

RISK-BASED SECURITY ASSESSMENT OF POWER SYSTEM VOLTAGE DROP: A CASE STUDY OF NIGERIAN 330KV 41-BUS TRANSMISSION GRID

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ABSTRACT

Researchers, system operators, engineers, and utility owners are making extensive efforts to fully utilize the installed facilities of power systems in response to increasing energy demand and thereby creating security challenges for power systems. Thus, this paper addresses the problem of power system security using the risk-based security assessment. A linearized risk-based method which uses fast decoupled load flow algorithm was used to assess the low voltage security of power systems. The method is based on the concept of risk, which considers both the likelihood of occurrence and the severity of the contingency. It requires the probability of voltage distribution, the probability of contingency and severity function to evaluate the impact of the contingency. The proposed method was illustrated on a real power system, the simulation model of the Nigerian 41 bus 330kV transmission grid network for calculating the risk indices of three simulated contingencies at various rates of occurrence. The calculated risk indices show that as the rate of occurrence increases, risk indices increase. This indicates that contingencies with high rate of occurrence with little impact possess higher or equivalent risk to contingencies with great impact, which rarely occur. Therefore, system operator, technician, and engineer should quickly identify, investigate, and proffer solution to them in order to alleviate their effects on the network and improve service delivery.

Keywords: Contingency, risk-based index, severity function, power system security

1. INTRODUCTION

The growing population and urbanization of Nigeria have resulted to the increase in size and complexity of the Nigeria power system network. Most components of the network are interconnected into a vast power grid for economic and technological reasons [1]. A response to increased power demand up to 19,100MW compared to the network operational capability of 5,500MW [2] is to fully utilize the installed facilities of the power system. However, power systems operated at this state are closer to their thermal and stability limits and they are constantly subjected to contingencies [3]. In order to limit the consequences of contingencies that are unpredictable and unavoidable in power systems, power systems security assessment must be carried out. Power system security involves practices, designed to keep the system operating even if one or more components fails [4].Determination of power system security level is done by two methods: deterministic and probabilistic (Risk-Based) methods. Deterministic methods evaluate security levels based

on the most severe and credible contingency while probabilistic methods are based on the concept of risk which considers both probability and impact of the contingency [5, 6, 7, 8].

This paper is aimed at evaluating the Nigerian 330KV transmission grid using the Risk-Based security assessment (RBSA) approach.

2. CONCEPT OF RISK

Risk is defined as a condition under which there is a possibility of an adverse deviation from a desired outcome that is expected or hoped for [9]. The risk of a power system is referred to as the system's exposure to failure and its analysis is done by considering both the probability of occurrence of an event and the impact of the event [10]. Furthermore, the amount of impact multiplied by the corresponding probability of outcome is refers to as the "degree of risk" [9]. The degree of risk of the current operating condition can be quantified as "risk index" [11].

(1)

The risk index can quantitatively capture probabilities (likelihood) of occurrence of contingencies and their impact. In simplified terms, risk index is the product of event likelihood and its severity.

In mathematical terms;

Risk Index

= (probability of event occurring)

× (Impact of event occurring)

From equation (1), the risk index of a real power system will be[10];

$$Risk(SM_{t,f}) = \sum_{i} P_{r}(E_{i}) \left| \sum_{i} P_{r}(SM | E_{i}, X_{t,f}) \times Sev(E_{i}, SM) \right|$$
(2)

Where,

 $X_{t,f}$: is forecast uncertain loading condition at time t. $P_r(SM|E_i, X_{t,f})$: Probability of the stability margin for ith contingency and forecast uncertain loading condition. $P_r(E_i)$: Probability of ith contingency

Sev (E_i , SM): Severity function which quantify the impact of the ith contingency with variation of stability margin. Equation (2) can be written in integral form as [10];

$$Risk(SM_{t,f}) = \sum_{i} P_{r}(E_{i}) \left[\int_{-\infty}^{\infty} P_{r}(SM | E_{i}, X_{t,f}) \times Sev(E_{i}, SM) dSM \right]$$
(3)

3. THE LINEAR APPROXIMATION METHOD

Sensitivity based method of probabilistic contingency analysis was adopted to evaluate the linear approximation method because sensitivity techniques are quick and easy ways of computing any possible violations of operating limits. The linear approximation method requires the probability of voltage distribution, probability of contingency, and the severity function to evaluate the severity of the contingency.

3.1. Probability of Voltage Distribution

The probability of voltage distribution requires the standard deviation calculation from variance – covariance matrix (Cp) and the sensitivities of voltage with respect to active power (P) and reactive power (Q). These sensitivities are developed from the Jacobian matrix (J) of the basic load flow algorithm by simply inverting the Jacobian matrix. Equation (4) shows the Jacobian matrix (J) of Fast Decoupled Power Flow [12].

$$J = \begin{bmatrix} \frac{\partial P_2}{\partial \delta_2} & \cdots & \frac{\partial P_2}{\partial \delta_n} & & & \\ \vdots & \ddots & \vdots & & 0 & \\ \frac{\partial P_n}{\partial \delta_2} & \cdots & \frac{\partial P_n}{\partial \delta_n} & & & \\ & & & \frac{\partial Q_2}{\partial |V_2|} & \cdots & \frac{\partial Q_2}{\partial |V_n|} \\ 0 & & \vdots & \ddots & \vdots \\ & & & & \frac{\partial Q_n}{\partial |V_2|} & \cdots & \frac{\partial Q_n}{\partial |V_n|} \end{bmatrix}$$
(4)

The sensitivities of only stressed buses voltage with respect to load bus active power and reactive power are evaluated for the low voltage risk assessment. The sensitivities of the voltages are located at the particular row of J^{-1} . Hence, we evaluate that particular row for the stressed buses.

After screening all the buses, the stressed voltage buses are identified and their particular row in the Jacobian matrix is inverted. Assume that the stressed voltage bus is ith bus, the sensitivity vector (Sp) for the probability calculation will be;

$$[S_p] = \begin{bmatrix} \frac{\delta V_i}{\delta Q_2} \\ \vdots \\ \frac{\delta V_i}{\delta Q_n} \end{bmatrix}$$
(5)

The variance – covariance matrix (C_p) can be obtained from historical data for real control room calculations. It is assumed that non – diagonal elements are zero as there is no dependence between loads on different buses and the diagonal elements are square of the product of the load and load standard deviation. The variance - covariance matrix is given as;

$$\begin{bmatrix} C_p \end{bmatrix} = \begin{bmatrix} \sigma Q_1^2 & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & \sigma Q_{nl}^2 \end{bmatrix}$$
(6)

The sensitivity of V_i and the variance – covariance matrix (C_p) of the uncertain operating parameters are required to evaluate the variance of V_i . The variance of V_i will be;

$$\gamma V_{i} = \begin{bmatrix} \frac{\partial V_{i}}{\partial Q_{i}} & \cdots & \frac{\partial V_{i}}{\partial Q_{n}} \end{bmatrix} \times \begin{bmatrix} \sigma Q_{1}^{2} & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & \sigma Q_{nl}^{2} \end{bmatrix} \begin{bmatrix} \frac{\partial V_{i}}{\partial Q_{i}} \\ \vdots \\ \frac{\partial V_{i}}{\partial Q_{n}} \end{bmatrix}$$
(7)

Hence the standard deviation σ will be;

$$\sigma V_i = \sqrt{\gamma V_i} \tag{8}$$

 V_i is assumed to be normally distributed and therefore, the probability distribution of V_i is

$$P_r(V_i) = \frac{1}{\sigma V_i \sqrt{2\pi}} e^{\frac{-(V_i - \mu V_i)^2}{2\sigma^2 V_i}}$$
(9)

Where: $P_r(V_i)$ is the probability distribution of V_i , σV_i is the standard deviation of V_i , and μV_i is the mean deviation of V_i

3.2 Probability of Contingency

The events of contingency (E_i) are modeled to be Poisson distributed since they are rare events. The probability of a certain contingency is the probability that the contingency occurs at least one time in next hour [10].

$$P_r E_i = \sum_{x=1}^{\infty} P_r(x) = 1 - P_r(x=0) = 1 - e^{-\lambda_i}$$
(10)

Where: λ_i is the occurrence rate of contingency per time interval and E_i is the *i*th contingency.

The occurrence rate of the contingency for a year can be obtained from the historical data and occurrence rate for an hour is by dividing the yearly rate by 8760.

3.3 Low Voltage Severity Function

Severity function (Sev(x)) is introduced to quantitatively evaluate the severity of the network condition in terms of performance indicator [6, 13]. Continuous severity function is selected because it measures the extent of the violation and it can be easily composed. The severity of the contingencies is measured in terms of voltage drop. It evaluates to 1.0 for each bus at the deterministic limits (0.95 p.u.) and increases linearly as voltage magnitude fall below limits as illustrated in Figure 1

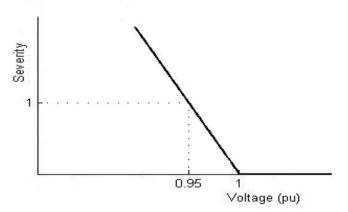


Figure 1: Continuous severity functions for low voltage [13].

3.4 Risk Evaluation

In order to evaluate the risk of low voltage, equation (2) is modified as follows [10]:

$$Risk(X_{t,f}) = \sum_{i} P_r(E_i) \sum_{i} \left[\int_{-\infty}^{\infty} P_r(V_i/E_i X_{t,f}) \times Sev(E_i V_i) dV_i \right]$$
(11)

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Where: $X_{t,f}$ is forecast uncertain loading conditions at time t. $P_r(V_i/E_iX_{t,f})$: is the probability of the stressed voltage of ith bus for ith contingency and forecast uncertain loading condition., $P_r(E_i)$: is the probability of ith contingency and $Sev(E_i, V_i)$: is the severity function which quantifies the impact of the ith contingency with variation of the bus voltage.

This modified equation (11) is used to evaluate the total low voltage risk for all probable contingencies. The probability of the stressed voltage and the severity function are multiplied together and the area under the resultant curve is evaluated. The area and the probability of contingency are multiplied to give the risk index of low voltage of a particular stressed bus.

In evaluating the risk indices, the following assumptions were made;

Assumptions:

- We invoke the assumption usually made for security assessment that a short term operating condition is given.
- The given operating condition has strong correlation with the condition in the near future so that we can predict the expectation of the future condition very well and that the variation of future condition is small and linear approximations are valid.
- The variation of the future condition away from its expectation, except for the contingences, is due to small parametric deviations.
- The steady state model of the power system is assumed and our interest is in the post contingency performance.
- The occurrences of contingencies are independent of each other and they are also independent of other system parametric deviation and the operating condition.
- The occurrence of contingency follows Poisson distribution.
- Parametric deviation follows a Multi Variant Normal (MVN) distribution around their expected values, and the distribution of load interruption voltages is normal.

4. MATERIALS

MATLAB software [14] was the tool used in achieving the solution of the load flow problem of the proposed model. The simulation model of Nigerian 330kV 41-bus network was used to demonstrate the proposed model. Figure 2 shows the single line diagram of the Nigerian 330kV 41-bus network while the network parameters: generator data, load data, and line data are shown in the appendix.

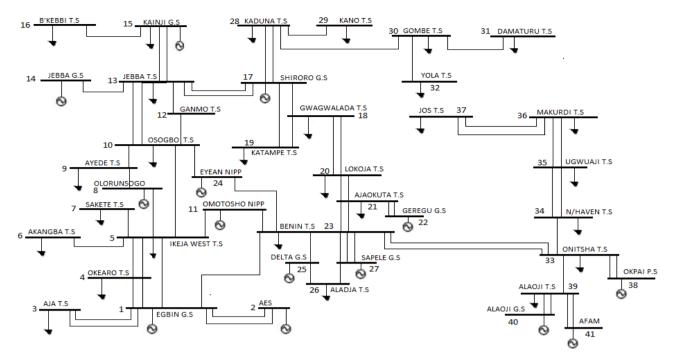


Figure 2: Single line diagram of the Nigerian 330kV 41-bus Transmission grid [15].

5. IMPLEMENTATION

Three contingencies were randomly simulated, contingency one on line 23-33, contingency two on line 1-5, and contingency three on line 30-31. The simulations of contingencies were carried-out assuming different yearly rates of occurrence. The assumed yearly rates of occurrence are 8, 12, 15, 20, and 25.

6. RESULTS

The results of voltage magnitude and risk indices obtained at various yearly rate of occurrence after simulating the contingencies are shown in Table 1, Table 2, and Table 3 respectively.

7. RESULT DISCUSSION

The results indicate that as the rate of occurrence increases, the risk indices increase. It shows that contingencies with high rate of occurrence pose more risk to the system than those that rarely occur. In comparison with Nigerian power system where contingencies are frequent and no longer rare, it implies that Nigerian power system is operating under highly risky conditions.

Therefore, to operate Nigerian power system under healthy conditions, that is when setting operating boundaries to delineate between acceptable and unacceptable operating regions, the occurrence rate should be considered. The results equally show that, contingencies with high rate of occurrence with little impact possess higher or equivalent risk to contingencies with great impact, which rarely occur. Therefore, system operator, technician, and engineer should quickly identify, investigate, and proffer solution to them in order to alleviate their effects on the network. In addition, it helps in deciding on whether to leave system facilities redundant due to the most sever contingency or fully utilize the facilities in power delivery.

	0	0		0		
Due Ne	Valtara (mu)	Risk indices at various yearly rate of occu				9
Bus No	Voltage (pu)	8	12	15	20	25
16	0.777	0.0016	0.0024	0.0031	0.0041	0.0051
28	0.933	0.0005	0.0007	0.0009	0.0012	0.0015
29	0.889	0.0008	0.0012	0.0015	0.0020	0.0025
30	0.933	0.0005	0.0007	0.0009	0.0012	0.0015
31	0.899	0.0007	0.0011	0.0014	0.0018	0.0023
	Total	0.0041	0.0061	0.0078	0.0103	0.0129

Table 1: Voltage magnitude and risk indices of contingency one on line 23-33

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Bus No	Valta an (mu)		Risk indices at v	arious yearly ra	us yearly rate of occurrence	
	Voltage (pu)	8	12	15	20	25
16	0.790	0.0008	0.0012	0.0015	0.0019	0.0024
29	0.946	0.0002	0.0003	0.0004	0.0005	0.0006
31	0.940	0.0002	0.0003	0.0004	0.0006	0.0007
Total		0.0012	0.0018	0.0023	0.0030	0.0037

Table 2: Voltage magnitude and risk indices of contingency two on line 1-5

Table 3: Voltage magnitude and risk indices of contingency three on line 30-31

	U	0		0,		
Bus No	Valtaga (nu)	Risk indices at various yearly rate of occurrence				•
	Voltage (pu)	8	12	15	20	25
16	0.798	0.0018	0.0028	0.0034	0.0046	0.0057
28	0.923	0.0007	0.0010	0.0013	0.0017	0.0022
29	0.902	0.0009	0.0013	0.0017	0.0022	0.0028
30	0.923	0.0007	0.0010	0.0013	0.0017	0.0022
31	0.923	0.0007	0.0010	0.0013	0.0017	0.0022
	Total	0.0048	0.0071	0.0090	0.0119	0.0151

8. CONCLUSION

Risk is decomposable and can be decomposed by perverting the conditions that make the network risky. Such conditions include contingencies with high rate of occurrence with little impact as well as contingencies that rarely occur with great impact. Hence, to operate the power system in healthy conditions in risk based security assessment, these risky scenarios have to be prevented. Therefore, adopting the risk based security assessment methods in Nigeria will help to alleviate the epileptic nature of the power system and improve power delivery to consumers because this method will help system operators, engineers, and technicians to quickly identify, investigate and proffer solution to risky scenarios.

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10. APPENDIX

Table 4.Generator bus data of Nigerian 330kV 41Bus Network

Bus No.	Bus Name	P (MW)	Q (MVar)
1	Egbin	0	0
2	AES	520	-18.578
8	Olorunsogo	525.6	-79.183
11	Omotosho	305.9	-75.119
14	Jebba G.S	80.0	-145.997
15	Kainji G.S	200.0	145.833
17	Shiroro G.S	108.0	70.513
22	Geregu G.S	243.0	-96.075
24	Eyean	343.0	-213.429
25	Delta G.S	503.0	-109.474
27	Sapele G.S	153.0	-94.814
38	Okpai G.S	248.0	-52.732
40	Alaoji G.S	148.0	37.930
41	Afam	508.0	136.981
	<u> </u>	E 4 4 7	

Source: [16]

Table 5.Load Bus Data of Nigerian 330kV 41-Bus
Network

Bus No.	Bus Name	P (MW)	Q (MVar)
3	Aja T.S	120.0	161.5
4	Okearo T.S	130.0	186.0
5	Ikeja West T.S	698.5	338.1
6	Akangba T.S	89.8	26.7
7	Sakete T.S	55.0	15.0
9	Ayede T.S	156.0	61.5
10	Osogbo T.S	16.8	114.5
12	Ganmo T.S	30.8	24.5
13	Jebba T.S	117.4	63.5
16	B'Kebbi T.S	276.0	224.5
18	Gwagwalada T.S	26.0	94.5
19	Katampe T.S	56.0	94.5
20	Lokoja T.S	26.0	14.5
21	Ajaokuta T.S	16.0	4.5
23	Benin T.S	134.0	46.5
26	Aladja T.S	14.0	46.5
28	Kaduna T.S	286.0	114.5
29	Kano T.S	305.0	49.0
30	Gombe T.S	196.0	164.5

Bus No.	Bus Name	P (MW)	Q (MVar)		
31	Damaturu T.S	156.0	85.5		
32	Yola T.S	85.0	26.5		
33	Onitsha T.S	326.0	114.5		
34	New Haven T.S	154.0	64.5		
35	Ugwuaji T.S	86.0	34.5		
36	Makudi T.S	39.0	12.5		
37	Jos T.S	90.0	140.5		
39	Alaoji T.S	414.2	330.5		
Source: [16]					

Table 6.Line Data of Nigerian 330KV 41Bus Network

		-		Bus Networ
From	То	R (pu)	X (pu)	½ B (pu)
1	2	0.0011	0.0220	0.178
1	2	0.0011	0.0220	0.178
1	3	0.0005	0.0043	0.053
1	3	0.0005	0.0043	0.053
1	4	0.0006	0.0055	0.068
1	4	0.0006	0.0055	0.068
1	5	0.0006	0.0055	0.068
4	5	0.0006	0.0055	0.068
4	5	0.0006	0.0055	0.068
5	6	0.0006	0.0047	0.070
5	6	0.0006	0.0047	0.070
5	7	0.0025	0.0213	0.266
5	8	0.0028	0.0234	0.292
5	10	0.0090	0.0760	0.949
5	11	0.0028	0.0234	0.292
8	9	0.0021	0.0182	0.228
9	10	0.0041	0.0349	0.437
10	12	0.0017	0.0143	0.178
10	13	0.0056	0.0477	0.596
10	13	0.0056	0.0477	0.596
12	13	0.0039	0.0133	0.418
13	14	0.0003	0.0022	0.033
13	14	0.0003	0.0022	0.033
13	15	0.0029	0.0246	0.308
13	15	0.0029	0.0246	0.308
15	16	0.0111	0.0942	1.177
17	13	0.0087	0.0742	0.927
17	13	0.0087	0.0742	0.927
18	17	0.0053	0.0406	0.606
19	17	0.0079	0.0607	0.902
19	18	0.0026	0.0200	0.299
20	18	0.0063	0.0486	0.725
20	18	0.0063	0.0486	0.725
20	21	0.0017	0.0132	0.197
20	21	0.0017	0.0132	0.197
21	22	0.0001	0.0005	0.006
21	22	0.0001	0.0005	0.006
21	23	0.0071	0.0543	0.807
21	23	0.0071	0.0543	0.807

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From	То	R (pu)	X (pu)	½ B (pu)
23	1	0.0072	0.0608	0.759
23	24	0.0009	0.0076	0.095
23	11	0.0018	0.0155	0.194
24	10	0.0089	0.0762	0.953
25	23	0.0015	0.0125	0.156
25	26	0.0011	0.0097	0.122
26	27	0.0023	0.0191	0.239
27	23	0.0018	0.0139	0.207
27	23	0.0018	0.0139	0.207
27	23	0.0018	0.0139	0.207
28	17	0.0034	0.0292	0.365
28	17	0.0034	0.0292	0.365
28	29	0.0082	0.0699	0.873
28	30	0.0085	0.0711	0.889
30	31	0.0064	0.0547	0.684
30	32	0.0086	0.0729	0.911
33	23	0.0049	0.0416	0.520
28 30 30	30 31 32	0.0085 0.0064 0.0086	0.0711 0.0547 0.0729	0.889 0.684 0.911

From	То	R (pu)	X (pu)	½ B (pu)	
33	23	0.0049	0.0416	0.520	
33	34	0.0034	0.0292	0.365	
34	35	0.0003	0.0019	0.029	
34	35	0.0003	0.0019	0.029	
35	36	0.0017	0.0132	0.197	
35	36	0.0017	0.0132	0.197	
36	37	0.0103	0.0796	1.187	
36	37	0.0103	0.0796	1.187	
38	33	0.0022	0.0167	0.248	
38	33	0.0022	0.0167	0.248	
39	33	0.0049	0.0419	0.524	
40	39	0.0021	0.0182	0.228	
40	39	0.0021	0.0182	0.228	
41	39	0.0009	0.0069	0.103	
41	39	0.0009	0.0069	0.103	
Source [16]					