ISSN 1112-9867

Available online at

t http://www.jfas.info

A NEW ANALYTICAL MODELING METHOD FOR PHOTOVOLTAIC SOLAR CELLS BASED ON DERIVATIVE POWER FUNCTION

R. Zieba Falama^{1,2,*}, A. Dadjé^{1,3}, N. Djongyang¹ and S.Y. Doka⁴

¹Department of Renewable Energy, The Higher Institute of the Sahel, University of Maroua, P.O Box 46 Maroua, Cameroon

²Institute of Geological and Mining Research, P.O. Box 4110 Yaoundé, Cameroon

³School of Geology and Mining Engineering, University of Ngaoundéré, P.O Box 454 Ngaoundere, Cameroon

⁴Department of Physics, Faculty of Science, University of Ngaoundéré, P.O Box 454 Ngaoundere, Cameroon

Received: 25 Jaunary 2016 / Accepted: 25 April 2016 / Published online: 01 May 2016

ABSTRACT

This paper presents a simple method of optimizing the photovoltaic (PV) generator based on the one diode electrical model. The method consists in solving a second degree equation representing the derivative of the power function. The maximum current and voltage are determined, and the maximum power is deduced. Two popular types of photovoltaic panels constructed with different materials have been considered for the test: the multi-crystalline silicon (Shell S75), and the mono-crystalline silicon (Shell SP70). For various environmental conditions, a comparative study is done between the simulated results and the product manufacturer data. The obtained results prove the efficiency of the proposed method.

Keywords: model; photovoltaic generator; power function; optimizing, maximum power.

Author Correspondence, e-mail: rubenzieba@yahoo.fr

doi: http://dx.doi.org/10.4314/jfas.v8i2.17



1. INTRODUCTION

Solar energy applications have been increasing gradually throughout the world. This is due to the decrease in the cost of PV panels with the increasing demand, and the increase in duration of use (lifetime). Photovoltaic is very competitive in areas far from the conventional electricity network. However, its exploitation requires a conception and implantation of a production system which also require a good sizing in order to avoid losses or lack of energy.

The evaluation of the maximum power produced by a PV generator is very important to size a PV system. Several models have been developed to determine the maximum power produced by a PV generator. In general, two main approaches are found in the literature [1, 2].

Nomenclature

Ι	:	Cell current (A)
V	:	Cell Voltage (V)
I_{ph}	:	Light current (A)
I_D	:	Diode current (A)
I _{sh}	:	Shunt current (A)
I_o	:	Saturation current of the diode (A)
I _{o,ref}	:	The reverse saturation current (A)
Isc	:	Short circuit current (A)
V_{oc}	:	Open circuit voltage (V)
α	:	Temperature coefficient of short-circuit current (A/K)
T_c	:	Cell Temperature (Kelvin)
T_r	:	Cell Temperature at reference condition (25°C or 298 K)
I_{mp}	:	Current at peak power point in reference condition (A)
V_{mp}	:	Voltage at peak power in reference condition (V)
I _{ph,ref}	:	Reference light current (A)

G	:	Irradiance (W/m ²)
G_r	:	Irradiance at reference condition (W/m ²)
п	:	Ideality factor of the diode
Ν	:	Number of cells in series
k	:	Boltzmann constant (1.38×10 ⁻²³ J/K)
q	:	Electron charge $(1.6 \times 10^{-19} \text{ coulomb})$
R_s	:	Series resistance of generator (Ω)
R_{sh}	:	Shunt resistance (Ω)
E_g	:	Gap Energy (for the silicon $E_g = 1.12 \text{ eV}$)

The first approach requires taking some measurements once the PV generator is installed. This is the case of Sandia and Cenerg models [3]. The second approach consists in using solely the data provided by the manufacturer; e.g. of Borowy and Salameh's model [4] and the model of Jones *et al* [5]. Modeling a PV generator needs to evaluate the different parameters of the module. The number of theses parameters varies with the type of module. In this study a one diode PV generator with five parameters is used.

Generally, the five parameters determination of a one diode PV generator is difficult due to the exponential equation of the diode p-n junction. The commonly used methods to determine these parameters are the analytical method, but recently novel techniques using computational intelligence algorithms have been carried out such as cuckoo search (CS) [6], pattern search (PS) [7], Chaos Particle Swarm Optimization (CPSO) [8], genetic algorithm (GA) [9], fuzzy logic (FL) [10], artificial neural network (ANN) [11, 12]. The analytical method based on datasheet is used in this work.

In ref. [2], a data-based approach has been presented to estimate the maximum power of the PV generator. An iterative method was used to solve the nonlinear equation of the maximum current, obtained by the derivative of power with respect to voltage.

In this work to get round the nonlinearity difficult of the maximum current equation, are both

used the derivative of power with respect to current and limit development, in order to estimate the maximum power of the photovoltaic generator.

To prove the efficiency of the proposed model, a comparison is doing with the data provided by the manufacturers for two types of photovoltaic panels.

2. PRESENTATION OF THE METHOD

2.1. Modeling of the photovoltaic generator

In the literature, two main electric photovoltaic generator models exist; namely the one and two diodes models, with three or several parameters. In this work, a one diode photovoltaic module with five parameters whose equivalent diagram is presented in figure 1 is studied. The five parameters here are: I_{ph} , R_s , R_{sh} , I_0 , and n.



Fig.1. Electrical model of a PV generator with five parameters [1,4]

The current produced by the generator is obtained from Kirchhoff's laws as follows:

$$I = I_{ph} + I_D \tag{1}$$

The diode current can be obtained through Shockley equation as follows [13]:

$$I_D = I_o \left(\exp\left(\frac{q\left(V + R_s I\right)}{nNkT_c}\right) - 1 \right)$$
(2)

While the shunt current is given by the relation:

$$I_{sh} = \frac{V + R_s I}{R_{sh}} \tag{3}$$

Replacing (2) and (3) into (1) give the photovoltaic current as:

$$I = I_{ph} - I_o \left(\exp\left(\frac{q\left(V + R_s I\right)}{nNkT_c}\right) - 1 \right) - \frac{V + R_s I}{R_{sh}}$$
(4)

In practice shunt resistance has a high values, therefore the term $\frac{V + R_s I}{R_{sh}} \rightarrow 0$ [14, 15], so:

$$I = I_{ph} - I_o \left(\exp\left(\frac{q\left(V + R_s I\right)}{nNkT_c}\right) - 1 \right)$$
(5)

2.1.1. Determination of the PV generator parameters

2.1.1.1. Evaluation of I_{ph}

The light current I_{ph} depends on both irradiance and temperature. It is given by [13, 15]:

$$I_{ph} = \left[I_{sc} + \alpha (T_c - T_r) \right] \left(\frac{G}{G_r} \right)$$
(6)

2.1.1.2. Evaluation of I_o

The reverse saturation current depending of cells temperature is given as follows [13, 15]:

$$I_{o} = I_{o,n} \left(\frac{T_{c}}{T_{r}}\right)^{3} \cdot \exp\left(\frac{qE_{g}\left(\frac{1}{T_{r}} - \frac{1}{T_{c}}\right)}{nk}\right)$$
(7)

At the open circuit voltage, I=0, V=V_{oc} and $I_{ph}=I_{sc}$:

$$0 = I_{sc} - I_{o,n} \left(\exp\left(\frac{qV_{oc}}{nNkT_c}\right) - 1 \right)$$
(8)

So the nominal saturation current is obtained through:

$$I_{o,n} = \frac{I_{sc}}{\exp\left(\frac{qV_{oc}}{nNkT_c}\right) - 1}$$
(9)

By replacing the eq. (9) into eq. (7) one gets:

$$I_{o} = \frac{I_{sc}}{\exp\left(\frac{qV_{oc}}{nNkT_{c}}\right) - 1} \left(\frac{T_{c}}{T_{r}}\right)^{3} \cdot \exp\left(\frac{qE_{g}\left(\frac{1}{T_{r}} - \frac{1}{T_{c}}\right)}{nk}\right)$$
(10)

2.1.1.3. Evaluation of R_s

Various techniques have been used to determine the series resistance R_s [16-20]. In this work

the series resistance is evaluated as follows:

$$R_s = -\frac{dV}{dI}\Big|_{V=V_{oc}}$$
(11)

Considering the asymptotic behavior of the I-V curve at short-and open-circuit conditions [21], (11) can be calculated as:

$$R_s = \frac{V_{oc} - V_{mp}}{N_s I_{mp}} \tag{12}$$

2.1.1.4. Evaluation of n

At the short circuit point, I=I_{sc}, V=0:

$$I_{sc} = I_{ph,ref} - I_{o,ref} \left(\exp\left(\frac{qR_s I_{sc}}{nNkT_r}\right) - 1 \right)$$
(13)

At the maximum power point, $I=I_{mp}$, $V=V_{mp}$:

$$I_{mp} = I_{ph,ref} - I_{o,ref} \left(\exp\left(\frac{q\left(V_{mp} + R_s I_{mp}\right)}{nNkT_r}\right) - 1 \right)$$
(14)

The reverse saturation current I_0 for any diode is a very small quantity, on the order of 10^{-5} or 10^{-6} A [2]. This minimizes the impact of the exponential term in Eq. (13), so it is safe to assume that the photocurrent equals the short-circuit current [22]. Another simplification [23] can be made regarding the first term in eqs. (8) and (14). In both cases, regardless of the system size, the exponential term is much greater than the first term. For this reason the first term can be neglected. Then, the equation system becomes:

$$I_{sc} \approx I_{ph,ref} \tag{15}$$

$$0 = I_{sc} - I_{o,ref} \cdot \exp\left(\frac{qV_{oc}}{nNkT_r}\right)$$
(16)

$$I_{mp} = I_{ph,ref} - I_{o,ref} \exp\left(\frac{q\left(V_{mp} + R_s I_{mp}\right)}{nNkT_r}\right)$$
(17)

Combining (16) and (17), the ideality factor is evaluated as follows:

$$n = \frac{q\left(V_{mp} + R_s I_{mp} - V_{oc}\right)}{NkT_r \ln\left(\frac{I_{sc} - I_{mp}}{I_{sc}}\right)}$$
(18)

2.2. Maximum power point determination

By using the expression of the PV current defined by eq. (5), the voltage supplied by the generator is:

$$V = \frac{nNkT_c}{q} \ln\left(1 + \frac{I_{ph} - I}{I_o}\right) - R_s I$$
(19)

The electric power produced by the generator is given by:

$$P = V.I \tag{20}$$

By replacing (19) into (20) one obtain,

$$P = \frac{nNkT_cI}{q} \ln\left(1 + \frac{I_{ph} - I}{I_o}\right) - R_s I^2$$
(21)

From the function P = f(I), the extremum is obtained by the resolution of the equation

$$\frac{\partial P}{\partial V} = 0$$

i.e.

$$2R_{s}I^{2} - \left[C\ln\left(1 + \frac{I_{ph} - I}{I_{o}}\right) + C + 2R_{s}\left(I_{o} + I_{ph}\right)\right]I + C\ln\left(1 + \frac{I_{ph} - I}{I_{o}}\right)\left(I_{o} + I_{ph}\right) = 0$$
(22)

In the above equation (22),

$$C = \frac{nNkT_c}{q}$$
(23)

The limit development near of I = 0, in one order for $\ln\left(1 + \frac{I_{ph} - I}{I_o}\right)$ is given by:

$$\ln\left(1 + \frac{I_{ph} - I}{I_o}\right) = \ln\left(1 + \frac{I_{ph}}{I_o}\right) - \frac{I}{I_o + I_{ph}}$$
(24)

By replacing equation (24) into equation (22), one can have:

$$2R_{s}I^{2} - \left[C\ln\left(1 + \frac{I_{ph}}{I_{o}}\right) - \frac{CI}{I_{o} + I_{ph}} + C + 2R_{s}\left(I_{o} + I_{ph}\right)\right]I + C\ln\left(1 + \frac{I_{ph}}{I_{o}}\right)\left(I_{o} + I_{ph}\right) - \frac{CI\left(I_{o} + I_{ph}\right)}{I_{o} + I_{ph}} = 0$$
(25)

By rearranging eq. (25), one can obtain the equation of the second degree (26) below:

$$\left(C + 2R_{s}\left(I_{o} + I_{ph}\right)\right)I^{2} - \left(I_{o} + I_{ph}\right)\left[C\ln\left(1 + \frac{I_{ph}}{I_{o}}\right) + 2C + 2R_{s}\left(I_{o} + I_{ph}\right)\right]I + C\ln\left(1 + \frac{I_{ph}}{I_{o}}\right)\left(I_{o} + I_{ph}\right)^{2} = 0$$

(26)

To solve this equation of the second degree let's put:

$$X_1 = \left(C + 2R_s \left(I_o + I_{ph}\right)\right) \tag{27}$$

$$X_{2} = -\left(I_{o} + I_{ph}\right) \left[C \ln\left(1 + \frac{I_{ph}}{I_{o}}\right) + 2C + 2R_{s}\left(I_{o} + I_{ph}\right)\right]$$
(28)

$$X_{3} = C \ln\left(1 + \frac{I_{ph}}{I_{o}}\right) \left(I_{o} + I_{ph}\right)^{2}$$
⁽²⁹⁾

The eq. (26) could be rewritten as follows:

$$X_1 I^2 + X_2 I + X_3 = 0 ag{30}$$

The resolution of eq. (30) permits to obtain the following solutions:

$$I_{\max} = \frac{-X_2 \pm \sqrt{X_2^2 - 4X_1 X_3}}{2X_1}$$
(31)

$$V_{\max} = \frac{nNkT_c}{q} \ln\left(1 + \frac{I_{ph} - I_{\max}}{I_o}\right) - R_s I_{\max}$$
(32)

$$P_{\max} = V_{\max} I_{\max}$$
(33)

 I_{max} , V_{max} , and P_{max} are respectivement the maximum current, the maximum voltage and the maximum power.

 I_{ph} , I_o , R_s , n and C are respectively given by equations (6), (10), (12), (18) and (23).

3. RESULTS AND DISCUSSION

The chosen points for the parameters determination under reference conditions are mainly: the short-circuit current (0, I_{SC}), the open-circuit voltage point (0, V_{oc}), and the maximum power point (I_{mp} , V_{mp}).

For various conditions (considering the variation of the temperature) the peak power and the peak-power voltage are extracted from the manufacturer's datasheet by considering the temperature coefficients of these two variables.

For the simulation, two electric PV modules for different technologies were used; these include multi-crystalline silicon and mono-crystalline silicon, namely, Shell S75 and Shell SP70, respectively.

The solutions presented in this work have been obtained for $I_{\text{max}} = \frac{-X_2 - \sqrt{X_2^2 - 4X_1X_3}}{2X_1}$, which has been found as the best solution.

The comparison between the simulation and practical data [24] using a typical multicrystalline solar module (Shell S75) is illustrated in Table 1. The results show that the average relative error on peak-power voltage is 2.343475% and the average relative error on peak power is 0.89645%.

The comparison between the simulation and practical data [24] using a typical mono-crystalline solar module (Shell SP70) is illustrated in Table 2. The results show that the average relative error on peak-power voltage is 1.442225% and the average relative error on peak power is 0.358175%.

Conditions	Data provided by the	Simulated results	Relative error (%)
	Manufacturers		
Temperature 50°C	P _{mp} =66.5625 W	P _{mp} =67.1917 W	0.9453 on P _{mp}
Insolation 1000W/m ²	V _{mp} =15.7 V	V _{mp} =15.5953 V	0.6669 on V_{mp}
Temperature 25°C	$P_{mp}=75 W$	P _{mp} =74.9423 W	0.0769 on P_{mp}
Insolation 1000W/m ²	V _{mp} =17.6 V	V _{mp} =17.2636 V	1.9115 on V_{mp}
Temperature 0°C	P _{mp} =83.4375 W	P _{mp} =82.6723 W	0.9171 on P_{mp}
Insolation 1000W/m ²	V _{mp} =19.5 V	V _{mp} =18.9252 V	2.9476 on V_{mp}
Temperature -25°C	P _{mp} =91.875 W	P _{mp} =90.3623 W	1.6465 on P _{mp}
Insolation 1000W/m ²	V _{mp} =21.4 V	V _{mp} =20.5765 V	3.8479 on V_{mp}

Table 1. Simulation errors on the maximum power point at different temperature (shell S75)

Conditions	Data provided by the	Simulated results	Relative error (%)
	Manufacturers		
Temperature 50°C	P _{mp} =62.125 W	$P_{mp} = 62.5010 \text{ W}$	0.6052 on P _{mp}
Insolation 1000W/m	² V _{mp} =14.60 V	V _{mp} =14.8412 V	1.6519 on V_{mp}
Temperature 25°C	$P_{mp}=70 W$	P _{mp} =70.12 W	0.1712 on P_{mp}
Insolation 1000W/m	² V _{mp} =16.5 V	V _{mp} =16.4892 V	0.0657 on V_{mp}
Temperature 0°C	P _{mp} =77.875 W	P _{mp} =77.7395 W	0.1739 on P_{mp}
Insolation 1000W/m	² V _{mp} =18.40 V	V _{mp} =18.1339 V	1.4462 on V_{mp}
Temperature -25°C	P _{mp} =85.75 W	P _{mp} =85.3364 W	0.4824 on P_{mp}
Insolation 1000W/m	² V _{mp} =20.30 V	V _{mp} =19.7712 V	2.6051 on V_{mp}

Table 2. Simulation errors on the maximum power point at different temperature (shell SP70)

4. CONCLUSION

This study consisted in developing a new simplified model to optimize the photovoltaic solar cells. This analytical proposed model uses data provided by the constructor as a basis. Two types of solar module (Multi-crystalline silicon and mono-crystalline silicon) were modeled and evaluated. The model accuracy is also analyzed through comparison between manufacturer's data and simulation results. The obtained results prove the efficiency of the proposed modeling approach.

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How to cite this article:

Zieba Falama R, Dadjé A, Djongyang N and Doka S.Y. A new analytical modeling method for photovoltaic solar cells based on derivative power function. J. Fundam. Appl. Sci., 2016, 8(2), 426-437.