

EFFECT OF AGGREGATE GRAIN SIZE DISTRIBUTION ON PROPERTIES OF PERMEABLE CONCRETE

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ABSTRACT

In this study, the effect of aggregate grain size distribution and water/cement (W/C) ratio on the mechanical properties of permeable concrete is investigated. The aim of this study is to prepare permeable concrete mixture with optimum properties in terms of strength and permeability. For this purpose, five different permeable concrete mixtures with 0.3 constant W/C ratio and containing different proportions of coarse aggregate which are 5-15 and 15-25 mm, but containing no fine aggregate are prepared. In addition, three different concrete mixtures with 0.35 W/C ratio and containing 20% (by weight) fine aggregate and different proportions of coarse aggregate which are 5-15 mm and 15-25 mm are prepared. Afterwards, some tests related to the compressive strength, splitting tensile strength, flexural strength, ultrasonic pulse velocity (UPV) and permeability of concrete mixtures are conducted. Test results demonstrate that permeability, strength and UPV of the mixtures increased upon using 20 wt% of fine aggregate instead of coarse aggregate and upon reducing coarse aggregate grain diameter though W/C ratio of mixtures increases from 0.3 to 0.35.

Keywords: Permeable concrete, permeability, compressive strength, splitting tensile strength, flexural strength, ultrasonic pulse velocity

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1. INTRODUCTION

The first studies related with the permeable concrete have been conducted approximately 50 years ago in the United Kingdom, United States and Japan. There is also an increasing interest in this type of concrete recently. The most important properties of permeable concrete are to have large porosity between 15-35% that linked to each other within their structure. Thanks to the mentioned properties permeable concrete has a characteristic of high water permeability [1, 2]. Thus, it helps to prevent accidents by reducing the puddle adversely affecting drivers. At the same time, it improves the road safety by reducing the road surface glare. In this way, the drivers are protected against accidents [3-5]. In the world where the urbanization keeps spreading, the rainwater flows into the rivers, lakes or seas swiftly without reaching underground. The permeable concrete can provide transferring of rainwater to the ground in a controlled manner. It can also be solution to environmental problems by preventing soil erosion. The cause of the increasing use of pervious concrete in addition to a variety of its environmental benefit is to good flow of water from its structure as well as to reduce the pollution of ground by feeding ground water [6].

Presence of more porosity in the structure of permeable concrete increases the permeability of the concrete whereas the mechanical properties are affected negatively [1, 2, 7]. Permeable concrete can be used for the coating of pavements which are not exposed to heavy loads as well as sports fields and parking areas that are generally subjected to rainfall. Permeable concrete can eliminate the complex drainage system requirements by providing the leak of rain water from traffic surface [8-14].

Compressive strength of the permeable concrete is affected by W/C ratio, aggregate-binding ratio, aggregate grain diameter, casting, compacting, finishing and curing conditions. Generally, compressive strength of permeable concrete varies between 5 and 30 MPa [15]. As it is shown in test results, permeable concrete mixtures have the ability to store and hold the water within its structure. The mentioned stored water is equal to the water required for 1-month irrigation of 10 m² garden during a dry season [16]. The results of some related studies are summarized below.

The effect of W/C ratio and coarse aggregate content on the properties of permeable concrete was investigated in a study. Compressive strength and unit weight of the permeable concrete mixtures increased; however, their void ratio and permeability decreased with the decrease in W/C ratio. At the same time, W/C ratio, permeability and void ratio of permeable concrete decreased; however, its compressive strength and unit weight arised with the increase in cement content. Increasing coarse aggregate content caused a reduction in the unit weight of

the mixture as well as causing an increase in the void ratio and permeability of the mixture [17].

Low strength of permeable concrete was increased with the addition of fine aggregate. This fact was more obvious with the increase in fine aggregate content [18]. Water permeability decreases at the same time. Neptune [19] claimed that there is an inverse relationship between water permeability and strength properties of the permeable concrete. Besides, it was also reported that there occurred an increase in the compressive strength and reduction in permeability of concrete by increasing its void ratio.

Strength, fracture and fatigue of permeable concrete were investigated by Chen *et. al.*, [20]. The results indicate that flexural strength of the concrete is more sensitive to porosity than compressive strength. Permeable concrete has more significant size effect than conventional concrete. Polymer-modified pervious concrete demonstrates much higher fracture toughness and far longer fatigue life than supplementary cementitious material-modified pervious concrete at any stress level.

Bing *et. al.*, [21] stated that the ratio of cement paste / mortar should be in the ideal value within the permeable concrete. In the absence of adequate mortar content for covering aggregate surface in the permeable concrete, aggregate cannot be held on to each other, hence compressive strength of the mixture decreases. In the presence of high cement paste/mortar ratio, permeability of the concrete decreases.

Microscopic analysis of paste and aggregate distresses in pervious concrete in a wet, hard freeze climate was investigated by Vancura *et. al.*, [22] in another study. As a result of the investigation, it is found out that freeze/thaw distresses were the suspected cause of a majority of the subsurface cracks due to the similarity of the cracking patterns in the pervious concrete to cracking patterns in conventional concrete that were caused by freeze/thaw damage. While it was revealed that the freeze/thaw damage was the cause for the subsurface cracks in the pervious concrete samples, the cracking patterns were not consistent throughout the samples. Furthermore, the cracking patterns were not contingent upon the concrete mixture designs or aggregate type.

Bing *et. al.*, [21] stated that the size of aggregate and specific gravity of cement affected the permeability of permeable concrete significantly. A reduction was observed in the permeability parameter of permeable concrete by decreasing aggregate grain diameter at the same mix proportion.

There are several different studies about properties of permeable concrete in the literature [23-31]. However, the aim of this study is to prepare the optimum permeable concrete in terms of

strength and permeability by considering the effect of aggregate grain distribution and W/C ratio of concrete mixture. The experimental study was performed in two stages. During the first stage, 5 different concrete mixtures with 0.3 W/C ratio and containing different amounts of, 5-15 mm and 15-25 mm, aggregate size fraction were prepared in the absence of fine aggregate. During the second stage of the study, 3 different mixtures with 0.35 W/C ratio and containing 20% 0-3 mm fine aggregate and different proportions of, 5-15 mm and 15-25 mm, aggregate size fraction were designed. Therefore, 8 different permeable concrete mixtures were prepared. The compressive strength, splitting tensile strength, flexural strength, ultrasonic pulse velocity and water permeability of the concrete mixtures were investigated.

2. EXPERIMENTAL STUDY

2.1. Materials

In this study, a CEM I 42.5 R type cement is used as binder. The chemical and some physical properties of the cement obtained from the producer are shown in Table 1. 0-3 mm, 5-15 mm and 15-25 mm sized fraction crushed limestone aggregates are used during the preparation of the mixtures. The sieve analysis results and some physical properties of the aggregate are shown in Table 2 and 3 respectively. The specific gravity, water absorption capacity and unit weight of the aggregates are determined in accordance with EN 1097-6 and EN 1097-3 standards respectively.

8 different permeable concrete mixtures with two different W/C ratios and containing different aggregate proportions were prepared. Cement and air content were kept constant as 300 kg/m³ and 20% (by volume) in all of the mixtures. The corrected mix proportion of the permeable mixtures as well as their theoretical and measured unit weight values are given in the Table 4. As it can be seen from Table 4, two permeable concrete series were prepared. The C series were without fine aggregate while C1 contained 100% 5-15 mm aggregate size fraction. In C2 mixtures 100% of 15-25 mm aggregate size fraction was used. However, in the C3, C4 and C5 mixtures, 5-15 mm aggregate was replaced with 15-25 mm aggregate as 25%, 50% and 75%. In the D concrete series, in addition to coarse aggregate, fine aggregate was used as 20 wt% of total aggregate content. In D1 and D2 mixtures, in addition to fine aggregate (as 20 wt% of total aggregate content), 80% of 5-15 mm and 15-25 mm aggregates were used respectively. In the D3 mixture 40% 5-15 mm, 40% 15-25 mm and 20% of 0-3 mm aggregates were used.

The compressive strength, splitting tensile strength and ultrasonic pulse velocity of 150 mm cube specimens and center point flexural strength of 100x100x600 mm prism specimens were

obtained during 28-day period in accordance with EN 12390-3 [38], EN 12390-6 [39], ASTM C597 [00] and EN 12390-5 [40] standards respectively. Besides, permeability of the concrete mixture was tested on 150 mm cube specimens at the end of 28-day water curing. As it is known, the void ratio of permeable concrete is much higher than that of the conventional concrete mixture. When the permeability of concrete mixture was measured in accordance with EN 12390-8 standard, the water was observed on the side surface of the concrete sample before reaching the lower surface. Hence, the permeability of the permeable concrete could not be measured in accordance with the standard methods. In order to measure the permeability of permeable concrete, the side surfaces of the cubes were sealed with an acrylic copolymer-based sealing material. As it is shown in Figure 2, the 500 ml water was decanted into concrete sample and the chronometer was started. The chronometer was stopped upon seeing the water in the lower side of the concrete sample. The transition time of water from the concrete sample was measured. Besides, the water absorption capacity of the concrete mixtures was compared by measuring the amount of water passed from the concrete sample.

3. TEST RESULTS AND DISCUSSION

3.1. Compressive, splitting tensile and flexural strength

The 28-day compressive strength of 150 mm cubic permeable concrete mixtures are shown in Figure 2. As it can be seen from the Figure, 28-day compressive strength of C series mixture were determined as 6.1 to 8.2 MPa. The minimum compressive strength was found in C1 mixture containing 100% of 5-15 mm sized aggregate. Compared to the C1 mixture, compressive strength of the mixture increased upon utilization of 15-25 mm sized aggregate. This was insistently stated for the mixture containing 50% of 5-15 mm and 15-25 mm sized aggregates. As it was mentioned earlier, C series mixture contains no fine aggregate. Compared to the C series without fine aggregate, compressive strength of the mixture increased by using fine aggregate in spite of increasing W/C ratio of the mixture from 0.3 to 0.35. Thus, in this case, the sand proportion change factor was more effective on the compressive strength of the mixture compared to W/C ratio factor. In the mixture containing fine aggregate (Series D), compressive strength of the mixtures was obtained as 11.69 to 16.88 MPa. The maximum performance in terms of compressive strength was shown in the D3 mixture containing 20% 0-3 mm, 40% 5-15 mm and 40% 15-25 mm sized aggregates.

28-day-long splitting tensile and flexural strength of concrete specimens are shown in Figure 3 and 4 respectively. As it can be seen from test results, splitting tensile strength of C series mixture containing no fine aggregate varies from 1.22 to 1.76 MPa. Mentioned range for

flexural strength was found between 1.5 and 1.82 MPa. Similar to compressive strength behavior, the maximum and minimum splitting tensile and flexural strength were found in C1 and C4 mixtures respectively. The performance of concrete mixture in terms of splitting tensile and flexural strength was improved by adding fine aggregate to the mixture. D3 mixture showed maximum splitting tensile and flexural strength.

The relationship between compressive strength – splitting tensile strength, and –flexural strength of the concrete mixture is shown in Figure 5. Figure 5 indicates that there is a strong relationship between strength parameters of concrete mixtures.

As it can be seen from the test results, in spite of higher W/C ratio of series D mixture compared to the series C mixture, this mixture showed compressive strength approximately 2 times higher than that of C series. Related to the aggregate proportion, the fill rate of the permeable concrete increased upon using fine aggregate. Hence, compressive strength of the mixture decreased in the absence of fine aggregate and with the increase in coarse aggregate grain diameter.

3.2. Ultrasonic pulse velocity

The UPV values of 28-day water cured 150 mm cubic concrete specimens are given in Figure 6. As it is known that the age, moisture condition, concrete porosity, aggregate type and ITZ characteristics can affect the UPV value of the concrete mixture. UPV value of C series mixture was changed in the range of 1.02 and 1.14 Km/s. Mentioned range was found 1.17 and 1.49 Km/s for Series D. UPV values of all permeable concrete mixtures were lower than 2 Km/s, the limit specified for weak concrete by Whitehurst [32]. The results indicate that UPV values of permeable concrete mixture were slightly increased by utilization of fine aggregate and decreasing coarse aggregate grain diameter in spite of increasing W/C ratio of the mixture. This fact is that due to reduction in void ratio of concrete mixture by adding fine aggregate particle, it acts as a filler. Besides, Figure 7 indicates that there is a strong relationship between compressive strength and UPV values as well as splitting tensile strength and UPV values of permeable concrete mixture.

3.3. Permeability test results

The permeability test results are given in Table 5. As it is known, the entrapped air and capillary porosity of the concrete affects the permeability of the concrete mixtures [33]. In D series mixture, W/C ratio of concrete mixture was increased from 0.3 to 0.35 by adding fine aggregate in order to provide adequate permeability properties for concrete mixture. Hence, D series mixture would be expected to be more permeable compared to that of the C series. However, the reverse results are obtained as it can be seen from Table 5. Thus, coarse

aggregate gradation, aggregate proportion and its size fraction as well as presence of fine aggregate in the mixture are the other important factors influencing permeability of the concrete. The minimum permeability value is shown in D3 mixture due to its proper aggregate proportion. C2 mixture shows the best performance in terms of water permeability. The relationship between compressive strength and water permeability of permeable concrete mixture is shown in Figure 8. As it can be seen from the Figure, there is inverse linear relation between strength and permeability of the concrete as expected. Void ratio of the concrete mixture is high in the absence of fine aggregate. Concrete mixture showed lower performance in terms of strength due to its higher porosity. Permeability of concrete mixture decreased by presence of fine aggregate and by decreasing coarse aggregate grain diameter. When the compressive strength of concrete mixture has no big significance, C series mixture can be used as permeable concrete. D3 mixture shows best performance in terms of compressive strength; moreover, it shows acceptable water permeability character.

4. CONCLUSION

In accordance with the used materials and obtained results, following conclusions may be drawn:

It was observed that in the absence of fine aggregate, ultrasonic pulse velocity as well as compressive, splitting tensile and flexural strength of mixtures including just 15-25 mm or 5-15 mm sized aggregates were lower than the mixtures with both 15-25 and 5-15 mm sized aggregates. This fact was more obvious in the mixture containing 50% 5-15 mm and 50% 15-25 mm sized aggregates. Strength performance and ultrasonic pulse velocity of permeable concrete mixture were improved by using 20% fine aggregate and decreasing coarse aggregate grain diameter although the W/C ratio of the mixture increased. However, permeability of pervious concrete decreased with the addition of fine aggregate. This fact was due to the reduction in void ratio of concrete mixture by adding fine aggregate particle acting as a filler. The reverse results were obtained in the absence of fine aggregate.

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Table 1. Some physical, chemical and mechanical properties of cement

Chemical properties		Mechanical and physical properties		
Oxide	(%)	Properties	Cement	
SiO ₂	19.13	Compressive strength (MPa)	2 Day	23.5
Al ₂ O ₃	5.10		7 Day	38.6
Fe ₂ O ₃	3.51		28 Day	48.4
CaO	63.29		Blaine Specific Surface (cm ² /g)	3680
MgO	1.06	Fineness	Residual of 0.090 mm sieve (%)	1.1
Free CaO	0.96		Residual of 0.032 mm sieve (%)	23.4
Na ₂ O	0.34			
K ₂ O	0.77			
SO ₃	2.83			
LOI	3.51			

Table 2. Particle size distribution of coarse and fine aggregates

Sieve size (mm)	Passing (%)		
	0-3 mm	5-15 mm	15-25 mm
32	100	100	100
16	100	100	5
8	100	42	3
4	100	2	0
2	75	0	0
1	53	0	0
0.50	27	0	0
0.25	14	0	0

Table 3. Physical properties of coarse and fine aggregates

	0-3 mm	5-15 mm	15-25 mm
Loose bulk density (kg/m ³)	1793	1504	1395
Surface saturated dry specific gravity	2.61	2.64	2.67
Water absorption capacity (%)	0.67	0.21	0.35

Table 4. Corrected mix proportions and designations of the permeable concrete mixtures

Mix	Cement (kg/m ³)	Water (kg/m ³)	W/C ratio	Aggregate			Measured unit weight (kg/m ³)
				15-25 mm (kg/m ³)	5-15 mm (kg/m ³)	0-3 mm (kg/m ³)	
C1	310	93	0.30	-	1686	-	2089
C2	312	94	0.30	1716	-	-	2114
C3	311	93	0.30	1272	422	-	2098
C4	309	93	0.30	843	840	-	2084
C5	300	90	0.30	409	1225	-	2024
D1	312	109	0.35	-	1323	336	2132
D2	317	111	0.35	1350	-	341	2169
D3	316	111	0.35	673	670	340	2160

Table 5. Permeability test results

Mix	The initial water outlet time from the sample (s)	Water transition time from the sample (s)	Amount of water passed from the sample (ml)	Rate of water passed from the sample (%)
C1	9.0	31	425	85
C2	4.7	225	469	94
C3	9.7	31	372	74
C4	4.4	27	392	78
C5	7.2	28	351	70
D1	9.2	35	347	68
D2	20.0	51	312	62
D3	13.0	32	289	59

**Fig.1.** Permeability test

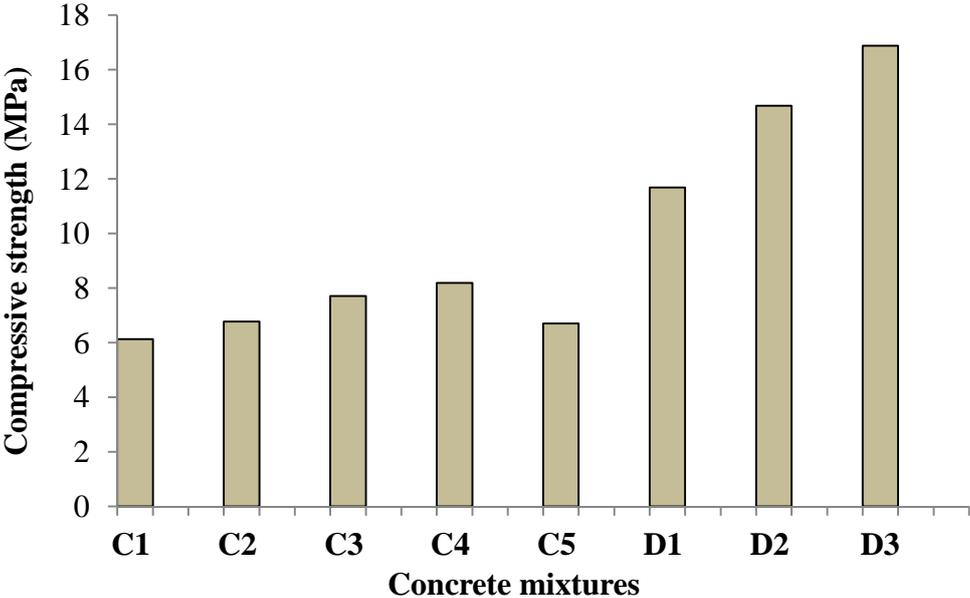


Fig.2. Compressive strength test results of the permeable concrete mixtures

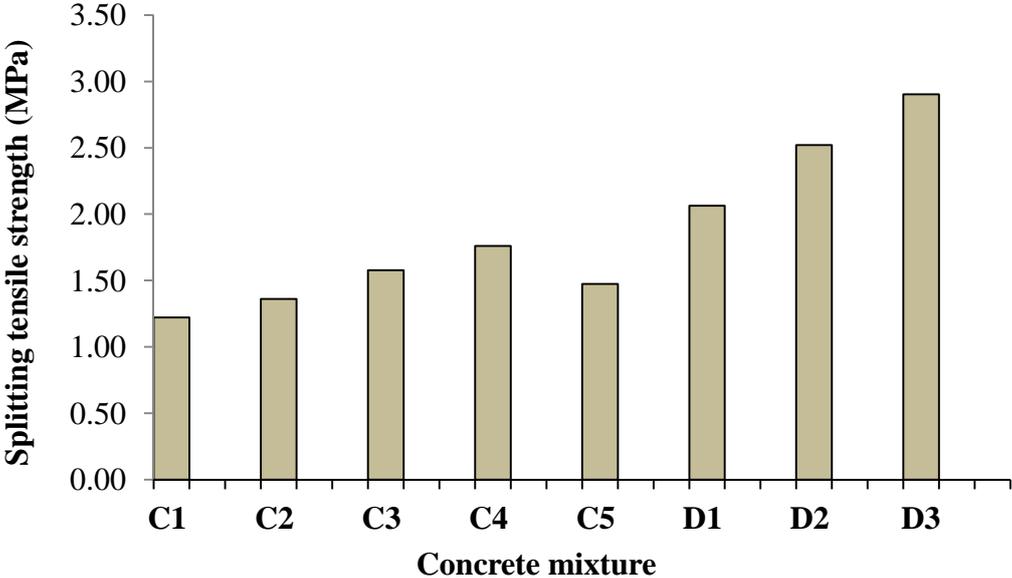


Fig.3. Splitting tensile strength test results

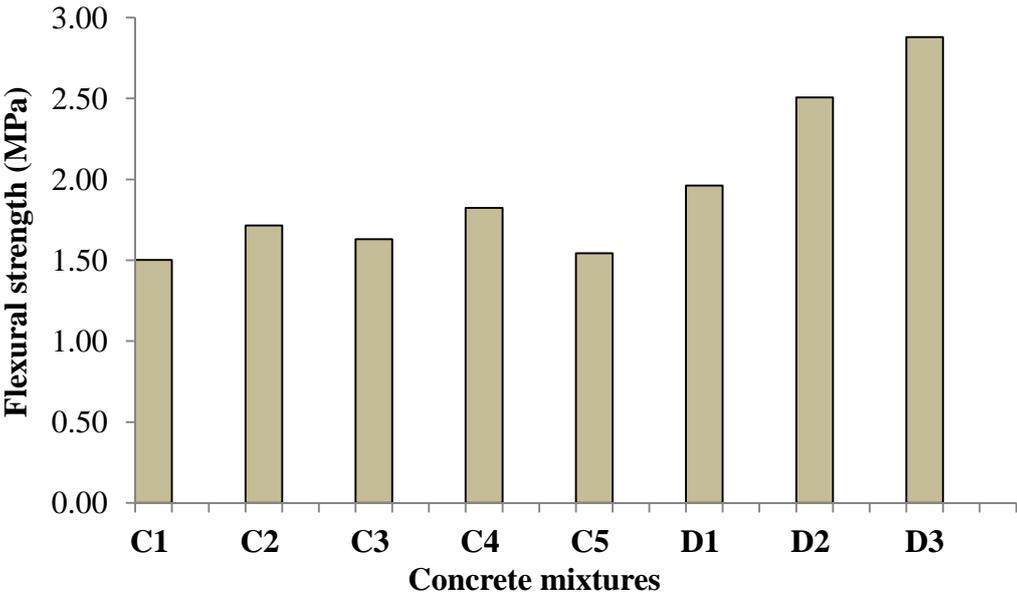


Fig.4. Flexural strength test results

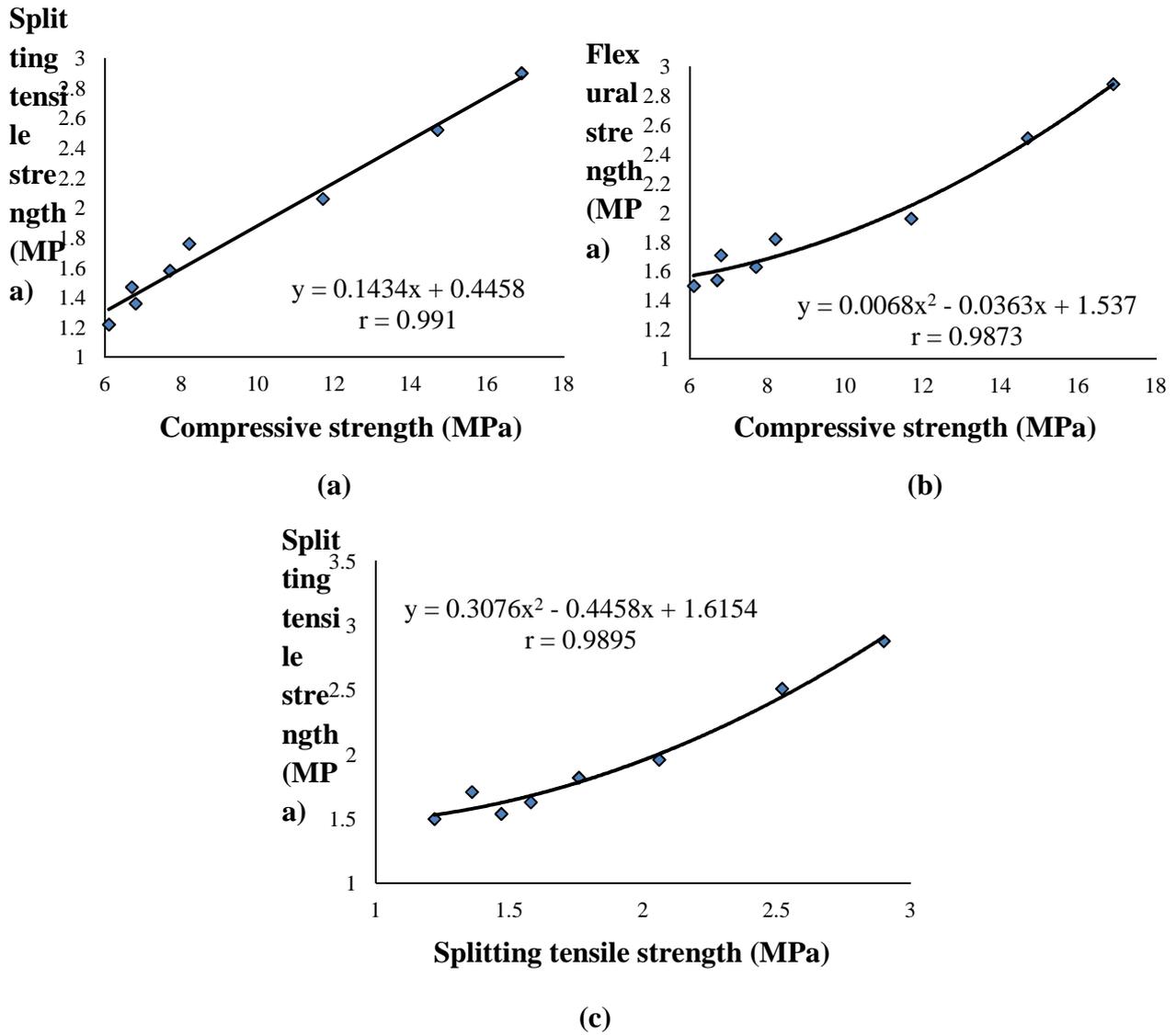


Fig.5. Strength relationships; a) compressive strength – splitting tensile strength, b) compressive strength – flexural strength c) splitting tensile – flexural strength

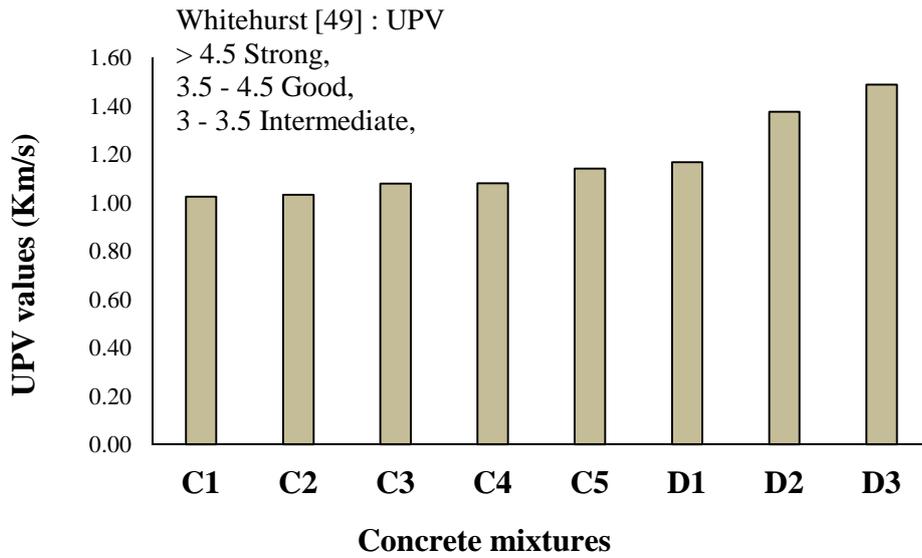


Fig.6. Ultrasonic pulse velocity test results

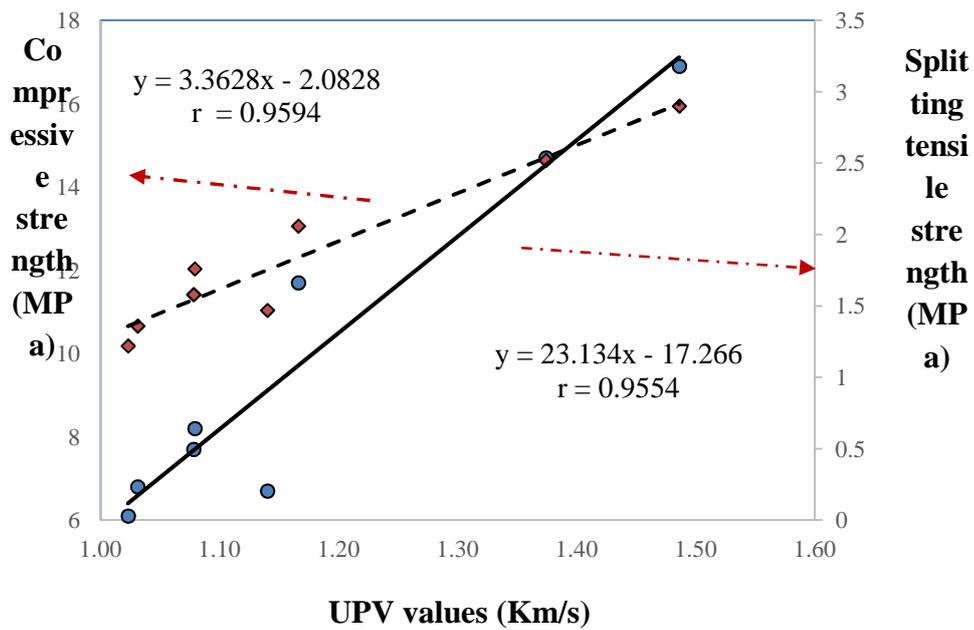


Fig.7. Relationship between UPV and -compressive strength and -splitting tensile strength of permeable concrete mixture

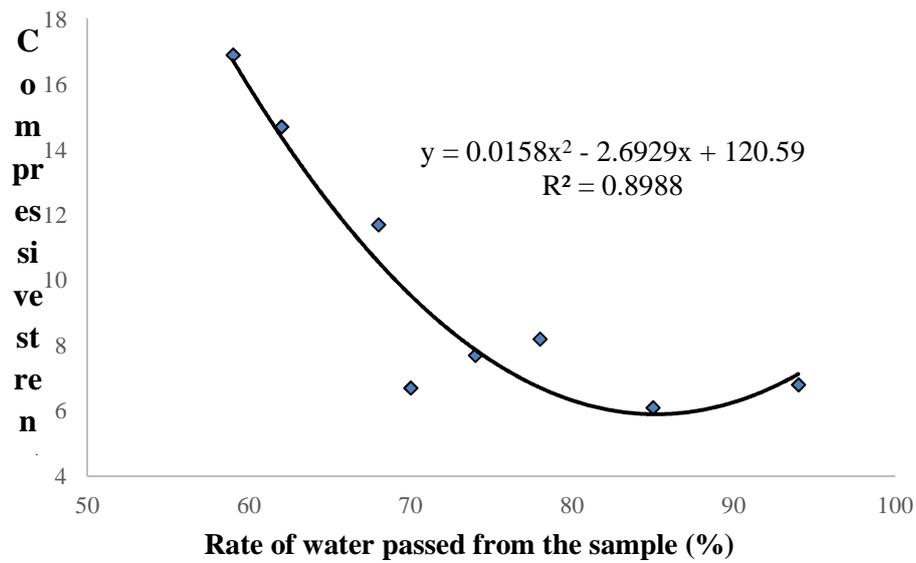


Fig.8. Relationship between compressive strength and rate of water passed from the permeable concrete sample

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