THE STRUCTURE OF INTRA-URBAN ROAD NETWORK DEVELOPMENT IN ILORIN, NIGERIA

A. J.ADERAMO

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ABSTRACT

The paper describes the structure of road network development in llorin between 1963-1999. This was done by determining the network pattern of the city for the study period and identifying some socio-economic variables considered to be responsible for road network development to build models of network structure.

Data on road network pattern of the city were acquired through mapping from sequential aerial photographs and land use maps of llorin. Data on socio-economic variables considered to be responsible for road network development were collected from State Ministries, Parastatals, Local Government offices and National Population Commission.

Using graph theoretic concept measures of network development for the city were determined. Multiple Regression procedure was then used to develop models of the structure of road network development of the city.

The results showed that the identified socio-economic variables are important in the explanation of road network development in llorin.

Key words: Ilorin, Road network development, graph theory, Socio-economic variables, Road network structure.

INTRODUCTION

Road Network development connotes changes in the structure of transportation network over time. These changes are brought about as a result of the need for additional links in the network or the expansion of existing network systems. Such developments require capital investments by governments in order to satisfy the transportation needs of the society.

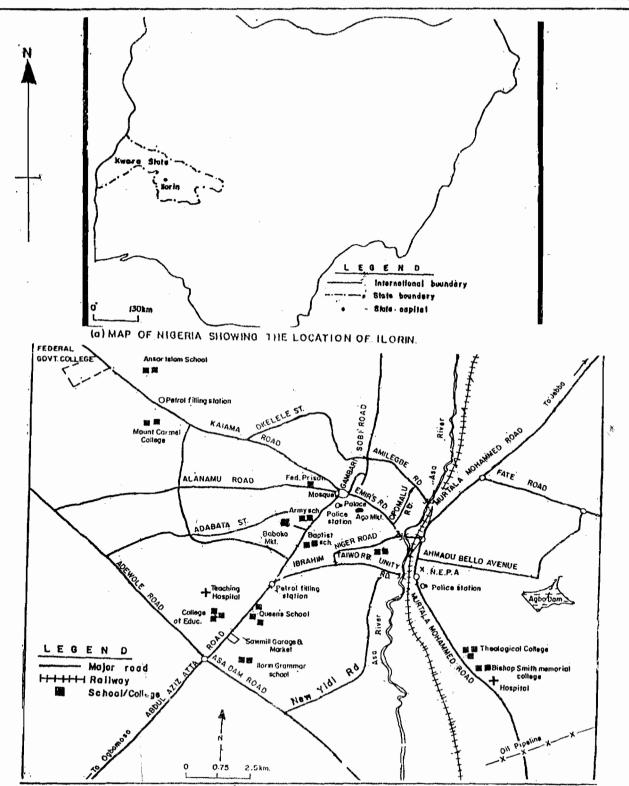
Various methods have been used to study the structure of transportation networks. These include the morphological approach (Appleton, 1967); the functional approach (Garrison and Marble 1965); and the topological approach (Kansky, 1963). However, the topological approach using graph theoretic concepts has been more widely used. Graph theory is a method of understanding, representing and manipulating spatial structure and in this respect it differed considerably from other thrusts in the quantitative

revolution (Tinkler, 1979). According to Harvey (1969), graph theory is an important descriptive device in the analysis of the structure of systems.

One of the advantages of graph theory is its relative simplicity. Garrison (1960) recognized this relative simplicity of graph theory and its ability to look at the system as a whole or to look at individual parts of it in terms of the whole.

According to Tinkler (1979), a major attraction of graph theory is the radical simplification it is possible to achieve.

Graph theoretic methods have been widely used in transport geography at both regional and intra-urban levels. Garison (1960) used graph theory to model the accessibility and connectivity of regional highway networks in the United States. Burghat (1969) also applied graph theoretic concepts to analyse the development of road network of the Niagara Penisula, Ontario (see also Carter, 1969; Haggett and Chorley 1969).



(b)MAP OF ILORIN (THE STUDY AREA). Fig.I. Map showing the study area.

On nodal analysis, Nystuen and Dacey (1961) determined functional connections between Central places in the state of Washington based upon communication flows in a network with the help of graph theoretic concept (see also Soja, 1968, Clayton, 1977; Cates 1978). Wood (1975) also used graph theoretical concepts to examine the functional structure and integration of rural markets in Kisii District, Kenya and found a highly connected nature of the marketer and trader network.

Kansky (1963) made simple structural analysis of regional networks using graph theory and found that a direct correlation exists between transport facilities and levels of economic development (see also Lowe and Moryadas, 1975; Tinkler, 1977a).

In an application of graph theory for assessing the effect on intra-urban accessibility of interstate highways in Columbus Indianapolis, U.S.A, Muraco (1972) found the existence of spatial regularities in their pattern of accessibility. Also, Ogunsanya (1986) using graph theoretic approach in network flow estimation for Barnsley, U.K., concluded that graph theory would prove useful in network structure identification at the intra-urban level. These studies affirm the utility of graph theory in the analysis of transportation networks and its applicability at both regional and intra-urban levels. This study applies graph theory to Ilorin, a medium-sized city in a developing country, Nigeria. The objective is to show the applicability of this useful quantitative technique in transport geography in identifying the structure of intraurban road network development in a developing environment.

STUDY AREA

The study area is Ilorin the Kwara State Capital. It is located on latitude 8° 30' North and longitude 4° 35' East. (fig!1). The creation of Wara State in 1967 and the choice of Ilorin as the State capital has resulted in its rapid population increase and area expansion. Over the years, the city has grown from what can be described as a "foot-city" with residential houses

located around the Emir's palace to an automobile city.

The development of intra-city roads to cope with the demand of the city when it became a state capital has affected the spatial expansion of the city. Thus developments have concentrated along the routes. The growth of the city has been in terms of physical expansion and growth of traffic The Western section of the city which is predominantly residential generates a lot of traffic daily which have to go through the three bridges linking the West and East. This creates a condition which makes traffic concentrate on and overstrech such routes as Emirs road, Taiwo and Unity roads and Michael Ibru road.

The location of markets and other centres of commercial activities in the city also act as traffic generation points and has significant effect on the city's traffic pattern. The distribution of various other land uses such as institutional, public and semi-public buildings, industrial and recreational all sum up to dictate the pattern of city traffic and route expansion. The study of road network development in llorin can serve as a guide for similar studies in other urban centres in developing countries.

TOPOLOGICAL ANALYSIS OF TRANSPORT NETWORKS

In graph theoretic applications of transport network, locations or points are interpreted as nodes or vertices while the routes are links or edges. In the regional scale application of graph-theoretic technique, settlements are taken as nodes and the routes as links in a network.

In the intra-urban application however, the nodes are considered as intersections or junctions and the roads as links in the network. This allows for the abstraction of an urban road network as a graph for the determination of its structural pattern.

In using the graph theory, various indices have been suggested (See Kansky, 1963). In this work however the indices used are:

a. Alpha index, defined as the ratio between the actual number of loops in a graph and the maximum possible number. The range

of the alpha index is from 0 to 1.0 indicating absolute non-connectivity to perfect connectivity.

b. Beta index, defined as the number of linkages per place or node and measures the linkage intensity. The range of the beta index is from 0.5 for minimally connected graph and 3.0 for maximally connected graph.

c. Gamma index, defined as the ratio between the number of edges in a network and the maximum possible number of edges in the graph. The limits of the gamma index are 0 and 1.0 indicating non-connectivity to maximal connectivity.

Although these simple indices have limitations, vet when used properly, they have a lot of usefulness (Monmonier, 1972; Royaltey et al 1975). The utility of the indices stems from their ability to provide a yardstick of comparability for transportation networks (Tinkler, 1979). Besides, the measures are useful in evaluating not only the accessibility of nodes but also the connectivity of networks (Lowe and Moryadas 1975). Also, such topological indices are very useful indicators of development in terms of achievement economic in general technological achievement in particular (Leung, 1982).

However, the indices have limitations for sophisticated purposes. James et al (1970) found out that the indices do not discriminate adequately between networks of different sizes. Also, Lowe and Moryadas (1975) noted that not all the indices can be modified to accommodate physical or economic distance. But if one's interest is in studying the geographic or structural properties of a network, physical distance between vertices is not of much importance and therefore may be ignored.

DATA COLLECTION STRATEGY AND METHODOLOGY

The data required for this study are the road network pattern of the city for 1963, 1973, 1982, 1988, 1991, 1997, 1999, and the socio-

economic variables considered to be responsible for network developments.

In the original works of Kansky (1963), a relationship was found to exist between the structure of transportation networks and the economic characteristics of an area. Indeed, areas with highly developed economies were expected to have well-developed networks while areas that were economically less developed exhibited simple transportation networks. Using this notion, a multiple regression equation can be formed using indices of network structure as dependent variables while the socio-economic factors served as independent variables. In this study, the socio-economic variables identified and used as independent variables are Population of the city; Land use, Commercial development, provision of amenities, land speculation and transportation. Our choice of these variables is strengthened by the assertion of White and Senior (1983) that the existence of economic activities will create a demand for transport. This is because locations of population and of commercial and industrial activities create a demand for transport to close the gap between them. As some of these variables cannot be measured directly, surrogate measures were used for them. The choice of a surrogate measure for any socio-economic variable depends on the problem of study. An important requirement of the variables however, is that they must be easily measurable and that they are projectable as aid to forecasting.

The first independent variable is the population of the city. Rapid population growth is a common phenomenon in urban centres of Nigeria. The effect of continuos urban population growth is that demand for transport services is very high (Ikya, 1993). Thus population growth has been chosen as a factor of transport development. As for measurement procedure, most population figures used for planning purposes rely on census information and their projections. The population census figures for llorin for 1963 and 1991 and their projections were used.

The second explanatory variable is transport demand. Transport demand is

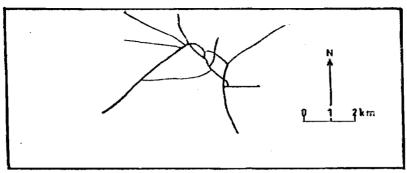


Fig. 2 Road network pattern of Norin, 1963.

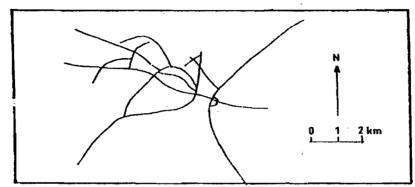


Fig 3 Road network pattern of Itorin, 1973.

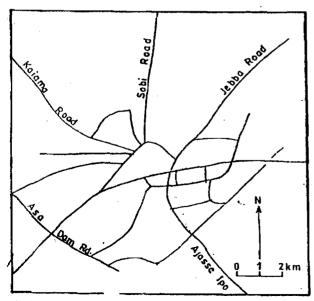


Fig.4 Road network pattern of Itorin, 1982.

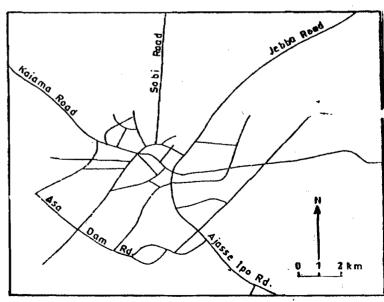


Fig. 5 Read network pattern of Itorin, 1988.

considered a key factor in city development since transportation is a catalyst of urban development. As for measurement of transport demand Maunder (1982) had found out in a study of bus operations in Delhi, India that transport demand is a function of income level, car ownership and personal preferences (see also Abdullahi 1998). He thus, used per capita income as a surrogate for transport demand. In this study per capita income has also been used as a surrogate of transport demand.

The third variable is landuse. The intimate relationship between transportation and landuse is acknowledged by the fact that at the heart of every city's master plan is a long-run transportation network (Bland, 1992): As for measurement of landuse, Stakie (1967) found that a relationship exists between a landuse type and the number of people employed in his study of traffic generation in Medway towns in Great Britain. He therefore used employment size to measure landuse. Employment size has also been used here as surrogate for landuse.

The fourth explanatory variable is land speculation. This entails the with-holding of land for development in anticipation of future high land prices. This type of growth process permits a sprawl pattern usually found along transportation routes (Clark, 1965). As for measurement of land speculation, Clawson (1962) had suggested that when land comes within the zone of suburban influence for possible later development its prices and taxes often rise. A reasonable surrogate for land speculation is thus the changing cost of land. This study therefore used the average cost of land in llorin as surrogate for land speculation.

The fifth variable is commercial is considered development. This important development because transport promotes commercial activities. As for measurement of commercial development, Krakover (1982) in a study of spatial reorganization of growth in urban fields in Eastern United States had used the number of employees in retail activity as surrogate measure for commercial development. In this study data on employment in retail trade in Ilorin was also used as proxy for commercial development.

The sixth variable is provision of amenities

in the city. The extension of social amenities to different parts of an urban area is facilitated through transport provision. Also urban dwellers seek housing environments which accessibility to urban facilities. As for measurement of social amenities, Berry (1961) used 43 indices for 95 countries in order to measure the degree of economic development of those countries. These include consumption, electricity consumption. per capita, exports per capita and similar indices Pred (1976) however suggested that composite as well as single-dimensional variables can also be used. This study uses primary school enrolment as surrogate measure for social amenities in the city. This is because in Nigeria primary education is free and universal while secondary and tertiary education are optional.

The data used were collected from various primary and secondary sources. Data on road network pattern for 1963, 1973 and 1982 were extracted from aerial photographs of llorin on scales 1:12,000, 1:10,000 and 1:6,000 respectively. The 1982 aerial photograph was updated through field survey conducted by the author in 1988 to obtain the network pattern for 1988 (See Aderamo, 1998). The network patterns for 1991, 1994, 1997 and 1999 were obtained from records of the Kwara State Ministry of Lands and Housing. Only the major roads were extracted for the study. (figs .2 - fig.9).

Data on population, were collected from National Population Commission; data on per capita income, total employment and manufacturing employment were collected from the State Ministry of Economic Development while data on schools enrolment were collected from the State's Schools Board and Ministry of Education. Data on cost of land were obtained from records of Ilorin West Local Government. These were used as input variables for the socioeconomic indices of network development.

MODELLING INTRA-URBAN NETWORK DEVELOPMENT FOR ILORIN

The modeling of network development for llorin can be conceptualized to take the following general form:

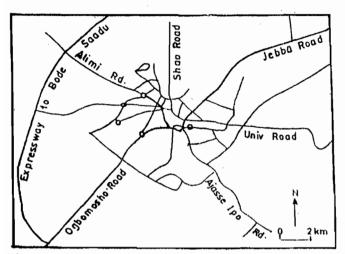


Fig. 6 Road network pattern of Itorin,1991.

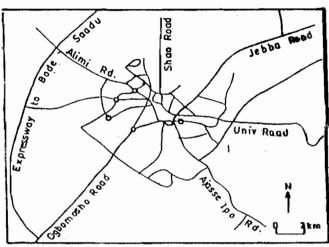


Fig. 7 Road network pattern of Itorin, 1994.

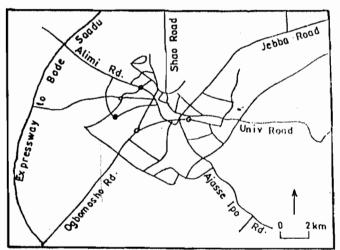


Fig & Road network pattern of Itorin, 1997.

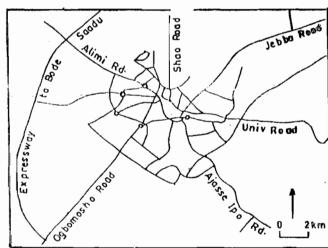


Fig. 9 Road network pattern of Itorin, 1999.

$$Y=F(X_1,X_2,....X_n)$$
....(1)

Where Y= Measures of Network Structure and

X₁,X₂,.....X_n are measures of socio-economic variables considered as factors of network development.

The model for our specific case is of the form

$$Y=F(X_1,X_2,X_3,X_4,X_5,X_{6_1})$$
 (2)

Where Y= Measures of Network Structure (Alpha index; Beta index; Gamma Index).

 X_1 is the Population of the city; X_2 is transportation demand; X_3 is land use control; X_4 is land Speculation; X_5 commercial development; X_6 social Amenities.

This can be made operational in the form

$$Y = a + b_1 X_1 + b_2 X_2 + b_3 X_3 + b_4 X_4 + b_5 X_5 + b_6 X_6 + e_1 (3)$$

RESULTS /

Table 1.0 shows the topological measures of network structure for the city from 1963-1999

TABLE 1.0 TOPOLOGICAL MEASURES OF NETWORK STRUCTURE FOR ILORIN (1963-1999)

Indices	1963	1973	1982	1988	1991	1994	1997	1999
œ	0.2381	0.3143	0.2824	0.2581	0.2323	0.2130	0.2056	0.2202
B	1.3077	1.5000	1.5111	1.4694	1.4231	1.3889	1.3750	1.4035
γ	0.5151	0.5556	0.5271	0.5106	0.4933	0.4808	0.4753	0.4848

Source: Authors Data Analysis 1999

TABLE 2.0 REGRESSION SUMMARY FOR 'ALPHA INDEX'

Dependent variable	Independent variables	Parameters estimates	Multiple R	R-Square
Alpha index	X ₄	-0.004818	-0.6789	0.4609
The state of the s	X ₂	0.002178	-0.7099	0.5039
magamatan ya ya ya ya safari kata da Amaganda saka dan da Ari A	X ₁	-0.001442	-0.7105	0.5048
PP from the Property of the State of the Sta	X ₅	0.016999	-0.7232	0.5229
	X ₆	-0.003396	-0.7468	0.5577
the same and the s	X ₃	-0.003975	0.7485	0.5602

Where a is the intercept, b_1 , b_2 , b_3 , b_4 , b_5 , b_6 are parameters determined by empirical evidence and e is the error term which explains the effects of the unspecified variables.

The structural indices of network and the socio-economic variables were used as dependent and independent variables for the period 1963-1999.

These were used as inputs into the regression models. Table 1.0 shows the structural indices of the city's network for the studied period, while figures 2.0 9.0 show the network patterns.

The topological measures of network structure for llorin show the progressive development of the city's network over the years. The pattern shows that the city's network experienced significant growth between 1963 and 1973. This can be attributed to the fact that within this period, llorin grew from being a Provincial headquarters to a State headquarters when special attention was paid to the construction of new roads and the improvement of existing ones.

Between 1973 and 1982, there was still some attention paid to the development of intraurban road network but the stringent measures being adopted by government in respect of funds being allocated to all sectors of the economy affected road construction. The pattern of changes in the network between 1982 and 1988 is a clear indication of the general state of the country's economy. In subsequent years to date, various economic reforms introduced by successive governments in Nigeria significantly affected all sectors of the country's economy including the transport sector (Taiwo, 1992). Although some links were added to the city's network between 1988 and 1999 the growth of the network had been at a very slow pace.

The initial rapid growth experienced by the city's network was also commensurate with the city's rapid expansion. As the city's expansion slowed down, there was also a decline in road construction.

The data on table 1.0 and on socioeconomic variables were used as input for the multiple regression analysis using the SPSS (Statistical Package for the Social Sciences). The indices alpha (x) Beta (β) , Gamma (γ) were used separately as dependent variables which resulted in obtaining three (3) multiple regression equations. Tables 2.0, 3.0 and 4.0 show the regression summaries for the 3 models.

Regression constant =0.639316; Coefficient of determination for all variables R^2 =0.9961. Adj - R^2 =0.9727. Regression equation is

 $Y=0.639316-0.00442X_1+0.002178X_2-0.003975X_3$ -0.004818 $X_4+0.01699\ X_5$ -0.003396 X_6

Table 2.0 shows that all the six independent variables have strong negative correlation coefficients with the dependent variable. The correlation coefficients range from - 0.6789 for X_4 (Land speculation) to -0.7099 for X_2

(Transportation); - 0.7105 for X_1 (Population); - 0.7485 for X_3 (Land use). Thus there is very strong direct but negative relationship between alpha index which is an index of network development with all the six identified independent variables.

Further the combined variables explain 97.27% of the total variation in the dependent variable with all of them significant at 0.15 level of significance, and can be used with any degree of confidence in the explanation of the development of intra-urban network in Ilorin.

Regression constant =2.283763,. Coefficient of Determination for all variables R^2 = 0.9959. Adj - R^2 = 0.9714. Regression equation is: Y=2 283763-0.004017X₁+0.005793X₂ -0.009321X₃ -0.009354X₄ + 0.043102X₅ -0.007493X₆.

Tables 3.0 shows that many 1 of the explanatory variables have weak relationships with the dependent variable. For instance, X_4 (Land peculation) has correlation coefficient of 0.3936 with the dependent variable. All the other explanatory variables have coefficient of correlations ranging from -0.1369 for X_2

(Transportation) to -0.1522 for X_6 (Social amenities); -0.1904 for X_1 (Population); -0.2291 for X_3 (Land use) and -0.2489 for X_5 (Commercial development). This implies that a weak relationship exists between the Beta index and the identified socio- economic variables.

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Dependent variable	Independent variables	Parameters estimates	Multiple R	R Square
Beta index	X ₂	0.005793	-0.1369	0.01873
	X ₆	-0.007493	-0.1522	0.0215
	X ₁	-0.004017	-0.1904	0.0363
	X ₃	-0.009321	-0.2291	0.0525
	X ₅	0.043102	-0.2489	0.06195
	X ₄	-0.009354	-03935	0.1548

Dependent	Independent	Parameters	Multiple R	R-Square
variable	variables	estimates		
Alpha index	Χ.	-0.023551	-0.3115	0.09704
and the state of t	Χ,	0.021783	-0,4410	0,19450
Personal Communication of the	X ₁	-0012114	-0.4577	0.20951
	X ₂	0.027694	-0.4681	0.21914
	Χ,	0.024792	-0.4793	0.22970
	X ₆	-0.086427	-0.5636	0.31768

TABLE 4.0 REGRESSION SUMMARY FOR 'GAMMA INDEX'

However the combined variables explain 97.14% of the total variation in the dependent variable. Thus the model can be used with reliable level of confidence in the explanation of the development of intra-urban network in llorin.

Regression constant =-2.131225; Adj $-R^2 = 0.5551$; Coefficient of Determination for all variables

 R^2 = 0.9364. Regression equation is: Y=-2.1312250.012114X₁+0.027694X₂+0.024792X₃ 0.02855X₄+0.021783X₅-0.086427X₆

Table 4.0 shows that only X_6 (Social amenities) has strong relationship with the dependent variable. The other five explanatory variables have weak relationship with the dependent variable.

The correlation coefficients are -05636 for X_6 (Social amenities). -0.4793 for X_3 (Land use); -0.4681 for X_2 (Transportation); -0.4577 for X_1 (Population).

Thus there is a weak relationship between the Gamma index and many of the identified independent variables.

Further the combined variables explain only 55.51% of the total variation in the dependent variable.

In all, the results of the analysis of the structure of intra-urban road network development in Ilorin show that all the independent variables are important in the explanation of Alpha index, Beta index, and

Gamma index, which are all measures of road net work development.

The results also show that socio-economic variables contribute significantly to intra-urban network development in Ilorin. Consequently the level of economic development of the country can be said to reflect very strongly on the development of transportation networks.

CONCLUSION

This study has been used to show the contributions of various socio-economic variables to the development of intra-urban road network in Ilorin. The study has used the simplicity and reliability inherent in graph-theoretic concepts to identify the structure of network development in the city between 1963 and 1999.

The results of the study revealed that six socio-economic variables namely population, transportation, land use, land speculation. commercial development and social amenities can be used with varying degrees of contribution to explain the development of the city's road network. Specifically all the six independent significantly variables contribute to the explanation of the Alpha index. Similarly these six variables also contribute fairly to the explanation of the Beta index and Gamma index. Overall, the six independent variables can be used reliably to

explain the structure of intra-urban road network development in llorin.

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REFERENCES

- Abdullahi, H.S., 1997. The Influence of income on the Demand for Transport. In Mahe, D: Vardu-Chikolo, I.; Ogunsanya, A.A. (eds.) Issues in Transport Planning and Management. NITT. Zaria
- Aderamo, A. J., 1998. A graph theoretic Analysis of Intra-Urban Road Network in Horin, Nigeria. Techforum 3(2 and 3).
- Appleton, A., 1967. A Morphological Approach to the Geography of Transport. University of Hull Publications.
- Berry, B.J.L., 1961. Basic Patterns of economic Development. In Ginsburg. N.S. (ed.) Atlas of Economic Development. Chicago. University of Chicago Press.
- Berry, B.J.L. 1962. Some relations of urbanization and patterns of economic development in Urban Systems and Economic Development. Eugene Oregon.
- Bland, B.H., 1992. The LUTE Landuse Transportation Model. TRRL Supplementary Report 716. Crowthrone.
- Burghat, A., 1969. The Origin and development of the road network of Niagara Peninsula, Ontario 1770-1851. Annals of the Association of American Geographers, 59: pp. 417-40
- Carter, F. W., 1969. An analysis of the medieval serbian oecumene a theoretical approach. Geografiska Annaler 51B,3a
- Cates, D.B., 1978. Short-run structural change in an active network of declining connectivity. Professional Geographer 30.
- Clawson, M., 1962. Urban sprawl and Speculation in Suburban Land. Land Economics 32 (2).

- Clayton, C., 1977. Interstate population migration process and structure in the United States. 1935-1970 Professional Geographer 24.
- Garrison, W.L., 1960.Connectivity of the interstate highway system. Papers and Proceedings of the Regional Science Association. 6.
- Garrison, W.I. and Marble, D.F., 1965. A prolegomenon to the forecasting of transportation development. Technical Report 65. Prepared for the U.S Army.
- Haggett, P. and Chorley, R.J., 1969. Network analysis in geography. London, Edward Arnold.
- Harvey, D.W., 1969. Explanation in Geography. London, Edward Arnold.
- Ikya, S.G., 1993. The Urban Transportation Problems in Nigeria. Heinemann Educational Books (Nigeria) Plc
- James, G.A. Cliff, A.D. Haggett, P. and Ord, J. K., 1970. Some discrete distributions with applications to regional transport networks. Geogra fiska Annaler's 52B: 14-21
- Kanaroglous, P.S; Anderson W.P and Kazakov, A., 1998.

 Economic Impacts of Highway Infrastructure
 Improvements Part 1 Conceptual framework.

 Journal of Transport Geography 6(3).
- Kansky, K. J. 1963. The Structure of transport networks. University of Chicago, Department of Geography, Research Paper 84.
- Krakover, S., 1982. Spread of Growth in Urban fields: Eastern United States 1972-1978. Ph.D., Dissertation, University of Maryland.
- Leung, C.K., 1982. The analysis and interpretation of National transportation. Networks. Third World Planning Review 4(2).
- Lowe, J.C and Moryadas, S., 1975. The Geography of Movement. Boston. Houghton Mifflin.
- Maunder, D.A.C., 1982. Studies of Bus operations in Delhi, India. TRRL Supplementary Report 710.
- Monmonier, M.S., 1972. Flow-linkage construction for spatial trend recognition. Geographical Analysis 4: 392-406.

- Muraco, W.A., 1972. Intra-urban accessibility. Economic Geography, 48: 388-405
- Nystuen, J.D. and Dacey M.F., 1961. A graph theory interpretation of Nodal Regions. Papers of the Regional Science Association, 7.
- Ogunsanya, A.A., 1985.Generating Urban Traffic Flow data for urban transport Studies in developing countries. Geo forum, 16(4).
- Ogunsanya, A.A., 1986. Graph Theory in Intra-Urban Traffic flow Estimation. Geo Journal 12.
- Royaltey, H.H; Astrachan, E and Soka, R.R., 1975. Tests for patterns in geographic variation. Geographic Analysis 7: 369-95
- Soja, E.W., 1968. Communication and territorial integration of East Africa – an introduction to transaction flow analysis. East Lakes Geographer 4: pp 57-57
- Starkie, D.N.M., 1967. Traffic and Industry. Tunselay and Co. ltd. Manur form Road. Alperton. Wembley Middx.

- Taiwo, LO., 1992. Financing Mass Transit Operations at the Local Government Level. In The Role of Local Governments in Mass Transit Operations in Kwara State. Seminar organied by University of Horin.
- Tinkler, K.J., 1977. An Introduction to Graph Theoretical Methods in Geography. Catmog No 14, Norwich Geo Abstracts.
- Tinkler, K.J., 1979. Graph Theory. Progress in Human Geography. 3(1).
- White, H.P and Senior, M.L., 1983. Transport Geography. Longman Scientific & Technical.
- Wood, L.J., 1975. The functional structure of rural market system. Geogra fiska Annaler 57B: 109-18