



## Estimation of Soil Water Retention Curve in Semi-arid Areas Using Fractal Dimension

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**ABSTRACT:** The soil water retention curve (SWRC) is one of the important hydraulic functions in water flow modeling and solute transport in the porous medium. Direct measurement of SWRC is time consuming and expensive, therefore different models have been developed to describe it. In this study, a model based on fractal theory was derived to estimate water retention curve. The fractal dimension of SWRC ( $D_{SWRC}$ ) for 130 soil samples (with a spread range of soil texture) were determined and tried to find out a simple relation between this parameter and easily available soil properties such as clay, silt and sand contents, lime percent and bulk density by applying multiple linear regression analysis. The measured  $D_{SWRC}$  for 110 soil samples used for regression analysis and 20 soil samples was used for model validation. The regression analysis showed a linear relationship between  $D_{SWRC}$ , with clay, silt contents and soil bulk density with the goodness of fit,  $R^2 = 0.909$ , but lime content did not show any significant effect on SWRC prediction improvement. Therefore, it can be concluded that estimating SWRC in calcareous soil using  $D_{SWRC}$  obtained from soil easily measured properties will be a good, rapid and reliable alternative for reliable estimation of soil hydraulic properties of these areas.

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The increasing concern with groundwater pollution and contamination of soils has stimulated the development of numerous mathematical models of pollutant transport in soils. The most important approaches to model transient water and solute transport in the vadose zone are based on the Richards equation. To solve this equation, the knowledge of the soil hydraulic properties, namely, the soil water retention curve (SWRC) and the unsaturated hydraulic conductivity is required and on the other hand, Measurements of hydraulic properties are expensive, time-consuming and highly variable (Patil and Chore, 2014). Models Parameters are usually estimated by fitting the functions to measured SWRC data. Recently, the pedotransfer functions are used to empirically describe the relationship between the parameters and basic soil data (Elsenbeer, 2001; Woosten *et al.*, 2001). In recent years, the formulation of fractal geometry has attracted much attention as a powerful tool for describing various complex natural phenomena, in particular, in mechanics and physics of rocks and soils.

Recent applications of fractal geometry provide a useful tool to bridge the gap between the use of empirical models and physical interpretation of their parameters. Fractals describe hierarchical systems and are suitable to model the heterogeneous soil structure with tortuous pore space (Xu and Sun, 2002). In general, fine-textured soils have higher fractal dimensions, while coarse-textured soils have smaller fractal dimensions (Comegna *et al.*, 2000; Huang and Zhan, 2002). Fractal dimensions of the solid matrix (that is, soil particle size distribution and soil texture) and the void phase (that is, soil pore size distribution and soil pore surface) can characterize by the fractal nature of soils. Nevertheless, further study is required to quantify the relationship between the fractal dimensions of the soil solid and void phases and the fractal dimension used in the SWRC (Huang and Zhang, 2005). Perfect (2005) used the fractal geometry to simulate porous media structure and revised by Cihan *et al.*, (2007). Some other researchers applied the fractal theory to investigate the SWRC and used the fractal dimensions of the SWRC to describe the corresponding SWRC (Wang *et al.*, 2005; Ghanbarian-Alavijeh and Hunt, 2012). However the

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exponent of soil water retention curve,  $D_{SWRC}$  is physically meaningful, its direct measurement is difficult in laboratory and also field soil water retention experiments are laborious and time consuming. So estimation of  $D_{SWRC}$  based on the available data, can be very useful alternative. Soil particle size distribution has fractal properties. Hence, fractal model can be used to estimate the soil water retention curve. Thus the main objectives of this study were (1) determining the  $D_{SWRC}$  from SWRC experimental data, (2) establishing a relationship among  $D_{SWRC}$ , and soil readily available characteristics (i.e. clay, silt and sand contents, lime percent and bulk density), (3) validating the developed relationship in SWRC estimation in calcareous soil.

### MATERIALS AND METHODS

**Study area:** A set of disturbed and undisturbed soil samples were collected from top 30 cm soil horizon of Varamin, Iran (from 35° 11' 46.07" to 35° 02' 41.65" east longitudes and from 51° 33' 49.92" to 51° 47' 02.66" north latitudes). The climate of the region is categorized as semi-arid with mean annual temperature and precipitation of 18°C and 150 mm, respectively and the areas soil is classified as Xeric Haplocalcid (Moravvej *et al.*, 2003).

**Soil sampling and soil properties measurement:** The soil samples cover a most range of texture classes. Table 1 shows the general characteristics of studied soils. Disturbed samples were air dried, passed through a 2 mm sieve, so, soil texture determined according to the USDA texture classification standards and lime percent were determined. Undisturbed samples were used to measure bulk density and to obtain the SWRC. The soil water retention data were measured using the pressure plate apparatus (Model 1500, Soil moisture Equipment, CA) at seven matric potentials (100, 300, 1000, 3000, 5000, 10000 and 15000 cm), then the SWRC for each soil was determined.

**Table 1:** Some statistic parameters of soil properties (n=130).

Soil properties	Maximum	Minimum	Mean
Clay (%)	53.96	15.68	36.81
Silt (%)	71.2	27.64	50.68
Sand (%)	26.84	7.04	12.50
Bulk density (gcm <sup>-3</sup> )	1.75	1.44	1.59
Lime (%)	28	7	17.35

The fractal model used in this study was the Tyler and Wheatcraft (1990) model that express by Eq. 1 as:

$$\theta = \theta_s \left(\frac{\psi}{\psi_a}\right)^{D_m-3} \quad (1)$$

Where  $\psi$ , is the capillary tension head (cm) and  $\theta$  is the soil water content (cm<sup>3</sup>cm<sup>-3</sup>),  $\theta_s$ , is the saturated soil water content (cm<sup>3</sup>cm<sup>-3</sup>),  $\psi_a$  is the air entry pressure (cm),  $D_m$  is the fractal dimension of SWRC. The measured  $D_{SWRC}$  for 110 soil samples, used for regression analysis and 20 soil samples was used for model validation. So, 110 soil samples in the regression model were employed to derive the relationship between the fractal dimension of SWRC and other soil physical parameters including clay, silt and sand percent, lime percent and bulk density. Multiple linear regression analysis was done using Sigma Plot software. Finally, the fractal dimension estimated with a regression model, rather than the fractal dimension in the fractal model was put, so the curve of soil moisture estimates was compared with the measured SWRC.

**Quantitative assessment of model performances:** To test the validity of the model in predicting retention curve plot of observed and estimated values, coefficient of determination ( $R^2$ ) (at the significant level of 1%) and Root Mean Square Error ( $R_{MSE}$ ) was used.

**Model Calibration:** To calibrate the model, were drawn the moisture content of the initial and final points of measured and estimated soil water retention curves (100 and 15000 cm), and was used the slope and intercept of the fitted line on the two points for calibration (Ghanbarian-Alavigh *et al.*, 2007). The estimated soil water retention curves were compared with the measured data, and the difference between the estimated soil water retention curves and the measured data was then quantified by using the Mean Absolute Error (MAE) and Mean Square error (MSE). Linear regression was then performed between measured and estimated water content for all soils and  $R^2$  was determined.

### RESULTS AND DISCUSSION

The SWRC fractal dimension determining with soil moisture curve ranged between 2.73 to 2.89 for loam and clay soil texture classes. Table 2 shows the values of maximum, minimum and average soil moisture curve measured fractal dimensions for texture studied. Estimated fractal dimension values depended on soil texture as soils with coarse texture had lower fractal dimension values than soils with a fine texture.

Based on the results, the relationship between the fractal dimension of SWRC and other parameters including clay, silt and sand percent, lime percent and bulk density using regression analysis were established as follows:

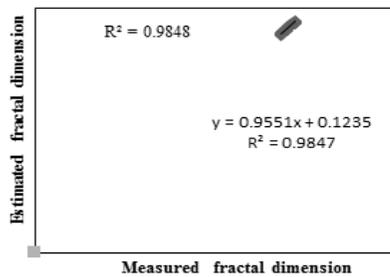
**Table 2:** Values of maximum, minimum and average soil moisture curve measured fractal dimensions for texture studied (n=130).

Texture	Measured fractal dimension		
	Max	Min	Mean
Silty Loam	2.764	2.733	2.748
Clay Loam	2.787	2.781	2.784
Silty Clay Loam	2.817	2.790	2.800
Silty Clay	2.882	2.788	2.836
Clay	2.891	2.862	2.878

$$D_{SWRC} = 2.673 + (0.00371 \times C) - (0.000641 \times S) + (0.0229 \times Bd) \quad (2)$$

$$R^2 = 0.909$$

where,  $D_{SWRC}$  is the estimated fractal dimension of soil water retention curve, C and S are clay and silt content and Bd is soil bulk density ( $cm^3cm^{-3}$ ).



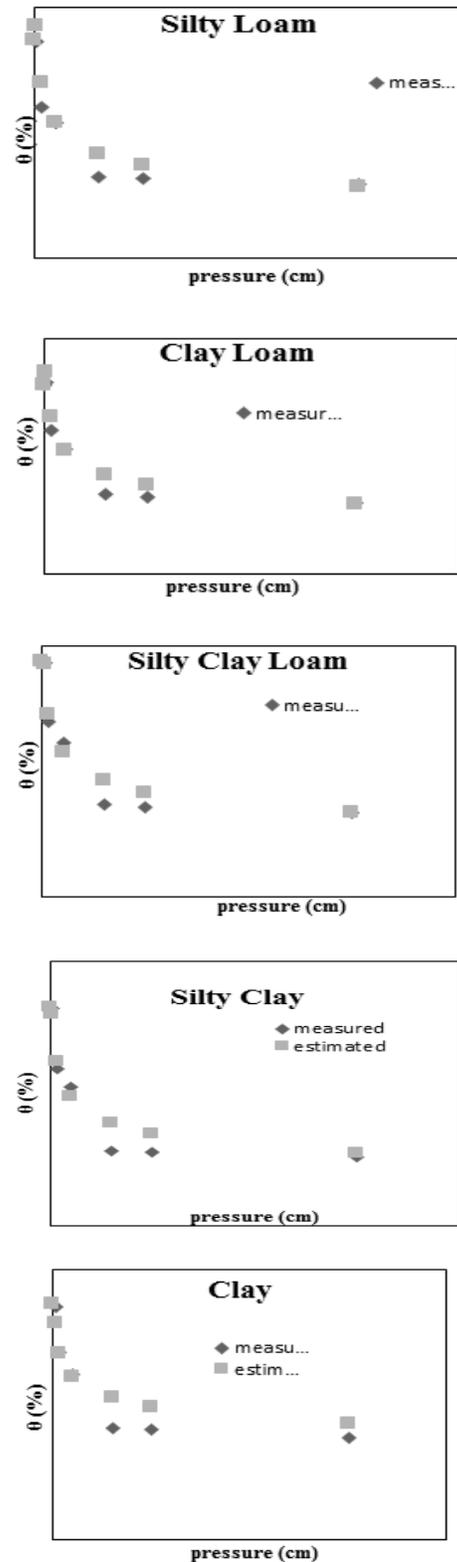
**Fig 1:** Distribution of estimated fractal dimension values with obtained regression model and measured fractal dimension with soil moisture curve

The regression analysis showed a high correlation between  $D_{SWRC}$ , clay and silt content and soil bulk density with the goodness of fit,  $R^2 = 0.909$ . On the other hand, the given result revealed that lime percent did not show a significant effect on  $D_{SWRC}$ . Hence, could not be found a methodical relation between lime percent and  $D_{SWRC}$ . Therefore, the  $D_{SWRC}$  could be approximated by using clay and silt contents and soil bulk density as obtained regression model. A comparison of estimated fractal dimension values with obtained regression model and measured fractal dimension with soil moisture curve is shown in Fig. 1.

**Table 3:** MAE, MSE and  $R^2$  obtained from comparing all data of the measured soil water content versus estimated by using obtained regression model.

	MAE	MSE	$R^2$
Fractal	0.0072	7.699E-05	0.9658

Table 3 shows the MAE, MSE and  $R^2$  obtained from comparing all data of the measured soil water content versus the estimated by using obtained regression model. The results showed a reasonably good estimation of soil water retention curves for the most of the soils. Similar results were also found by Fazeli et al., (2010).



**Fig 2:** Estimated and measured SWRC for five typical soil: Silty Loam, Clay Loam, Silty Clay Loam, Silty Clay and Clay.

Estimated and measured SWRC had shown in figure 2 for five typical soils: Silty Loam, Clay Loam, Silty Clay Loam, Silty Clay and Clay. Results showed that for most of the soils, using regression relationship, gave a good estimation of SWRC. Additionally, linear regression of the measured and estimated SWRC for validation data set showed that the intercept values for all tested soils were close to zero, most of the slope values were close to unity, and the coefficients of determination ( $R^2$ ) between the estimated results and measured data for all soils ranged from 0.993 to 0.998. Hence, this method could be recommended for estimating SWRC in calcareous soil.

In this study, we assessed the estimation of soil water retention curve using fractal dimensions of SWRC ( $D_{SWRC}$ ) and the relationship between  $D_{SWRC}$  and soil readily available characteristics were analyzed in calcareous soil. The results showed that fractal dimensions of SWRC increased with clay content and decreased with sand content. On the other hand, regression analysis showed a linear relationship between  $D_{SWRC}$ , clay and silt content and soil bulk density but lime percent did not show a significant effect.

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