Detection and classification of four phase to ground faults in a 138 kV six phase transmission line using Hilbert Huang transform

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Abstract

In this work, the Hilbert Huang transform (HHT) is used for the detection and classification of four phase to ground faults in the six-phase transmission line (SPTL). Using the HHT, the faults can be detected, classified and the faulted phase can be recognized merely, by calculating the amplitudes of HHT coefficients of six-phase fault currents. HHT is utilized for extracting the features of the six-phase fault currents recorded at one end only. The HHT is extensively tested using the MATLAB model of 138 kV, 60 Hz, and 68 km long SPTL. The possibility of HHT is investigated under extensive variations of the fault factors. The results exemplify that the HHT effectively detects and categorizes all types of four phase to ground faults regardless of varying the fault factors.

Keywords: Fault detection, fault classification, faulty phase recognition, Hilbert Huang transform, six phase transmission line.

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1. Introduction

The possibility of fault occurrence on the six-phase transmission line is more when comparing with the double circuit transmission lines. Thus, exact detection of the faults in the six-phase transmission line turns out to be very influential for extenuating the loss of gain and providing rapid renovates.

Quite a few newly reported research studies addressed the issues related to fault recognition and categorization in six-phase transmission line. Some important research attempts are presented in brief in this section. In (Gautam et al., 2018), wavelet transform has been used for fault detection in series capacitor compensated double circuit transmission line. Wavelet transform based fault detection and classification tool has been proposed for the protection of a 400 kV double circuit transmission line (Gautam et al., 2018). A back-up protection technique has been presented in (Jena et al., 2017) for the series capacitor compensated transmission line. Detection and recognition of multi-position three phase to ground faults in a twelve phase transmission line using wavelet transform has been presented in (Kapoor, 2018). Wavelet transform based detection of far-end and near-in faults in six-phase transmission line has been reported in (Kapoor, 2018). Phase to phase faults detection in a series capacitor compensated six-phase transmission line using wavelet transform has been proposed in (Kapoor, 2018). In (Kapoor, 2018), mathematical morphology has been used for the detection of far-end and near-in faults. Hilbert Huang transform has been applied for the detection and classification of single line to ground near-in and far-end faults in a 138 kV six-phase transmission line (Kapoor, 2019). In (Kapoor, 2019), discrete Walsh Hadamard transform has been used for the protection of wind farm integrated series capacitor compensated three phase transmission line. A protection scheme based on discrete wavelet transform has been presented in (Kapoor, 2018) for a twelve phase series capacitor compensated transmission line. In (Kapoor, 2018), a fault detector based on wavelet transform has been proposed for series capacitor compensated three phase transmission line. In (Koley et al., 2015), wavelet transform in conjunction with artificial neural network has been applied for the protection of six-phase transmission line. Sharma et al., 2017 used mathematical morphology for the protection of boundary of a six-phase transmission line. Walsh Hadamard transform has been used for fault detection in series capacitor compensated transmission line (Sharma et al., 2018).
Hilbert Huang transform has been applied for the detection of faults in a wind farm integrated series capacitor compensated transmission line (Sharma et al., 2018).

In this work, the Hilbert Huang transform (HHT) is executed for the detection and classification of four phase to ground faults in a six-phase transmission line. Such type of research has not been depicted so far to the best of the information of the author. The results illustrates that the HHT competently detects the faults, and the uniformity of the HHT is not susceptible to the deviations in the fault factors.

This article is structured as: Section 2 presents the specifications of six-phase transmission line. Section 3 describes the process for fault detection using HHT. Section 4 reports the performance appraisal of the investigations carried out in this work. Section 5 concludes the article.

2. The Specifications of Six-Phase Power Transmission System

Figure 1 shows the schematic of six-phase power transmission system. The power transmission system consists of a 138 kV, 60 Hz, 68 km long six-phase transmission line which is divided into two zones. Each zone has a length of 34 km. The six-phase transmission line is fed from a 138 kV source at the sending and at the receiving end. The two loads of 300 MW and 150 MVAr are connected at the receiving end of a six-phase transmission line. The model of six-phase transmission line is developed and simulated using the simscape power system toolbox of MATLAB.

As shown in Figure 1, the current measurements blocks for the relay are connected at bus-1 to protect the entire length of six-phase transmission line. Figure 2 shows the six-phase current and voltage waveforms for no-fault. Figure 3 depicts the Hilbert Huang coefficients of six-phase currents for no-fault. Table 1 reports the response of the HHT for no-fault condition.

![Figure 1. The schematic of proposed simulation model](image1)

![Figure 2. Six phase current and voltage waveforms for no-fault](image2)
3. The Hilbert Huang Transform Based Fault Detection Technique

The Hilbert transform for a test signal \( f(t) \) is defined as given in equation-1 below (Sharma et al., 2018):

\[
H \{ f(t) \} = -\frac{1}{\pi} \int_{-\infty}^{\infty} \frac{f(\tau)}{\tau-t} \, d\tau = -\frac{1}{\pi} * f(t)
\]  

(1)

Hilbert transform can be defined as the convolution between \( f(t) \) and \(-1/\pi t\).

This equation defines an inappropriate integral, because for \( t = \tau \) the integral has an exceptionality. So the integral is calculated symmetrically to avoid this difficulty.

\[
\int_{-\infty}^{\infty} g(\tau) \, d\tau = \lim_{\epsilon \to 0} \left[ \int_{-\infty}^{-\epsilon} g(\tau) \, d\tau + \int_{\epsilon}^{\infty} g(\tau) \, d\tau \right]
\]  

(2)

Inverse Hilbert transform can be deliberated by equation-3, where \( g^\prime(t) \) and \( g(t) \) are part of pair transform of Hilbert (Kapoor, 2019).

\[
g(t) = -\frac{1}{\pi} \int_{-\infty}^{\infty} g^\prime(t) * d\tau
\]  

(3)

From the definition of Hilbert Transform it is observed that \( g^\prime(t) \) can be understood as the convolution of \( g(t) \) with the signal \( -1/\pi t \).

\[
g^\prime(t) = g(t) * \frac{1}{\pi t}
\]  

(4)

Figure 4 shows the process of Hilbert Huang transform for fault detection and classification. The steps for the same are shown below.

Step 1  Simulate the model for different four phase to ground faults and generate the six-phase fault current signals.

Step 2  Analyze the six-phase currents using Hilbert Huang transform for the removal of their characteristics.
Step 3  Calculate the amplitudes of HHT coefficients for each fault current signal.

Step 4  The phase will be declared as the faulted phase if its HHT coefficient has the larger amplitude in comparison to the healthy phase.

\[
\text{Measure phase fault currents}
\]
\[
\text{Analyze currents using Hilbert Huang transform}
\]
\[
\text{Evaluate Hilbert Huang coefficients}
\]
\[
\text{Is} |\text{HHT coefficient}| \text{ faulted phase} > |\text{HHT coefficient}| \text{ healthy phase} \quad \text{NO}
\]
\[
\text{Fault detection and classification}
\]

\[
\text{No fault}
\]

Figure 4. HHT procedure for fault detection and classification

4. Results and Discussions

The efficacy of Hilbert Huang transform has been tested for various types of four phase to ground faults. The fault factors of the simulation model are varied in each case. The results are shown in the subsequent subsections.

4.1 Performance in Case of ACDFG Fault: The performance of HHT is evaluated for ACDFG four phase to ground fault triggered at 34 km away from the relaying point at fault triggering time of 0.05 seconds with \( R_F = 2 \, \Omega \) and \( R_G = 4 \, \Omega \). Figure 5 demonstrates the waveform of six phase current for ACDFG fault. Figure 6 depicts the Hilbert Huang transform coefficients of six phase current for ACDFG fault. Table 2 reports the response of HHT for ACDFG fault. It is examined from Table 2 that the amplitudes of Hilbert Huang coefficients of the faulted phases are greater than the amplitudes of Hilbert Huang coefficients of the healthy phases. Thus, the HHT correctly detects the ACDFG fault.

Figure 5. Six phase current for ACDFG fault at \( \text{FIT}=0.05 \) seconds with \( R_F = 2 \, \Omega \) and \( R_G = 4 \, \Omega \)
4.2 Performance in Case of BDEFG Fault: The performance of HHT is checked for BDEFG four phase to ground fault simulated at 40 km away from the relaying point at fault triggering time of 0.1 seconds with $R_F = 4 \ \Omega$ and $R_G = 8 \ \Omega$. Figure 7 demonstrates the waveform of six phase current for BDEFG fault. Figure 8 depicts the Hilbert Huang transform coefficients of six phase current for BDEFG fault. Table 3 reports the response of HHT for BDEFG fault. From Table 3, it is inspected that the amplitudes of Hilbert Huang coefficients of the faulted phases are greater than the amplitudes of Hilbert Huang coefficients of the healthy phases. Therefore, it is clear from Table 3 that the HHT accurately detects the BDEFG fault.
Figure 8. HHT coefficients of six phase current for BDEFG fault at FIT=0.1 seconds with $R_F = 4 \, \Omega$ and $R_G = 8 \, \Omega$

<table>
<thead>
<tr>
<th>Phase</th>
<th>Hilbert Huang Transform Coefficients</th>
</tr>
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<tbody>
<tr>
<td>A</td>
<td>248.5096</td>
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<tr>
<td>B</td>
<td>$2.8393 \times 10^3$</td>
</tr>
<tr>
<td>C</td>
<td>235.8718</td>
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<tr>
<td>D</td>
<td>$6.2949 \times 10^3$</td>
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<tr>
<td>E</td>
<td>$6.4717 \times 10^3$</td>
</tr>
<tr>
<td>F</td>
<td>$7.9797 \times 10^3$</td>
</tr>
</tbody>
</table>

Table 3. Result for BDEFG fault at 40 km at FIT = 0.1 seconds with $R_F = 4 \, \Omega$ and $R_G = 8 \, \Omega$

4.3 Performance in Case of ACDEG Fault: The response of HHT is investigated for ACDEG four phase to ground fault triggered at 45 km away from the relaying point at fault initiation time of 0.15 seconds with $R_F = 6 \, \Omega$ and $R_G = 12 \, \Omega$. Figure 9 exemplifies the waveform of six phase current for ACDEG fault. Figure 10 depicts the Hilbert Huang coefficients of six phase current for ACDEG fault. Table 4 reports the result of HHT for ACDEG fault. From Table 4, it is clear that the amplitudes of Hilbert Huang coefficients of the faulted phases are larger than the amplitudes of Hilbert Huang coefficients of the healthy phases. Therefore, it is obvious from Table 4 that the HHT correctly detects the ACDEG fault.

Figure 9. Six phase current for ACDEG fault at FIT=0.15 seconds with $R_F = 6 \, \Omega$ and $R_G = 12 \, \Omega$
Figure 10. HHT coefficients of six phase current for ACDEG fault at FIT=0.15 seconds with $R_F = 6 \Omega$ and $R_G = 12 \Omega$

<table>
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<tr>
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<td>$3.7413\times10^3$</td>
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<td>F</td>
<td>235.1222</td>
</tr>
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</table>

Table 4. Result for ACDEG fault at 45 km at FIT=0.15 seconds with $R_F = 6 \Omega$ and $R_G = 12 \Omega$

4.4 Performance in Case of BCEFG Fault: The performance of HHT is tested for BCEFG four phase to ground fault simulated at 5 km away from the relaying point at 0.02 seconds with $R_F = 8 \Omega$ and $R_G = 16 \Omega$. Figure 11 illustrates the waveform of six phase current for BCEFG fault. Figure 12 depicts the Hilbert Huang coefficients of six phase current for BCEFG fault. Table 5 shows the response of HHT for BCEFG fault. From Table 5, it is seen that the amplitudes of Hilbert Huang coefficients of the faulted phases are larger than the amplitudes of Hilbert Huang coefficients of the healthy phases. Therefore, it is apparent from Table 5 that the HHT perfectly recognizes the BCEFG fault.

Figure 11. Six phase current for BCEFG fault at FIT=0.02 seconds with $R_F = 8 \Omega$ and $R_G = 16 \Omega$
Figure 12. HHT coefficients of six phase current for BCEFG fault at FIT=0.02 seconds with $R_F = 8 \, \Omega$ and $R_G = 16 \, \Omega$

<table>
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<tr>
<th>Phase</th>
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<td>A</td>
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<td>D</td>
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<td>E</td>
<td>1.6790*10^4</td>
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<tr>
<td>F</td>
<td>1.4123*10^4</td>
</tr>
</tbody>
</table>

Table 5. Result for BCEFG fault at 5 km at FIT= 0.02 seconds with $R_F = 8 \, \Omega$ and $R_G = 16 \, \Omega$

4.5 Performance in Case of CDEBG Fault: The performance of HHT is inspected for CDEBG four phase to ground fault triggered at 65 km away from the relaying point at 0.075 seconds with $R_F = 10 \, \Omega$ and $R_G = 20 \, \Omega$. Figure 13 depicts the waveform of six phase current for CDEBG fault. Figure 14 shows the Hilbert Huang coefficients of six phase current for CDEBG fault. Table 6 reports the results of HHT for CDEBG fault. It is examined from Table 6 that the amplitudes of Hilbert Huang coefficients of the faulted phases are larger than the amplitudes of Hilbert Huang coefficients of the healthy phases. Hence, it is understandable from Table 6 that the HHT accurately detects the CDEBG fault.

Figure 13. Six phase current for CDEBG fault at FIT=0.075 seconds with $R_F = 10 \, \Omega$ and $R_G = 20 \, \Omega$
Figure 14. HHT coefficients of six phase current for CDEBG fault at FIT=0.075 seconds with $R_F = 10\ \Omega$ and $R_G = 20\ \Omega$

<table>
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<tr>
<th>Phase</th>
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<tr>
<td>B</td>
<td>$2.5383 \times 10^3$</td>
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<tr>
<td>C</td>
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</tr>
<tr>
<td>D</td>
<td>$2.5313 \times 10^3$</td>
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<tr>
<td>E</td>
<td>$2.9412 \times 10^3$</td>
</tr>
<tr>
<td>F</td>
<td>284.2040</td>
</tr>
</tbody>
</table>

Table 6. Result for CDEBG fault at 65 km at FIT=0.075 seconds with $R_F = 10\ \Omega$ and $R_G = 20\ \Omega$

4.6 Performance in Case of ABCDG Fault: The HHT is tested for ABCDG four phase to ground fault at 50 km away from the relaying point at 0.125 seconds with $R_F = 12\ \Omega$ and $R_G = 24\ \Omega$. Figure 15 exemplifies the waveform of six phase current for ABCDG fault. Figure 16 depicts the Hilbert Huang coefficients of six phase current for ABCDG fault. Table 7 shows the result of HHT for ABCDG fault. It is clear from the results that the amplitudes of Hilbert Huang coefficients of the faulted phases are greater than the amplitudes of Hilbert Huang coefficients of the healthy phases. Hence, the HHT correctly recognizes the ABCDG fault.
Figure 16. HHT coefficients of six phase current for ABCDG fault at FIT=0.125 seconds with $R_F = 12 \ \Omega$ and $R_G = 24 \ \Omega$

<table>
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<tr>
<th>Phase</th>
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<td>$3.7116 \times 10^3$</td>
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<td>B</td>
<td>$3.2429 \times 10^3$</td>
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<tr>
<td>C</td>
<td>$4.4120 \times 10^3$</td>
</tr>
<tr>
<td>D</td>
<td>$1.2360 \times 10^3$</td>
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<tr>
<td>E</td>
<td>$229.8691$</td>
</tr>
<tr>
<td>F</td>
<td>$263.0660$</td>
</tr>
</tbody>
</table>

Table 7. Result for ABCDG fault at 50 km at FIT=0.125 seconds with $R_F = 12 \ \Omega$ and $R_G = 24 \ \Omega$

4.7 Performance in Case of CDEFG Fault: The response of HHT is explored for CDEFG four phase to ground fault at 55 km away from the relaying point at 0.03 seconds with $R_F = 14 \ \Omega$ and $R_G = 28 \ \Omega$. Figure 17 shows the waveform of six phase current for CDEFG fault. Figure 18 depicts the Hilbert Huang coefficients of six phase current for CDEFG fault. Table 8 exemplifies the results of HHT for CDEFG fault. It is seen from Table 8 that the amplitudes of Hilbert Huang coefficients of the faulted phases are greater than the amplitudes of Hilbert Huang coefficients of the healthy phases. Hence, the HHT perfectly detects the CDEFG fault.

Figure 17. Six phase current for CDEFG fault at FIT=0.03 seconds with $R_F = 14 \ \Omega$ and $R_G = 28 \ \Omega$
Figure 18. HHT coefficients of six phase current for CDEFG fault at FIT=0.03 seconds with $R_F = 14 \, \Omega$ and $R_G = 28 \, \Omega$

<table>
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<tr>
<th>Phase</th>
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<td>C</td>
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<td>D</td>
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</tr>
</tbody>
</table>

5. Conclusion

The Hilbert Huang transform (HHT) is seemed to be very efficient under miscellaneous fault categories for the 138 kV six-phase transmission line. The HHT coefficients of the six-phase fault currents are estimated. The fault factors of the simulation model are varied and it is explored that the fault factors do not influence the reliability of the HHT. The results substantiates that the HHT has the capability to protect the six-phase transmission line besides various fault categories. The future work is planned on execution of the proposed technique on a digital platform (preferably digital signal processor) and assessing the scheme for more practical conditions.

References


Biographical notes

Gaurav Kapoor received B.E. in Electrical Engineering from University of Rajasthan, Jaipur, India and M. Tech. in Power System specialization from University College of Engineering, Rajasthan Technical University, Kota, India in 2011 and 2014, respectively. He is an Assistant Professor in the Department of Electrical Engineering, Modi Institute of Technology Kota, India. He has published more than forty five papers in various journals. He has also presented many research papers in national and international conferences. His research interests include power system digital protection.

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