



MEAN OF MEDIAN ABSOLUTE DERIVATION TECHNIQUE FOR SPECKLE NOISE VARIANCE ESTIMATION IN COMPUTERISED TOMOGRAPHY IMAGES

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ABSTRACT

The accurate estimation of noise variance in an image is the first important stage in image filtering using adaptive filters. In this paper, a new technique for the estimation of speckle noise present in Computerised Tomography (CT) lung image was developed. The development of mean of median absolute derivation technique based on the estimated mean of speckle noise present in CT images is presented. From the result of the simulations, the new technique gave a reasonably accurate estimate of variance of speckle noise present in CT Images. Ten samples of 85x73 CT images corrupted by speckle noise level ranging from 10% to 30% were used as test images. Also, the new technique gave the lowest average speckle noise variance estimation error of 2.53% compared to 12.53% for the Median of Median Absolute Derivative Technique, 18.18% for the Transfer function technique and 37.14% for the Mode of Variance Technique. The simulation software used in the paper is Matrix Laboratory (MATLAB2012).

Keywords: Speckle Noise, CT Image, Adaptive Filter, Variance Estimation, Statistics

1. INTRODUCTION

A CT image is a medical image captured using Computerised Tomography machine. The predominant noise type present in CT images is speckle noise [1]. Speckle noise is a form of multiplicative noise that occurs due to constructive and destructive interference of wave during capturing. The accurate estimation of variance of noise present in a noisy CT image makes suitable filtering possible [2]. The value of noise variance obtained during estimation determines the extent to which the adaptive filter is tuned to achieve good noise suppression. Adaptive filters use the estimated noise variance as an input to determine the extent to vary filter centre-pixel weight or the window size to ensure better noise suppression [2, 3]. The priori knowledge of the type of noise present in a noisy image helps in the accuracy of the estimation [5]. The accuracy of the noise variance estimation technique used to estimate the variance of noise present in a noisy image determines the accuracy with which adaptive filters are tuned for effective noise suppression [6]. For effective performance, modern filters are tuned based on the level of the noise present in the noisy image. The estimation of the variance of multiplicative noise

present in a noisy image is a very difficult task due to speckle decorrelation [4, 5]. When a noiseless image ($Y(m, n)$) is corrupted by speckle noise ($N(m, n)$), the noisy image ($X(m, n)$) is given by (1) [9].

$$X(m, n) = Y(m, n)N(m, n) \quad (1)$$

The noise present in (1) is converted to additive noise as shown in (2) using logarithm transform [7, 8].

$$\log_e X(m, n) = \log_e Y(m, n) + \log_e N(m, n) \quad (2)$$

The logarithmic transformation is used to transform speckle noise from multiplicative noise to additive noise. For non-speckle noises, other transform techniques such as Ascombe transform (for transforming Poisson noise to additive noise) and Ascombe-like transform (for transforming a combined additive and Poisson-like noise) exist [11]. The logarithmic transformation is applied to speckle noise so that linear filtering is used to suppress noise in the noisy image. When a noisy image is filtered using linear filter, the expression for the logarithm of approximate speckle noise approximate image edge and residual image surface is computed using (3) where $h(m, n)$ is the linear filter kernel.

$$\log_e W(m, n) = \log_e X(m, n) - h(m, n) * \log_e X(m, n) \quad (3)$$

The parameter, $W(m,n)$ in (3) is made up of the approximate speckle noise and approximate image edges and residual image surface. The variance of speckle noise present in the noisy image is estimated from (3) using speckle noise variance estimation techniques. For more accurate noise variance estimation, nonlinear filter like median filter is used for filtering because it preserves the edge of the filtered image [12]. When an edge preserving filter is used for filtering, the parameter, $W(m,n)$ includes the approximate speckle noise, residual image edge and residual image surface.

In this work, a Mean of Median Absolute Derivation Technique for estimating the variable of speckle noise present in an image is developed. The technique uses the statistical mean of noise present in an image to estimate the variance of noise present in CT images and other images with uniform intensity.

Many researchers have worked on the multiplicative noise variance estimation techniques. In [2], data masking using histogram technique was used. It was shown that the noise variance is the square of the standard deviation from the histogram. In [13], a Median of Median Absolute Derivation technique was developed. Transfer function based technique was developed in [14]. Local mean and local standard deviation of noisy image was used in noise variance estimation in [15]. In [16], a Robust Median Estimator technique was used. Principal component analysis technique was used to estimate the noise variance in [17]. In [18], statistical mode of noise present in an image was used to estimate the noise variance and median filter was used as a pre-estimation filter since it preserves image edge. In [19], the mode of local variance of the noise present in an image was used to estimate the noise.

However, in this paper, a Mean of Median Absolute Derivation technique for noise variance estimation is developed. Both the Mean of Median Absolute Derivation technique and Median of Median Absolute Derivation technique used median filter for filtering. The two techniques differ since the new technique used statistical mean property of noise for variance estimation while Median of Median Absolute Derivation technique used statistical median of noise for noise variance estimation.

2. DEVELOPMENT OF MEAN OF MEDIAN ABSOLUTE DERIVATION TECHNIQUE

The noise variance estimation technique proposed in this work is the Mean of Median Absolute Derivation

Technique. The proposed technique utilizes the value of noise mean to estimate the speckle noise variance. Noise mean property is selected in this paper because it has established quadratic relationship with noise variance. However, the estimation of speckle noise variance is complicated since some pixels give output that are non-real numbers during initial processing stages of the noise variance estimation. This is because the pixels with zero values gives $-\infty$ after logarithm transformation and gives Not-a-Number (NaN) output when the operation in (3) is carried out. NaN is a numeric data type representing an undefined value. For that reason, images corrupted by speckle noise is corrected by adding the correction factor (β) to the corrupted image ($X(m,n)$) before transformation and (1) is modified as shown in (4).

$$\log_e(X(m,n) + \beta) = \log_e(Y(m,n)N(m,n) + \beta) \quad (4)$$

The parameter, β is a real number such that $\beta \leq 10^{-7}$. The value of β is made very negligible to avoid excessive change in pixel values.

For filtering in this paper, Median filter is used because it preserves the edge of the image [12]. The expression in (5) was obtained when the transformed image in (4) was filtered using median filter and subtracted from (4) which is a modification of work done by [13]. The parameter, $\log_e W(m,n)$ is the logarithm of combined approximate speckle noise present in the noisy image, residual image edge and residual image surface due to error during filtering.

$$\log_e W(m,n) = \log_e(X(m,n) + \beta) - h_{MED}(\log_e(X(m,n) + \beta)) \quad (5)$$

The parameter h_{MED} is the median filter function. Convolution operation was omitted because the filtering in (5) is nonlinear filtering not linear filtering. The mean of the right hand side of (5) is obtained as given in (6) where M and N are the row and column length of the image respectively.

$$mean = \frac{1}{MN} \sum_{m=1}^M \sum_{n=1}^N abs(\log_e W(m,n)) \quad (6)$$

The Algorithm for Noise variance (δ_n^2) estimation technique is given in (7). The expression in (7) is obtained by modeling the relationship between the actual variance (σ_n^2) of speckle noise present in CT images and estimated noise mean computed in (6) using Quadratic Least Squares Regression Method. The Quadratic Least Squares Regression was used in this modeling because the relationship between variance and mean is quadratic relationship.

$$\delta_n^2 = 0.3907(mean + 1.3570)(mean - 0.1133) \quad (7)$$

The algorithm in (7) is obtained by plotting a scatter plot of the actual variance against the estimated mean for many CT images for noise variance ranging from 0% to 40% and drawing a quadratic curve of best fit. The expressing for the line of best fit is the algorithm in (7). The new technique works for other images but gives unique result when applied to CT images. The mean is chosen in this paper because it best represents the noise variance in the image. Based on observation during simulation, the estimation technique developed in this work is effective for speckle noise variance ranging from 10% (0.1) to 30% (0.3).

3. PERFORMANCE METRICS

The performance of an estimation technique depends on the performance of the preprocessing filter and the statistical quantity used. To effectively discuss the new technique, the Peak Signal to Noise Ratio (PSNR) and Mean Square Error (MSE) metrics of the preprocessing filter and the estimation error (ξ) of the developed technique are discussed.

3.1. PSNR and MSE Metrics

The PSNR of an image is the ratio of the maximum power of the image to the maximum power of the noise distorting the image [20]. For a normalized image, the PSNR can be rewritten as shown in (8). A normalized image is an image in which each pixel value has been divided by 255.

$$PSNR = 10 \log_{10} \left(\frac{255^2}{MSE} \right) \tag{8}$$

The PSNR is measured in decibel. The PSNR Gain is the PSNR of filtered image minus the PSNR of noisy image. On the other hand, MSE is the average of the squared intensity differences between the filtered image pixels and noiseless image.

$$MSE = \frac{1}{MN} \sum_{m=1}^M \sum_{n=1}^N [Y(m, n) - \bar{Y}(m, n)]^2 \tag{9}$$

The mean square error according to [21] is calculated using (9) where $Y(m, n)$ is the normalized noiseless image and $\bar{Y}(m, n)$ is the filtered normalized image.

3.2. Noise Estimation Metrics

The performances of the noise variance estimation techniques are quantified using estimation error (ξ) as shown in (10) [14].

$$\xi = \frac{abs(\sigma_n - \delta_n)}{\sigma_n} \times 100 \tag{10}$$

The parameter, σ_n is the standard deviation of the actual speckle noise present in the noisy image while δ_n is the estimated standard deviation of speckle noise present in the same image.

4. STEPS IN USING THE MODEL

The steps involved in the use of the proposed method in estimating that variance of speckle noise present in a noisy image are as follows:

1. Convert the noisy image to grayscale image and divide each pixel value by 255 to normalize the image.
2. Transform the normalized noisy image using logarithmic transformation.
3. Filter the transformed noisy image using a median filter.
4. Subtract the filtered image from the noisy image to leave approximate noise, residual image edge and residual image surfaces.
5. Compute the absolute values of the output in step 4.
6. Compute the mean of the output of step 5.
7. Compute the speckle noise variance by substituting the value of mean obtained in step 6 in (7).

5. RESULTS AND DISCUSSION

The performance of the developed technique in estimating the variance of speckle noise in images was compared with other estimation techniques using ten samples of 85x73 CT lung images corrupted by speckle noise of variance ranging from 10% (0.1) to 30% (0.3). Noise variance has no unit and is often measured in percentage (%) or fraction of total noisy image variance. The average estimated speckle noise variances obtained in the analysis using four techniques are shown in Table 1. The average speckle noise variance estimation errors calculated from Table 1 using (10) for the four techniques are as shown in Table 3.

The estimated speckle noise variances using the four techniques are shown in Table 1. From this table, it is seen that the noise variance estimated using the proposed technique is closest to the actual noise variance present in the image for all noise levels compared to other techniques. Also, it can be observed that the estimated noise for the proposed technique becomes more accurate as the actual noise variance present increases.

Based on Table 1, it is concluded that the proposed technique has best average speckle noise variance

estimation performance for all the noise variance range considered.

The large gap between the performance of the proposed technique and the performances of other techniques is because the proposed technique is

developed specially for CT images. CT images were used during the development of the technique to accommodate the inherent properties of images captured using CT machines such as high resolution and quantum noise properties [22].

Table 1: Average estimated speckle noise variance for the four noise estimation techniques

Noise Variance Estimation Technique	Actual Noise Variance (σ_n^2)				
	0.10	0.15	0.20	0.25	0.30
	Average Estimated noise variance (δ_n^2)				
Proposed Technique	0.0894	0.1457	0.1902	0.2412	0.3091
Mode of Local Variance [19]	0.0322	0.0537	0.0740	0.1133	0.1453
Transfer function based technique [14]	0.1070	0.1146	0.1248	0.1366	0.1565
Median of Median Absolute Derivative Technique [13]	0.0828	0.1182	0.1471	0.1892	0.2160

Table 2: Estimated speckle noise variance for proposed and Median of Median Absolute Derivative Technique for different images

Noise Variance Estimation Technique	Image	Actual Noise Variance (σ_n^2)				
		0.10	0.15	0.20	0.25	0.30
		Average Estimated noise variance (δ_n^2)				
Proposed Technique	Lena	0.0950	0.1498	0.2009	0.2571	0.3085
	Pepper	0.0964	0.1445	0.1901	0.2414	0.3112
	Cameraman	0.2112	0.2605	0.3030	0.3654	0.4597
Median of Median Absolute Derivative Technique [13]	Lena	0.1008	0.1686	0.2118	0.2467	0.2976
	Pepper	0.0998	0.2536	0.2018	0.2323	0.2880
	Cameraman	0.1308	0.1803	0.2052	0.2998	0.3767

Table 3: Average speckle noise estimation error for the four noise estimation techniques

Noise Variance Estimation Technique	Actual Noise Variance (σ_n^2)					Mean of Average Variance estimation Error (%)
	0.10	0.15	0.20	0.25	0.30	
	Average Variance Estimation Error (%)					
Proposed Technique	5.4537	1.4471	2.4756	1.7839	1.5037	2.5328
Mode of Local Variance [19]	43.2550	40.1948	39.1724	32.6828	30.3964	37.1403
Transfer function based technique [14]	3.4360	12.5929	21.0095	26.0919	27.7712	18.1803
Median of Median Absolute Derivative Technique [13]	9.0000	11.2457	14.2416	13.0005	15.1570	12.5289

The performance of any estimation technique depends on the properties of the image considered. This can be seen in Table 2 when the proposed technique and the Median of Median Absolute derivation Technique are applied to Lena, Cameraman and Pepper images. From Table 2, it is seen that the two techniques give the same result for Lena and Pepper images but the proposed technique gives worse result for Cameraman image.

The difference in performances among the four estimation techniques considered is clearly seen in Table 3. From Table 3, it is observed that the proposed technique has the lowest estimation error showing that it has the best estimation accuracy except for noise variance of 0.10 where

Transfer function technique was lower. This is because Transfer function technique was optimized for estimating noise variance ranging from 0.0 to 0.12. Looking at Table 3, it is observed that the estimation error of the proposed technique decreases as the variance of noise present increases for noise variance ranging from 0.10 to 0.15 and from 0.20 to 0.3 but for noise variance ranging from 0.15 to 0.20 the estimation error increases as the noise variance increases.

In this paper, 3X3 Median Filter kernel was used for preprocessing of a noisy image since it causes less blur and preserves the edges of the filtered image. Other simple filters that may be used for the same purpose are Averaging Filter and Binomial Filter (Optimized

Gaussian Filter). The decision to use Median Filter in this work is justified by considering Table 4 obtained from ten samples of 85X73 CT lung images.

Table 4 shows how the PSNR Gain for the filters varies with the variance of speckle noise present in noisy images. From Table.4, it is observed that Median filter gives the highest average PSNR Gain (3.6591dB) compared to Averaging filter (2.8479dB) and Binomial filter (3.0140dB).

From Table 4, it is observed that for all noise levels greater than 15%, Median filter gives the largest values of average PSNR Gain. However, for all noise levels less that 12%, the Median filter has the least

PSNR Gain among the three filters. The increase in average PSNR Gain with increase in the noise variance for Median filter is because median filter is nonlinear filter and is therefore the most stable filter among the three filters.

This shows that median filter gives the best result and therefore is the best filter for the preprocessing.

6. CT LUNG IMAGES USED IN THE PAPER

The CT images used in the paper are shown in Figure 1. The images are of sizes 85X73. Figure 2 shows the images when each is corrupted by speckle noise of 30% total variance.

Table 4: Average PSNR Gain for three preprocessing filters

Preprocessing Technique	Actual Noise Variance (σ_n^2)					Mean of Average PSNR Gain (dB)
	0.10	0.15	0.20	0.25	0.30	
	Average PSNR Gain (dB)					
3X3 Median Filter	3.0946	3.3119	3.7511	3.9574	4.1805	3.6591
3X3 Averaging Filter	3.2544	3.1302	3.0490	2.6649	2.1412	2.8479
3x3 Binomial Filter	3.6862	3.3507	3.1576	2.7134	2.1620	3.0140

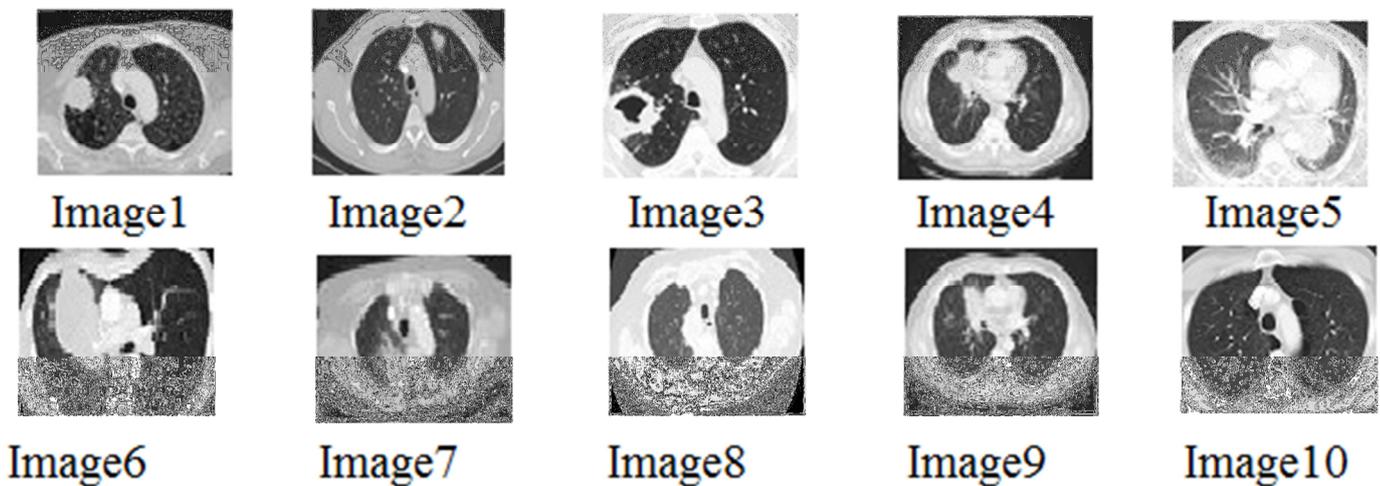


Figure 1: Noiseless images used in the paper

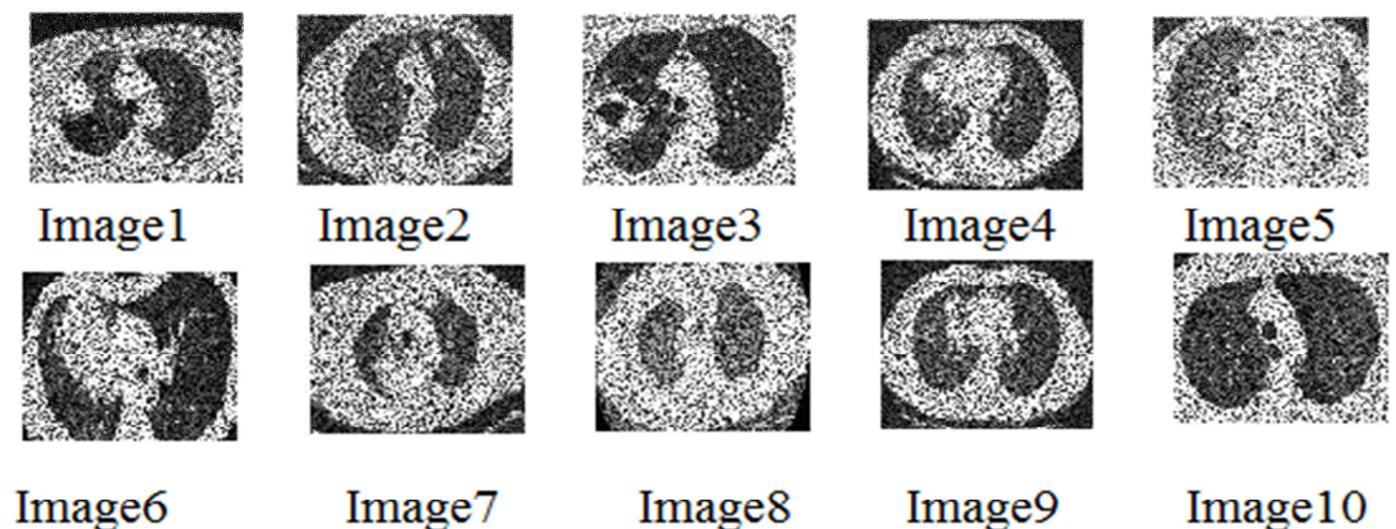


Figure 2: Unfiltered images corrupted by speckle noise of 30% total variance

7. CONCLUSION

In this paper, a speckle noise estimation technique based on the Mean of Median Absolute Derivation was developed. The developed technique estimates the speckle noise variance in a noisy CT image with an average estimation error as low as 2.5328% for noise variance ranging from 10% to 30%. The new technique out performs other techniques used to verify its performance including the *Median of Median Absolute Derivative Technique* which gave an error of 12.5289%. Median filter was selected for the preprocessing before noise estimation since it preserves image edges and performs better than Averaging filter and Binomial filter in suppressing speckle noise, especially at high noise level.

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