

## DETERMINATION OF DESIGN INFLOW RATE IN FURROW IRRIGATION USING SIMULATED ADVANCE AND RECESSION CURVES

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### **ABSTRACT**

*Advance and recession curves were simulated for three stages of maize growth in furrow irrigation. The selected stages were: the emergence stage, two weeks after planting; the development stage, about two months after planting; and the maturing stage, about one month to harvest time. The advance and recession times were predicted for successive points along the furrow lines for various inflow rates at the development stage of the crop growth using three models. The simulated advance and recession data were used to compute the intake opportunity time distribution along the furrow line. The infiltrated depth distribution and hence the water application efficiency and distribution uniformity were computed for the inflow rate, which gave 87% and 89% for the maize emergence stage; 75% and 60% for the maize development stage and 95% and 89% for the maize maturing stage. The design inflow rate for each furrow was taken as the minimum inflow rate which gave rise to a minimum water application efficiency of 60% and a minimum distribution uniformity of 75%. It is recommended that the procedure described in this work is useful for the modification of existing furrow irrigation systems and the establishment of new ones. Also, the design procedure presented can be used for any field that is suitable for furrow irrigation system by making use of the relevant parameter estimates that can be obtained from the field.*

### **INTRODUCTION**

In the development of a furrow irrigation system, certain factors are considered. These factors could be political, social, economic or technical. The aspirations, however, are realized or lost at the farm level because, whether or not the goal is achieved at the end will ultimately translate into crop water requirements during each growing season. Therefore the farm level should be the logical focus of irrigation planning and design; Doorenbos, et al. (1980).

For an adequate inflow rate, the intake opportunity times at measurement points along the furrow length will be approximately the same, thus indicating that the advance and recession curves must be

approximately parallel (Mudiare, 1987 and Okereke, 1999) Fok and Bishop (1965) advance model was used to simulate advance data and compared with field data while for the vertical and horizontal recessions, Shockley, et al (1964) and Sherman and Singh (1978) models were used respectively.

### **Hydraulics of Furrow Irrigation**

The flow rate down the furrow equals the application rate (Elliott and Walker 1982), which is given as:

$$Q = \frac{(r)^{8/3} S^2}{n} \quad (1)$$

$$\text{and } q = Q/r \quad (2)$$

$$= \frac{(r)^{8/3} S^2}{n} \quad (3)$$

where

$Q$  = application rate

$q$  = inflow per unit width of furrow

$r$  = flow depth of furrow

$s$  = bed slope of furrow

$n$  = Manning's roughness coefficient

### Infiltration in furrows

The infiltration function  $r(t')$  is defined as the rate at which water enters into the soil per unit area which is taken as a power function of time. The total quantity of water that is absorbed by the soil after time  $t'$  from the beginning of ponding, is:

$$D(t') = \int t' o^r(t') dt' \quad (4)$$

And

$$r(t') = kt'^n, \quad (5)$$

$r$  = infiltrated depth of water

$t'$  = elapsed opportunity time

$k, n$  = empirical constants

### Advance Rate in furrows:

The advance rate of the water front down the furrow is found to be a power function of time of advance (Sirjani and Wallender, 1989).

$$X = at_x^b \dots \quad (6)$$

Where

$X$  = advance distance

$t_x$ , = time to advance a distance  $X$

$a$  and  $b$  = empirical constants

### Recession rate in furrows:

The Shockley, et al (1964) equation also known as SWP model is given by Ram and Singh (1982) as:

$$t_v = t_o - t_a \quad (7)$$

$$= r^2 / 2sq \quad (8)$$

for the vertical recession

Where

$t_v$  = time of vertical recession  
 $t_o$  = time at completion of vertical recession  
 $t_a$  = time of application cut off  
 $r$  = average flow depth  
 $s$  = furrow slope  
 $q$  = inflow rate per unit width while Sherman and Singh (1978) derived an expression for the time of horizontal recession for a free-draining furrow as:

$$t_r = \frac{1}{60} \left( \frac{x}{\alpha t^{\beta-1}} \right)^{1/\beta} \quad (9)$$

where

$\beta$  = 5/3 for manning's expression

$X$  = distance from the upstream end

$$\alpha = S^{1/2} / n \quad (10)$$

$$f = \frac{1}{120} \left( \frac{D_o}{t_o} + \frac{D_N}{t_N} \right) \quad (11)$$

### Water application efficiency and distribution uniformity:

Irrigation system efficiency can be evaluated by two types of efficiency parameters which includes: water application efficiency and water distribution uniformity or efficiency.

Merriam (1980) and Adamu (1990) defined water application efficiency as the ratio of the average low quarter depth of irrigation water infiltrated and stored in the root zone to the total depth of water delivered to the field thus:

$$E_a = \frac{D_z}{D_g} * 100 \quad (12)$$

where

$E_a$  = water application efficiency (%)

$D_z$  = average low-quarter depth infiltrated and stored

$D_g$  = gross irrigation depth.

Hart, et al (1979) specified that the water application efficiency,  $E_a$ , must not be less than 60% for satisfactory furrow irrigation performance.

Water distribution uniformity is defined as the ratio of the average, low- quarter depth

of irrigation water infiltrated and stored to the average depth infiltrated, expressed in percent, thus (Merriam, 1980 and Adamu, 1990):

$$U_d = \frac{D_z}{D_{av}} * 100 \quad (13)$$

Where

$U_d$  = water distribution uniformity (%)

$D_{av}$  = average infiltrated depth

Water distribution uniformity,  $U_d$  must not be less than 70% for satisfactory furrow irrigation performance (Hart, et al 1979).

## MATERIALS AND METHODS

The field work was carried out at the Lake Geriyo Irrigation Project located in Yola, Adamawa State of Nigeria, on the Upper Benue River Basin Development Authority Irrigation Project. The periods of the experiments were from January to June, 1996 and the early part of 1997. The experimental plot was planted to a maize crop of variety PAN 6195 of 120 days duration.

Lake Geriyo Irrigation Project (Lat  $9.30^{\circ}\text{N}$ , Long  $12.25^{\circ}\text{E}$ ), is located in the North-East of Yola town. The area records a mean annual rainfall of 910mm, the average maximum temperature is  $35^{\circ}\text{C}$  while the average minimum temperature is  $23^{\circ}\text{C}$ . The vegetation of the area is savannah type (Sudan savannah).

The experimental field measured about 6m by 110m producing six ridges and five furrows. The field was graded to a furrow slope of 0.10%. A drainage channel was provided at a distance of 100m from the upper end of each furrow, thus giving a total advance distance of 100m. The experimental field was found to have a soil type of predominantly sandy loam soil.

The field experiments were necessary in order to generate relevant data to verify the advance and recession models.

### Determination of design inflow rate

The procedure adopted is to assume a value for the inflow rate,  $q$ , in the range  $0.01 \leq q \leq 0.36 \text{ m}^3/\text{min}/\text{m}$  and simulate the advance and recession times for successive points along the furrow length (Michael, 1978). The intake opportunity times and infiltrated depths along the furrow length are then obtained using the advance and recession data. The water application efficiency and distribution uniformity are calculated and compared with recommended values for efficient furrow irrigation available in the literature. The procedure is repeated until the calculated water application efficiency and distribution uniformity indicate an efficient furrow irrigation system.

## RESULTS AND DISCUSSION.

### Results:

The summary of the design parameters are presented below:

Average slope of furrow strip,  $s = 0.001$

Average infiltration depth,  $D = 0.5 t^{0.78}$

Manning's roughness coefficient,  $n = 0.025$

Length of furrow strip,  $X = 100\text{m}$

Water application depth  $= 20\text{mm}$

Infiltration opportunity time,  $t' = (20/0.5)^{1/0.78} = 113\text{min}$

Water application efficiency,  $E_a. = 60\%$  (assumed)

Corresponding design inflow rate,  $q$

$$q = (0.020 * 100) / (0.60 * 113) = 0.03\text{m}^3/\text{min}/\text{m}$$

The calculated corresponding inflow rate of  $q = 0.03\text{m}^3/\text{min}/\text{m}$  based on maize crop water requirement, evaluated average infiltration depth and soil moisture capacity were tested for water application efficiency and water distribution uniformity.

### Determination of water application efficiency and distribution uniformity

The maize development stage (stage II) is normally the stage at which water stress can most significantly affect the crop yield. Thus, the furrow irrigation system design is

based on the parameters obtained for this stage. The evaluated water application efficiency and water distribution uniformity

for  $q=0.03\text{m}^3/\text{min}/\text{m}$  of the three growth stages of maize are presented in Tables 1, 2 and 3.

**Table 1:** Evaluation of Water Application Efficiency and Distribution Uniformity for  $q=0.03\text{m}^3/\text{min}/\text{m}$  for stage I.

S/No	Dist. X (m)	$t_x$ (min)	$t_i$ (min)	$t'$ (min)	T (min)
1	0	0	28.0	28.0	-
2	10	4.0	35.0	31.0	29.5
3	20	8.0	38.9	30.9	31.0
4	30	12.0	45.2	33.2	32.1
5	40	16.0	47.8	31.8	32.5
6	50	20.0	50.2	30.2	31.0
7	60	24.0	52.4	28.4	29.3
8	70	28.0	54.5	26.5	27.5
9	80	32.0	56.5	24.5	25.5
10	90	36.0	58.3	22.3	23.4
11	100	40.0	60.1	20.1	21.2

$$t_x = (X/0.03) (0.005 + 0.00054t^{0.8})$$

$$t_x = 40; t_i = t_o + 1.83x^{0.6}$$

$$t' = t_i - t_x$$

$$t_N = 807$$

$$R_x = 0.052; t_{av} = 30.12\text{min}$$

$$D_{av} = 9.2; D_g = 9\text{mm}$$

$$t'_{min} = 30\text{min}; D_{min} = 8\text{mm}$$

$$U_d = (D_{min}/D_{av}) * 100 = 87\% \text{ (satisfactory)}$$

$$E_a = (D_{min}/D_g) * 100 = 89\% \text{ (satisfactory)}$$

**Table 2:** Evaluation of Water Application Efficiency and Distribution Uniformity for  $q = 0.03\text{m}^3/\text{min}/\text{m}$  for stage II.

S/No	Dist. X (m)	$t_x$ (min)	$t_i$ (min)	$t'$ (min)	T (min)
1	0	0	18.9	18.9	-
2	10	2.3	35.1	32.8	25.9
3	20	4.7	43.4	38.7	35.8
4	30	7.0	50.1	43.1	40.9
5	40	9.3	56.0	46.7	44.9
6	50	11.7	61.4	49.7	48.2
7	60	14.0	66.3	52.3	51.0
8	70	16.0	70.8	54.8	53.6
9	80	18.7	75.2	56.5	55.7
10	90	21.0	79.3	58.3	57.4
11	100	23.3	83.2	59.9	59.1

$$t_x = (X/0.03) (0.005 + 0.0002t^{0.7})^8$$

$$t_x = 23.3; t_i = 17.5; t_o = 18.9$$

$$t_i = 18.9 + 4.06 x^{0.6}$$

$$t_N = 796$$

$$R_x = 23.3/(796-23.3) = 0.030$$

$$t_{av} = 47.2$$

$$D_{av} = 0.2 (47.2)^{0.7} = 4\text{mm}$$

$$D_g = (0.03 * 17.5/100) * 1000 = 5\text{mm}$$

$$t'_{min} = (26+36)/2 = 31\text{mm}$$

$$D_{min} = 0.2 (31)^{0.7} = 3\text{mm}$$

$$U_d = (3/4) * 100 = 75\% \text{ (satisfactory)}$$

$$E_a = (3/5) * 100 = 60\% \text{ (satisfactory)}$$

**Table 3: Evaluation of Water Application and Distribution Uniformity  
for  $q = 0.03\text{m}^3/\text{min}/\text{m}$  for stage III.**

S/No	Dist. X (m)	$T_x$ (min)	$t_i$ (min)	$t'$ (min)	T (min)
1	0	0	31.7	31.7	-
2	10	4.0	41.8	37.8	34.8
3	20	8.0	47.0	39.0	38.4
4	30	12.0	51.2	39.2	39.1
5	40	16.0	54.8	38.8	39.0
6	50	20.0	58.2	38.2	38.5
7	60	24.0	61.2	37.2	37.7
8	70	28.0	64.1	36.1	36.7
9	80	32.0	66.8	34.8	35.5
10	90	36.0	69.3	33.3	34.1
11	100	40.0	71.8	31.8	32.6

$$\begin{aligned}
 t_r &= (X/0.03) (0.006+0.0007^{t_0}) \\
 t_x &= 40; = t_a = 30\text{min} \\
 t_i &= 31.7+2.53X^{0.6} \\
 t_N &= 619.5; t'_{av} = 36.84 \\
 D_{av} &= 0.7(36.84)^{0.6} = 8.43\text{mm} \\
 D_g &= (0.03*30/100)*1000 = 9\text{mm} \\
 t'_{min} &= 36.6 \\
 D_{min} &= 0.7(36.6)^{0.6} = 8\text{mm} \\
 U_d &= (8/8.43)*100 = 95\% \text{ (satisfactory)} \\
 E_a &= (8/9)*100 = 89\% \text{ (satisfactory)}
 \end{aligned}$$

The result of the simulated advance and recession curves, the water application efficiency and water distribution uniformity are given in Tables 1, 2 and 3 respectively for the three stages of growth of maize, namely emergence (stage 1), development (stage 11) and maturing (stage 111) while the curves are shown in Figures 1, 2, and 3 for the design inflow rate of  $0.03\text{m}^3/\text{min}/\text{m}$ . The application rate,  $q = 0.03\text{m}^3/\text{min}/\text{m}$  is found to be adequate for the furrow irrigation system based on the computed water application efficiency and distribution uniformity

## DISCUSSION

### Rate of Advance in Furrows

Fok and Bishop (1965) equation which is a form of the volume balance equation, was modified further and simplified on the assumption that both advance and infiltration functions can be represented by power

functions of time. On verification (see Tables 1,2 and 3) the equation is found to be suitable for the maize emergence, development and maturing stages with mean error not exceeding -15.1 %.

### Rate of Recession in Furrows

It is an experimental fact that when the water application at the upstream end of the furrow is cut off, water recedes first vertically and then horizontally due to the combined effects of infiltration and surface runoff. On verification (see Tables 1,2, and .3), the Shockley, Woodward and Phelan (SWP) 1964 vertical recession model was found to be better in terms of error margin between observed and calculated vertical recession times when compared to the time of irrigation, the error margin not exceeding -4%.

The Sherman and Singh (1978) and Ram and Singh (1982) in the horizontal recession model assumed constant average infiltration rate and used kinematics wave theory to derive explicit expressions for the time of horizontal recession for a free draining furrow. The error margin was within allowable limit and thus found suitable for the field test.

### Evaluation of Inflow Rate:

Various inflow rates were evaluated at different stages of maize growth. They yielded

satisfactory advance ratio and satisfactory distribution efficiency/ uniformity but very low application efficiency. But an evaluated inflow rate of  $0.03\text{m}^3/\text{min}/\text{m}$  yielded satisfactory advance ratio; satisfactory water distribution efficiencies/ uniformities and

water application efficiencies of 87% and 89% for the maize emergence stage; 75% and 60% for the maize development stage; and 95% and 89% for the maize maturing stage respectively.

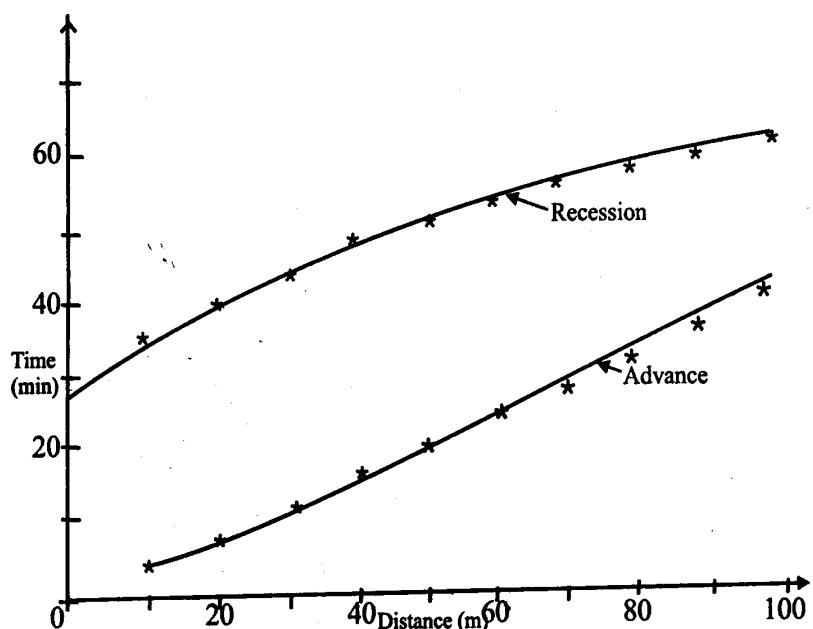


Fig. 1 Simulated Advance and Recession Curves for  $q_a = 0.03\text{m}^3/\text{min}/\text{m}$  of maize stage I

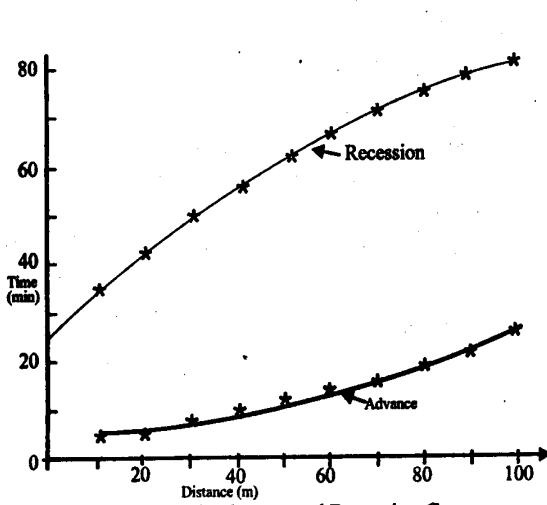


Fig. 2 Simulated Advance and Recession Curves for  $q_a = 0.03\text{m}^3/\text{min}/\text{m}$  of maize stage II

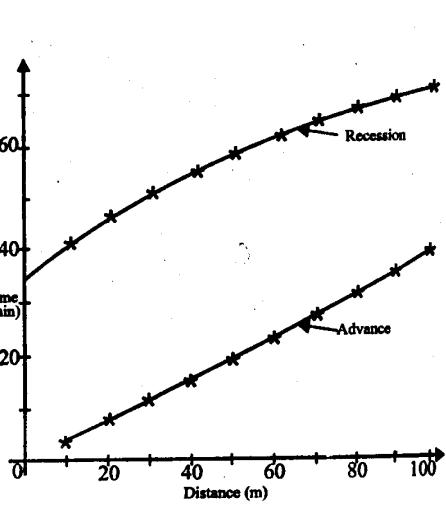


Fig. 3 Simulated Advance and Recession Curves for  $q_a = 0.03\text{m}^3/\text{min}/\text{m}$  of maize stage III

## CONCLUSION

In conclusion, the following points are made:

- a. The optimum application rate,  $q$ , of  $0.03m^3/min/m$  for the three phenological stages of growth of maize was obtained and it gave satisfactory water distribution uniformities and application efficiencies of 87% and 89% for the emergence stage; 75% and 60% for the development stage; and 95% and 89% for the maturing stage respectively.
- b. The procedure in this work is useful both for the modification of existing furrow irrigation systems and the establishment of new ones.

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