers to an autonomous ionospheric current. The paper also presents the first altitude-latitude cross section of worldwide part of Sq (WSq) current density.

#### 2 THEORETICAL CALCUALTIONS.

### (a) ALTITUDE-LATITUDE CROSS SECTION

For the continuous distribution of current density model. The eastward current density j(x, z) at the point (x, z) is given by:

$$j = j_0 \frac{a^2(a^2 + \alpha x^2)}{(a^2 + x^2)^2} \frac{b^2(b^2 + \beta z^2)}{(b^2 + z)^2}$$

where x is northwards, y is eastwards and z is downwards; the origin is at the center of the current x=0=z; a and b are constant scale lengths along x and z respectively;  $\alpha$  and  $\beta$  are dimensionless constants controlling the current distribution latitudinally and vertically respectively; and jo is the peak current density at the current center.

In geocentric spherical polar coordinators [(R + r),  $\phi$ ,  $\lambda$ ] the model is

$$j = j_0 \frac{a^2(a^2 + \alpha \phi^2)}{(a^2 + \phi^2)^2} \frac{b^2(b^2 + \beta r^2)}{(b^2 + r^2)^2}$$

where R is the radial distance to the center of the current,  $\phi$  is southward latitude from the center of the current,  $\lambda$  is eastward longitude, and a is a constant scale latitude.

Since Eqs.(1) and (2) are essentially the same, we may in general use Eq.(1). When a and x are in degrees, it refers to geocentric polar coordinates but when a and x are in km, it refers to Cartesian coordinates.

The cross section is presented as contours of equal current density j Akm<sup>-2</sup> on the (x, z) plane at a given local time. We therefore need expressions for the coordinates of the point with current density j.

We may rewrite Eq.(1) as

$$p = \frac{(1 + \alpha r^2)}{(1 + r^2)^2} \frac{(1 + \beta s^2)}{(1 + s^2)^2}$$

where  $p = j/j_0$ , r = x/a and s = z/b.

For points along the x axis, s = 0 = z. The solution for r and x from the resulting equation.

$$p = \frac{1 + \alpha r^2}{\left(1 + r^2\right)^2}$$

is: 
$$x^2 = a^2 \left[ (\alpha - 2p) \pm \sqrt{(\alpha - 2p)^2 - 4p(p-1)} \right] / 2p.$$
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For points along the z axis, r = 0 = x. The solution for s and z from the resulting equation

$$p = \frac{1 + \beta s^2}{\left(1 + \alpha r^2\right)^2} \tag{6}$$

is: 
$$z^2 = b^2 \left[ (\beta - 2p) \pm \sqrt{(\beta - 2p)^2 - 4p(p-1)} \right] / 2p$$

For the general case we rewrite Eq.(3) as

$$q = p \frac{(1+r^2)^2}{1+\alpha r^2} = \frac{1+\beta s^2}{(1+s^2)^2}$$

We choose r or x = ar and calculate q for given p. Then the solution for s and z is

$$z^{2} = b^{2} \left[ (\beta - 2q) \pm \sqrt{(\beta - 2q)^{2} - 4q(q - 1)} \right] / 2q$$

Some landmark positions also help. At the current foci

$$j = 0 = p$$
,  $x^2 = w^2 = -a^2/\alpha$ .

At xm where the return current peaks as im we have

$$j_m = j_0 \alpha^2/4(\alpha - 1)$$
.  $X_m^2 = a^2(\alpha - 2)/\alpha$ .

From the above analysis, the altitude-latitude cross section is easily constructed provided we know the values of the parameters:  $j_0$ , a,  $\alpha$ , b and  $\beta$ . These are obtained from least square fitting of observational data with the model for the selected local time. Then choosing a current density like 2 Akm<sup>-2</sup> or -1 Akm<sup>-2</sup>, its contour is calculated from the above equations.

The current intensity J Akm<sup>-1</sup> and the total forward current I<sub>F</sub> amperes are independent of altitude. Therefore, they cannot have altitude-latitude cross section.

# (b) ALTITUDE-LATITUDE CROSS SECTION OF WORLDWIDE PART OF Sq (WSq) CURRENT DENSITY

So far there is no determination of  $j_0$ , a,  $\alpha$ , b and  $\beta$  from the same data set of worldwide part of Sq (WSq). We are therefore compelled to combine the latitudinal parameters a and  $\alpha$  from ground-based geomagnetic variation observations with the vertical distribution parameters  $j_0$ ,b and  $\beta$  from rocket measurement for the purpose of producing the first altitude-latitude cross section of WSq current system. Onwumechili (1967) obtained five concordant values of each parameter a and  $\alpha$  from the recordings of worldwide distribution of observatories. Their means are  $a=63^\circ$  and  $\alpha=-3.11$ . Their worldwide origin makes them preferable to the  $a=63^\circ$  and  $\alpha=-3.14$   $\pm$  0.17 from the Indian sector alone.

Onwumechili (1992a) determined the vertical parameters j<sub>0</sub>, b and  $\beta$  from altitude profiles of WSq current density measured by rockets. The peak current density j<sub>0</sub> = 2.37  $\pm$  0.38 Akm<sup>-2</sup>.

He determined two sets of the parameters b and  $\beta$  because the profile is not symmetrical about the altitude of the peak current density. For the lower part of the profile below the altitude of the peak current density  $b_1=6.59\pm2.18$  km and  $\beta_1=0.234\pm0.32$ , and for the upper part of the profile above the altitude of the peak current density  $b_2=7.09\pm2.47$  km and  $\beta_2=0.021\pm0.35$ .

Onwumechili (1992b) showed that the altitude of the peak current density of WSq was higher close to the dip equator than elsewhere. The rockets found that from 7° to 77° latitude, the mean altitude of the peak current density of WSq was  $118\pm7$  km with a median of 118 km. When weighted by the range of latitude in which an altitude occurs, the mean from 0° to 77° latitude is  $117.6\pm5.5$  km. For the purpose of constructing the altitude-latitude cross section of WSq current density we adopt a peak current density of  $j_0=2.5$  Akm<sup>-2</sup> at an altitude of h=120 km.

With the above parameters the altitude-latitude cross section of the WSq current system shown in Fig. 1 was calculated and plotted as described in section 2 above. It may be noted that the latitudes are full scale latitudes measured from the current axis. It is also noted that the contours extend more below than above the altitude of 120 km. This is due to the differences of b1 and  $\beta_1$  from  $b_2$  and  $\beta_2$ , which thus preserves the lack of symmetry of the altitude profile of current density about the altitude of the current density peak. Ultimately, this arises from the interaction of the upper current layer (WSq layer) and the eastward lower current layer (EEJ layer) which often stretches the lower part of the upper current layer.

Contours are given for the current densities of 2, 1.5, 1, 0.5, 0.1, -0.1, -0.5, and -1  $Akm^2$ . The total altitude extent of the 0.5  $Akm^2$  contour is about 17 km, in accord with the total altitude extent of  $18 \pm 3$  km for the upper current layer observed by rockets (Onwumechili 1992b). The rocket may not easily detect less than 0.5  $Akm^2$ . The forward current decreases to zero at the focus,  $35.7^\circ$  latitude from the current center. From there the return current grows from zero to a peak of about -59 percent of the peak of forward current at the current center. This ratio is about double the ratio for EEJ because the return current in Fig. 1 covers about

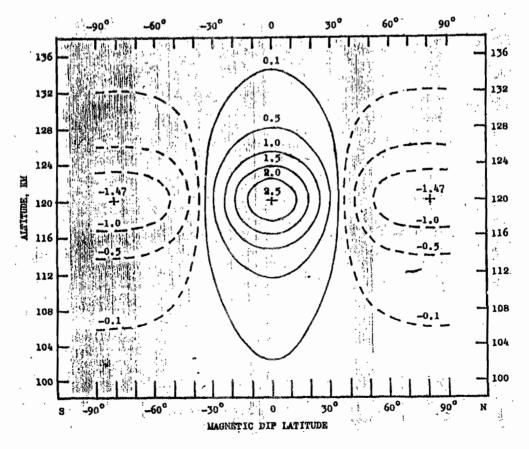


Fig. 1 Altitude-latitude cross section of worldwide part of Sq current density j Akm<sup>-2</sup>. Continuous contours are for forward current densities of 2.0, 1.0, 0.5 and 0.1 Akm<sup>-2</sup>, and broken contours are for return current densities of -1.0, -0.5 and -0.1 Akm<sup>-2</sup>. Crosses mark the peak forward current density of  $j_0 = 2.5$  Akm<sup>-2</sup> and the peak return current density of  $j_m = -1.47$  Akm<sup>-2</sup>.

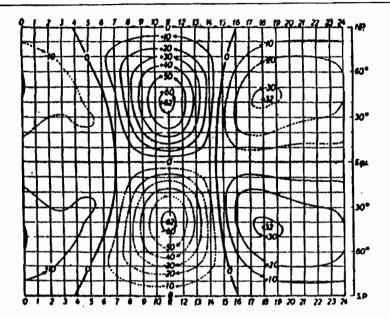


Fig. 2. Worldwide map of the ionospheric current systems corresponding to the solar daily geomagnetic variations in the equinoxes of the sunspot minimum year 1902. The meridians refer to local time, 12 = noon. Between consecutive streamlines, 10,000 A flow. Solid lines are for counter-clockwise and broken lines are for clockwise directions. After Chapman and Bartels (1940), p.229)

twice the area of the forward current whereas in the case of the EEJ the return current covers about four times the area of the forward current.

The return current contours rise quickly in altitude and then tend to maintain fairly steady altitude. This fairly steady altitude explains the tendency for return current streamlines to appear equidistant from shortly after the focus towards the poles. This may be seen in Fig. 2 from Chapman and Bartels (1940). The current terminates in latitude when all the forward current returns. At this latitude, all the return current density contours need not close. This explains why the return current density contours remain open in fig. 1

### ALTITUDE - LATITUDE CROSS SECTION OF EQUATORIAL (c) ELECTORJET (EEJ) CURRENT DENSITY

Fortunately, in the case of the equatorial electorjet (EEJ), Onwumechili and Ezema (1992) have determined the necessary parameters:  $j_{\alpha}$ ,  $\alpha$ , b and  $\beta$  from an autonomous data set. For the altitude-latitude cross section of the EEJ current density at local noon we adopt their values of jo = 10.44 Akm<sup>2</sup>, a =  $3.37^{\circ}$ ,  $\alpha$  = -1.5274, b = 8.845 km,  $\beta$  = 0.5253. Rockets determined the altitude of the EEJ peak current density as h = 106 km (Onwumechili 1992c). With these values the altitude-latitude cross section of the EEJ current system in fig. 3 The continuous contours are for was calculated and plotted as described in section 2 above. the eastward current densities of 10, 8, 6, 4, 3, 2, 1, 0.5 and 0.1 Akm<sup>-2</sup>, and the broken contours are for the westward return current densities of -2, -1,-0.5 and -0.1 Akm<sup>-2</sup>. For hours outside local noon the cross section has the same pattern as Fig. 3 but the current density is normally lower everywhere.

At a given altitude, the eastward current density peaks at the dip equator. From the peak the current density decreases to zero at a focus on either side of the dip equator. At the altitude of 106 km the focus occurred at  $w = 2.73^{\circ}$  dip latitude. Beyond the focus, westward return currents commence tenuously and increase to a peak  $j_m$  at the dip latitude of  $x_m = 5.13^\circ$ .

The percentage ratio of the peak return to the peak forward current density 100jm/jo = 23.12. The peak forward current density of 10.44 Akm<sup>-2</sup> and the peak return current density of -2.41 Akm<sup>-2</sup> are marked with crosses. Beyond that latitude the current density decreases towards zero. The current terminates at dip latitude of  $L_1 = 11.63^{\circ}$ , by which latitude all the eastward current has returned. Therefore some return current contours are not closed as in the

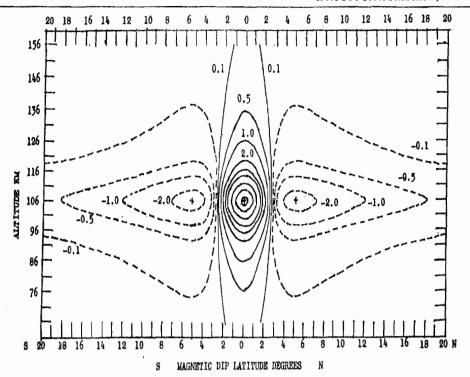


Fig. 3 Altitude-latitude cross section of equatorial electrojet current density j Akm<sup>2</sup> at local noon. Continuous contours are for the eastward current densities of 10, 8, 6, 4, 2, 1, 0.5 and 0.1 Akm<sup>2</sup>, and broken contours are for the westward return current densities of -2, -1, -0.5 and -0.1 Akm<sup>2</sup>. Crosses mark the peak forward current density of j<sub>0</sub> =10.44 Akm<sup>2</sup> at the centre and the peak return current density of j<sub>m</sub> = -2.41 Akm<sup>2</sup> at x<sub>m</sub> =5.13°dip latitude. The focus is at w = 2.73° dip latitude and the return currents extend to L<sub>1</sub>=11.63° dip latitude.

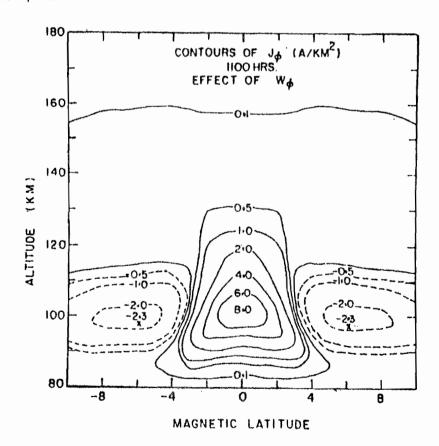


Fig.4 Altitude-latitude cross section of equatorial electrojet current density  $J_0$  Akm<sup>2</sup> at 1100 hour local time calculated with observed eastwest wind  $W_0$ . Continuous contours are for eastward current densities and broken contours are for westward current densities. The peak forward current density  $j_0 = 8 \text{Akm}^2$  at the centre and crosses mark the peak return current density of  $j_m = -2.3 \text{ Akm}^2$  at  $m_m = -6^0$  magnetic latitude. At the altitude of 106 km the focus is at  $m_m = 3^0$ . The return currents extend to  $L_1 = 12^0$  magnetic latitude. After Anandarao and Raghavarao (1979)

case of WSq current contours. Indeed Fig. 3 has been extended far beyond the latitudinal extent of the return currents.

The numerical model calculations of Anandarao and Raghavarao (1979) using observed winds and electron density resulted in the altitude-latitude cross section of EEJ in Fig. 4. Within the same latitude range of  $\pm 10^{\circ}$ , Fig. 3 resembles Fig. 4 Indeed, their features are very much in agreement. At the altitude of 106 km, the current focus of Fig. 4 is at  $3^{\circ}$  latitude. The peak return current  $j_m$  of =2.3 Akm<sup>-2</sup> in Fig. 4 occurs at  $x_m=6^{\circ}$  latitude, indeed Anandarao and Raghavarao (1979) say at  $5^{\circ}$  latitude. Their percentage ratio of the peak return to the peak forward current density is  $100j_m/j_0=\pm 20.75$ . Raghavarao and Anandarao (1997) state that the return currents extend to latitude of  $L_1=12^{\circ}$ . The comparison of the features of Figs. 3 and 4 above evidences their remarkable similarity.

### 3

### CONCLUSIONS

The first altitude-latitude cross section of worldwide part of Sq (Wsq) current density has been reproduced with latitudinal parameters derived from ground-based geomagnetic variation measurements and vertical parameters derived from current density altitude profiles measured by rockets. The peak current density is at an altitude of 120 km and the WSq current focus occurs at 35.7° latitude from the current center. It depicts the current as extending more below than above the aititude of the peak current density as a result of interaction with the lower current layer. It also depicts the tendency of the return current streamlines of Chapman and Bartels (1940) to be equidistant towards the poles.

The first altitude-jatitude cross section of the equatorial electrojet (EEJ) current density on the continuous distribution of current density model based on one data set has been presented with both latitudinal and vertical parameters derived from the POGO satellites data. It is set at an altitude of 106 km. The peak current density jo = 10.44 Akm<sup>-2</sup> at the current centre and the focus occurs at w = 2.73°. The peak return current density jm = -2.41 Akm<sup>-2</sup> at  $x_m = 5.13°$  and the latitudinal extent of the current system is  $L_1 = 11.63°$  dip latitude.

The altitude-latitude cross section of the equatorial electrojet current density of Anandarao and Raghavarao (1979) from numerical model calculations using observed winds and selection density very much resembles the cross section described in 2 above. Its peak current density jo =  $8 \text{ Amk}^{-2}$  at the current centre and the focus at 106 km altitude occurs at  $w = 3^{\circ}$ . The peak return current density  $j_m = -2.3 \text{ Akm}^{-2}$  at  $x_m = 6^{\circ}$  and the latitudinal extent of the current system is  $L_1 = 12^{\circ}$  magnetic latitude.

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