

Hotspot Advance Speed - Hotspot Size/Core-Hotspot distance Relation

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Abstract

We examined the evolution of extragalactic radio sources using the observed core-hotspot distance and hotspot size. Analysis indicates a fairly strong positive correlation in the ratio of core-hotspot distance to hotspot size between that of the approaching arm and the receding arm with a correlation coefficient of $r \sim 0.7$. Simple kinematic consideration enabled us to obtain an expression to constrain the advance speed of hotspots. In general, the average projected hotspot advance speed estimated for our sample ranges from $0.13 \leq \langle \beta \rangle \leq 0.40$

Keywords: *Galaxies – General; Galaxies – Active; Methods – Analytical; Methods – Data Analysis.*

1 INTRODUCTION

Active Galactic Nucleus (AGN) describes the nucleus of extragalactic radio sources (EGRSs) with very high luminosities believed to be produced through accretion of matter onto a central object possibly a super massive black hole. The activity of the central engine is often accompanied by highly-relativistic collimated jets/beams (e.g. Begelman et al. 1984) of plasma material formed and accelerated in the vicinity of the black hole (Blandford & Konigl 1979), which transport some of the accretion power to the lobes of EGRSs where they are thermalized in the hotspots (Scheuer 1974). A long debated issue is the speed (β) which these hotspots advance away from the AGN core, where β is the bulk advance speed of the hotspot in units of c , the speed of light.

Observational evidence in support of the jets in AGN being relativistic include (i) one-sided jet morphology, (ii) high brightness temperature of the AGN core determined with interferometers and from flux density variations (e.g. Kellermann & Pauliny-Toth, 1968; Kellermann & Pauliny-Toth, 1981; Kellermann et al. 2004; Lähteenmäki & Valtaoja (1999); Cohen et al. 2007), (iii) the asymmetry of the polarization of the

jet at the two opposite sides (the so-called Laing-Garrington effect, Garrington et al. 1988; Laing, 1988) and (iv) the observed apparent superluminal motion (e.g. Whitney 1971; Cohen et al. 1977; Jorstad et al. 2001; Kellermann et al. 2004; Piner et al. 2007).

In most high luminosity radio sources with one-sided kiloparsec scale jets, the observed parsec jets always points in the same direction as the kiloparsec jets (Pearson & Readhead, 1988; Wardle & Aaron, 1997), implying the persistence of relativistic motions in kiloparsec region of EGRS. Hardcastle et al. (1999) reported that relativistic beaming is needed to explain the observed relationship between core and jet prominence in their sample.

The advance speed of the hotspots/lobes for asymmetric radio sources can be estimated using the asymmetry parameters such as the arm-length ratio and apparent flux density ratio (e.g. Banhatti (1980); Best et al. 1995; Scheuer 1995, Ryś 2000), but this depends highly on the degree of asymmetry and the assumption that the observed asymmetry is entirely due to relativistic beaming. However, environmental and other intrinsic factors have been shown to be important in interpreting observed asymmetries in EGRSs (e.g. McCarthy et al. 1991; Wardle & Aaron 1997; Jeyakumar & Saikia, 2000; Jeyakumar et al. 2005; Onuchukwu & Ubachukwu, 2013). Another method for estimating hotspot advance speed is the synchrotron age estimates (Liu et al. 1992; Parma et al. 1999; Murgia et al. 1999; Schoenmakers et al. 2000; Jamrozy et al. 2005), but the uncertainty is large. The major source of uncertainty in estimating hotspot advance speed using synchrotron age estimates lies in the assumption of minimum-energy field in the estimation of the magnetic field (B), since synchrotron age (t_{syn}) estimate depends more on magnetic field than the radio spectrum break frequency ν_b as ($t_{syn} \propto B^{-1.5} \nu_b^{-0.5}$ (see Longair (1981); De Young (2002)) uncertainty in the value of magnetic field makes it difficult to derive the source age.

In this article, we wish to estimate the projected advance speed of hotspot using the observed core-hotspot distance and hotspot size. In this method we will assume constant advance speed of hotspot from the core and constant aspect ratio. The use of core-hotspot distance rather than core-lobe distance is due to the fact that hotspots are more compact and brighter thus angular extension should be more clearly defined. Gopal-Krisna & Wiita (2004) noted that the main thrust of the collimated energy supply from the galactic nucleus is focused through the jets into the hot-spots, thus any relativistic motion is more likely to be associated

with them (Longair et al. 1973; Blandford & Rees, 1974; Scheuer, 1974), and not with the extended lobes.

In Section 2, we obtain an analytical expression that relates the hotspot expansion to hotspot size and core-hotspot distance, in Section 3, we carry out the analysis and conclude in Section in 4.

2 THEORY OF RELATIONSHIP

According to the standard beam model of radio-loud AGNs, it is believed that a fraction of accretion material forms an outflow (beam of relativistic plasma) along the rotational axis of the black hole (Blandford & Znajek, 1976; Mundell et al. 2003). These beams transport the bulk kinetic energy from the central engine to kiloparsec regions $\sim 100 - 1000 \text{ kpc}$ away from the central engine where they terminate and are thermalized at the hotspots (Blandford & Rees, 1974). Scheuer (1974) noted that the shocked relativistic plasma should expand sideways due to the interactions between the ambient intra cluster medium and the AGN jet. Assuming twin ejection of materials on the opposite sides of the central engine of AGN, and a simple kinematic model, then, in the frame of the source, the distance of the plasma element from the core (D_0) can be described by

$$D_0 = \beta ct_0 \quad (1)$$

where β is the bulk advance speed of the jets in units of c , the speed of light, t_0 is the time taken for the plasma element to traverse the distance (D_0). Putting into consideration time delay effects and orientation effect, the observed time in the AGN rest frame is related to time in the observer's frame by, for the approaching arm (see Gopal-Krishna & Wiita, 2004)

$$t_a = \gamma(1 - \beta \cos \theta)t_0, \quad (2)$$

and for the receding arm,

$$t_r = \gamma(1 + \beta \cos \theta)t_0, \quad (3)$$

where θ is the angle to the line of sight of a distant observer, γ is the Lorentz factor related to the bulk speed by $\gamma = \frac{1}{\sqrt{1-\beta^2}}$. Thus, the time (t) taken to traverse a given distance in the frame of the plasma element in terms of the observed distances, for the approaching arm (D_a) can be written as

$$t_a = \frac{D_a}{\beta c \sin \theta} \gamma (1 - \beta \cos \theta) (1 + z) \quad (4)$$

and for the receding arm D_r we have

$$t_r = \frac{D_r}{\beta c \sin \theta} \gamma (1 + \beta \cos \theta) (1 + z) \quad (5)$$

Here D is the projected core-hotspot distance, the subscripts a and r represent approaching and receding arm respectively. We have defined $D_0 = D \sin \theta$ (see Ubachukwu, 1998); the factor $(1 + z)$ is needed to transform the observed time to the time in the frame of our galaxy (see Blandford & Konigl, 1979; Homan et al. 2009). Thus, the ratio of the time to reach an observed distance can be written as

$$\frac{t_r}{t_a} = \frac{D_r(1 + \beta \cos \theta)}{D_a(1 - \beta \cos \theta)} \quad (6)$$

When the plasma is thermalized, they expand sideways. Following KÖrding & Falcke (2004), the expansion speed will depend on the speed of sound (β_s) in the plasma. Now let R_a be the observed size of the approaching side hotspot and R_r the observed size of the receding side hotspot. The time (t_R) to reach an observed size for the approaching arm may be written (assuming an isotropic medium) as

$$t_{aR} = \frac{R_a}{\beta_s} \quad (7)$$

and for the receding arm we have

$$t_{rR} = \frac{R_r}{\beta_s} \quad (8)$$

Assuming that the time to reach an observed size (t_R) is related to the time (t) to reach an observed core-hotspot distance by $t_R \propto t^y$ with $y = 1$ for simplicity (other values of y are possible), then, from the above equations, we have

$$\frac{D_r R_a}{D_a R_r} = \frac{(1 + \beta \cos \theta)}{(1 - \beta \cos \theta)} = \frac{1 - \bar{\beta}}{1 + \bar{\beta}} \quad (9)$$

where $\bar{\beta} = \beta \cos \theta$ is the projected advance speed of the hotspot on the plane of the sky. Kawakatu et al. (2008), had shown that there is a correlation between hotspot size and core-hotspot distance.

We note that the assumption for $y = 1$, may not be entirely true for different regimes of core-hotspot distance and expansion mode due to

different modes of interactions expected between the jet plasma and the ambient medium in the host galaxy (e.g. Saikia et al. 1995; O’Dea 1998; Dallacasa et al. 2002). For sources with core-hotspot distance less than 1 kpc and for those with core-hotspot distance greater than 1 kpc, Kawakatu et al. (2008) obtained different slopes to the linear fits of the core-hotspot distance/hotspot size relation. Furthermore, the power-law index for the evolution of the hotspot size may change at transition between interstellar medium and intergalactic medium (e.g. Jeyakumar & Saikia 2000; Perucho & Marti, 2002). But for constant jet advance speed and constant aspect ratio usually assumed in self-similar model treatment of extragalactic radio sources (Begelman & Cioffi, 1989; Loken et al. 1992; Cioffi & Blondin, 1992), the assumption that the time (t_R) to reach a given hotspot size correlates with the time (t) to reach a given core-hotspot distance with $y = 1$ seems reasonable. Equation (8) can be inverted to give

$$\bar{\beta} = \frac{1-b}{1+b} \quad (10)$$

where $b = \frac{D_r R_a}{D_a R_r}$ and gives us an expression to constrain the projected advance speed of hotspots for sources with observed core-hotspot distance and hotspot size. In general, a linear regression fit to equation (8) in the form

$$\log\left(\frac{D_r}{R_r}\right) = \log\left(\frac{D_a}{R_a}\right) + \log\left(\frac{1-\bar{\beta}}{1+\bar{\beta}}\right) \quad (11)$$

will enable us estimate the average projected bulk expansion speed $\bar{\beta}$. Also, the $\log\left(\frac{D_r}{R_r}\right) - \log\left(\frac{D_a}{R_a}\right)$ plot is theoretically expected to yield a slope of 1. This can be tested using a well-defined source sample. The logarithmic form of the relationship was chosen due to the expected wide spread in the observed core-hotspot distance and hotspot size

3 DATA ANALYSIS/RESULT

The analyses were based on a sample of extragalactic radio sources obtained from Kawakatu et al. (2008) which they culled from literature. According to Kawakatu et al. (2008), to minimize the difference in estimation of physical quantities between approaching hotspot and counter hotspot, they selected mainly sources with relatively symmetric lobes. For our analysis, we selected sources with observed information on jet and counter jet core-hotspot distance and hotspot size. We

excluded 3 sources (1005+070, 0255+460 and 1314+453) with core-hotspot distance and hotspot size exactly the same for both arms, these sources will give a ratio of 1, and thus not suitable for our expression in estimating projected hotspot advance speed. The final sample consists of 98 FR II sources. These sources depending on the projected linear size may be further classified as Compact Symmetric Objects (CSO), Medium-size Symmetric Objects (MSO), and Compact Steep Spectrum Sources (CSS). In Kawakatu et al. (2008), there was no identification of the approaching arm and the receding arm. Assuming simple relativistic beaming scenario (e.g. Ryle & Longair 1967; Gopal-Krishna & Wiita 2004), the longer arm is assumed to be the approaching arm.

In relativistic beaming scenario and twin beam model of AGN, for plasma elements ejected from the core and observed at the same time, the receding lobe will be at a shorter distance from the core and smaller in size than the approaching lobe. Thus, we expect a positive correlation in the ratio of core-hotspot distance to hotspot size between that of the approaching arm and receding arm. The correlation coefficient result is strong for our sample with $r \sim 0.7$ with $p = 3.4 \times 10^{-7}$ (where p is the probability of getting the given value of r by chance. Using equation (9), the average projected hotspot advance speed estimated for our sample is $\langle \bar{\beta} \rangle = 0.3 \pm 0.2$, with the distribution plot of the estimated projected speed for each source shown in figure 1. Figure 2 shows the $\log\left(\frac{D_r}{R_r}\right) - \log\left(\frac{D_a}{R_a}\right)$ plot.

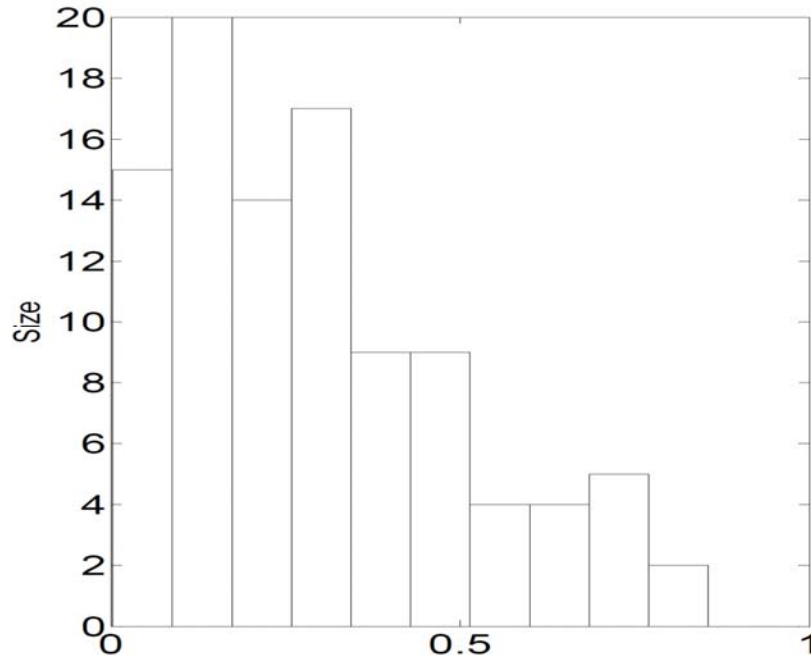


Fig 1 Histogram Plot of The Estimate Hotspot Advance Speed ($\beta \cos \theta$) for Each Source in The Sample.

If the sources were sub-divided based on core-hotspot distance (see Kawakatu et al. 2008) into CSO (with $D \leq 1 \text{ kpc}$), MSO (with $1 \leq D \leq 10 \text{ kpc}$) and large size FR II radio sources (with $D \geq 10 \text{ kpc}$), the average estimated projected hotspot advance speed is $\langle \bar{\beta} \rangle = 0.3 \pm 0.2, 0.4 \pm 0.1$ and 0.3 ± 0.1 for the large size FR II, MSO and CSO sources respectively. A linear regression fit to the $\log\left(\frac{D_r}{R_r}\right) - \log\left(\frac{D_a}{R_a}\right)$ plot (equation (11) gives: $\log\left(\frac{D_r}{R_r}\right) = (0.9 \pm 0.2) \log\left(\frac{D_a}{R_a}\right) - (0.11 \pm 0.03)$ this gives a mean projected advance speed of $\langle \bar{\beta} \rangle = 0.13 \pm 0.03$. The slope of the regression fit to equation (11) agrees well with the theoretical value, indicating that our assumption is plausible.

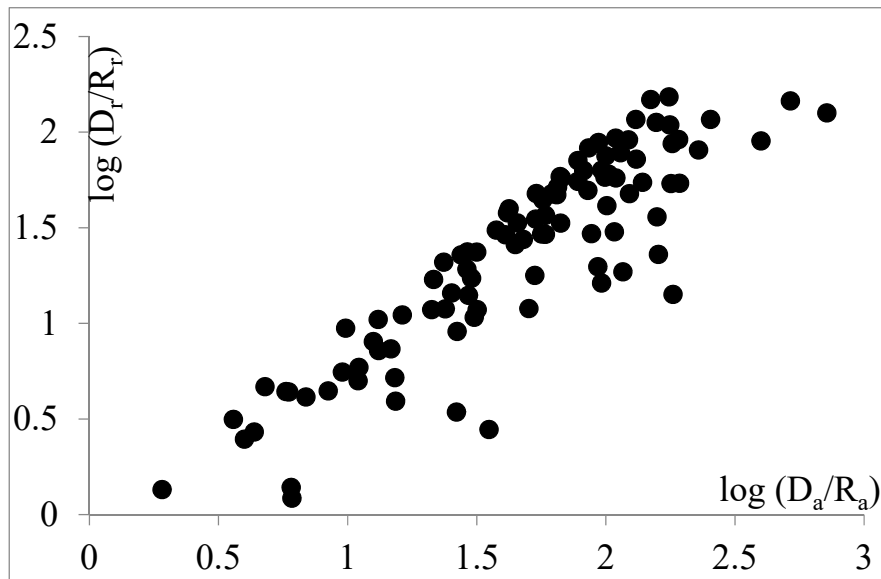


Fig 2. Plot of $\log\left(\frac{D_r}{R_r}\right)$ against $\log\left(\frac{D_a}{R_a}\right)$ For The Sources In Our Sample

4 DISCUSSION AND CONCLUSION

We have investigated a simple consequence of kinematic evolution of hotspot size and core-hotspot distance. We also used it to obtain an estimate for the projected hotspot advance speed of $0.1 \leq \langle \bar{\beta} \rangle \leq 0.4$ for a sample of radio sources. There are several sources of uncertainties in the estimation of the projected hotspot advance speed using the observed hotspot size and core-hotspot distance of radio sources. According to Kawakatu et al (2008), these include (i) Hotspots sizes – the sizes of larger hotspots may be underestimated due to a lack of sensitivity for diffuse emission. (ii) Uncertainties in the angular resolution of the angular size of radio source may affect the estimation of the hotspot size. The higher the angular size resolution, the finer the details revealed and this might lead to underestimation of the hotspot sizes. (iii) Projection effect - The estimated size of the hotspot may not be intrinsic, but the size projected onto the celestial plane.

The estimated speed within the limits of error, supports the assumption of constant advance speed of hotspots, though there seems to be a mild increase at the CSO – MSO phase with $\langle \bar{\beta} \rangle$ from 0.3 – 0.4 and mild deceleration at the MSO – large size FR II with $\langle \bar{\beta} \rangle$ from 0.4 – 0.3

phase. The CSO - MSO phase seemingly acceleration is expected for a power-law ambient density profile that scales approximately as King (1972) profile with $\rho_D \sim \rho_0 \left(\frac{D}{D_0}\right)^{-\epsilon}$, where ρ_0 is the central density distribution of the source environment, and here D_0 is the assumed inner radius and ϵ index of decline. Thus, for $D \geq D_0$ there will be less interaction with environment and less obstruction to advance motion away from the core, leading to higher speeds. From the observed values of advance speed shown in Kawakatu et al. (2008), the average advance speed in CSO - MSO – large size FR II phases are $\beta \sim 0.13$; 0.15 and 0.05 respectively for CSOs, MSOs and large size FR IIs. These values follow similar trend (though of lower values) to the average projected advance speed we estimated. The assumption of simple relation between the time for hotspot growth and distance away from the core may have been responsible for the discrepancies in the two results. Our results may be considered the upper limit to the expansion speed while Kawakatu et al. (2008) result may reflect the lower limit.

Observations of the synchrotron radiation spectrum of extragalactic radio sources (assuming equipartition magnetic field) have led to the estimation of the advance speed of the hotspots for most powerful extragalactic radio sources as $\beta \sim 0.2 - 0.3$ (Myers & Spangler 1985; Liu et al. 1992). Using the prevalence of long lobe of radio sources, Longair & Riley (1979) estimated that the expansion speed of the lobes in general cannot be more than $\beta \sim 0.25$. Furthermore, Best et al. (1995) showed that a hotspot speed in the range $\beta \sim 0.2 - 0.3$ would be required to reproduce the arm-length ratio distribution for the 3CRR sample. More recently, Stanghellini et al. (2009) in their study of three compact radio sources obtained hotspot speed which lies in the range $\beta \sim 0.2 - 0.4$. Orienti & Dallacasa (2010) reported a mean apparent expansion speed in intrinsically compact radio sources of $\beta \sim (0.39 \pm 0.18)$ which is in agreement with the values obtained by Polatidis & Conway (2003) who studied a dozen of the most compact radio sources. These results are in general, consistent with the values obtained in this paper.

On the other hand, Scheuer (1995) obtained a somewhat lower value $\beta \leq 0.15$, with most probable speed value of $\beta \sim 0.03 - 0.02$ which may be taken as the lobe speed (a rapid backflow is expected if the jet material is much less dense than the ambient plasma); such strong backflows are clearly observed in many numerical simulations of jet propagation (see Norman 1996; Hooda & Witt 1998). Furthermore, Arshakain & Longair

(2000) using the jet-sidedness ratio for a large sample of quasars and galaxies, obtained similar small values of hotspot advance speed of $\beta \sim 0.11 \pm 0.01$. However, in their analysis, they pointed out that intrinsic/and environmental effects also contribute to the observed asymmetries.

In conclusion, using the observed core-hotspot distance, hotspot size and assumption of constant hotspot advance speed/aspect ratio, we obtained an expression that helped us constrained projected hotspot advance speed of extragalactic radio sources.

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References

- Arshakian, T. G., & Longair, M.S., (2000). An asymmetric relativistic model for classical double radio source. *Monthly Notices of the Royal Astronomical Society (MNRAS)*, 311, 846
- Banhatti, D. G., (1980). Expansion Speeds in Extended Extragalactic Double Radio Sources from Angular Structure. *Astronomy & Astrophysics (A&A)*, 84, 112
- Begelman, M. C., & Cioffi, D. F. (1989). Overpressured cocoons in extragalactic radio sources. *Astrophysical Journal (ApJ)*, 345, L21
- Begelman, M. C., Blandford, R. D., & Rees, M. J. (1984). Theory of extragalactic radio sources . *Reviews of Modern Physics (Rev. Mod. Phys)*, 56, 255
- Best, P.N., Bailer, M.D., Longair M.S. & Riley, J.M., (1995). Radio Source Asymmetries And Unified Scheme. *Monthly Notices of the Royal Astronomical Society (MNRAS)*,, 275, 1171.
- Blandford R.D., & Konigl A., (1979). Relativistic jets as compact radio sources. *Astrophysical Journal (ApJ)*, 232, 34
- Blandford R.D., & Rees, M.J., (1974). A 'Twin-Exhaust' Model for Double Radio Sources. *Monthly Notices of the Royal Astronomical Society (MNRAS)*, 169, 395

- Blandford, R. D., & Znajek, R. L. (1977). Electromagnetic extraction of energy from Kerr black holes. *Monthly Notices of the Royal Astronomical Society (MNRAS)*, 179, 433-456
- Blondin, J. M., (1992). The evolution of cocoons surrounding light, extragalactic jets. *Astrophysical Journal (ApJ)*, 392, 458
- Cohen, M. H., et al. (1977). Radio sources with superluminal velocities. *Nature*, 268, 405
- Cohen, M. H., et al. (2007). Relativistic Beaming and the Intrinsic Properties of Extragalactic Radio Jets, *Astrophysical Journal (ApJ)*, 658, 232
- Dallacasa, D., et al. (2002). The B3-VLA CSS sample. II. VLBA images at 18 cm. *Astronomy & Astrophysics (A&A)*, 389, 126
- De Young, D.S. (2002). *The Physics of Extragalactic Radio Sources*. University of Chicago Press Limited. Chicago. pp557
- Garrington S.T., et al. (1988). A Systematic Asymmetry in the Polarization Properties of Double Radio Sources with one Jet. *Nature*, 331, 147
- Gopal-Krishna, & Wiita P.J., (2004). Asymmetries in Powerful Extragalactic Radiation Sources. arXiv:astrophysics-ph/040976]v2 1-27
- Hardcastle, M. J., et al. (1999). FR II radio galaxies with $z < 0.3$ - II. Beaming and unification,. *Monthly Notices of the Royal Astronomical Society (MNRAS)*, 304, 135
- Homan, D.C., et al. (2009). MOJAVE: Monitoring of Jets in Active Galactic Nuclei with VLBA Experiments. VII. Blazar Jet Acceleration. *Astrophysical Journal*, 706, 1253
- Hooda, J.S., & Wiita, P.J., (1998). Instabilities in Three-dimensional Simulations of Astrophysical Jets Crossing Tilted Interfaces. *Astrophysical Journal (ApJ)*, 493, 81.
- Jamrozy, M., et al. (2005). Ageing analysis of the giant radio galaxy J1343+3758. *Astronomy & Astrophysics (A&A)*, 433, 467

- Jeyakumar, S., & Saikia, D. J., (2000). Collimation of Extragalactic Radio Jets in Compact Steep-Spectrum and Larger Sources. *Monthly Notices of the Royal Astronomical Society (MNRAS)*, 311, 397J
- Jeyakumar, S., et al. (2005). Jet propagation and the asymmetries of CSS radio sources. *Astronomy & Astrophysics (A&A)*, 432, 823
- Jorstad, S. G., et al. (2001). Highly Variable Apparent Speed in the Quasar 3C 279. *Astrophysical Journal Supplement Series (ApJS)*, 134, 181
- Kawakatu, N., et al. (2008). The Fate of Young Radio Galaxies: Decelerations Inside Host Galaxies? *Astrophysical Journal (ApJ)*, 687, 141
- Kellerman, K.I., et al. (2004). Sub-Milliarcsecond Imaging of Quasars and Active Galactic Nuclei. III. Kinematics of Parsec-scale Radio Jets. *Astrophysical Journal (ApJ)*, 609, 539
- Kellermann, K. I., & Pauliny-Toth I. I. (1968). Variable Radio Sources. *Annual Review of Astronomy and Astrophysics (ARA&A)*, 6, 417
- Kellermann, K. I. & Pauliny-Toth I. I. K. (1981). Compact radio sources. *Annual Review of Astronomy and Astrophysics (ARA&A)*, 19, 373
- King, I. R., (1972). Density Data and Emission Measure for a Model of the Coma Cluster. *Astrophysical Journal (ApJ)*, 174, L123
- Körding, E., & Falcke, H., (2004). The Role of VLBI in Astrophysics, Astrometry and Geodesy. Proceedings of the NATO Advanced Study Institute, held September 17-29, 2001, in Bologna, Italy. Series II, Mathematics, Physics and Chemistry, Vol. 135. Edited by Franco Mantovani and Andrzej Kus. ISBN 1-4020-1875-4: ISBN 1-4020-2406-1 (e-book). Published by Kluwer Academic Publishers, Dordrecht, The Netherlands, 2004, p.107 (bibcode: [2004rvaa.conf..107K](https://ui.adsabs.org/abs/2004rvaa.conf..107K))
- Lähteenmäki, A., & Valtaoja, E., (1999). Total Flux Density Variations in Extragalactic Radio Sources. Iii. Doppler Boosting Factors, Lorentz Factors, And Viewing Angles For Active Galactic Nuclei. *Astrophysical Journal (ApJ)*, 521, 493

- Laing, R.A., (1988). The Sidedness of Jets and Depolarization in Powerful Extragalactic Radio Sources. *Nature*, 331, 149
- Liu, R., et al. (1992). Spectral Ageing an A Sample of 14 High-Luminosity Double Radio Sources. *Monthly Notices of the Royal Astronomical Society (MNRAS)*, 257, 545.
- Loken, C., et al. (1992). Ram-pressure confinement of a hypersonic jet. *Astrophysical Journal (ApJ)*, 392, 54
- Longair, M.S. & Ryle, M., (1979). Models of Extended Radio Sources. *Monthly Notices of the Royal Astronomical Society (MNRAS)*, 188, 625.
- Longair, M.S., (1981). High Energy Astrophysics, Cambridge University Press. Cambridge. pp412
- Longair, M.S., et al. (1973). Models of Extended Radio Sources. *Monthly Notices of the Royal Astronomical Society (MNRAS)*, (164) 243
- McCarthy, P. J., et al. (1991). Correlated Radio and Optical Asymmetries in Powerful Radio Sources. *Astrophysical Journal (ApJ)*, 371, 478.
- Mundell, C.G., et al. (2003). The Nuclear Regions of the Seyfert Galaxy NGC 4151: Parsec-Scale H I Absorption and a Remarkable Radio Jet, *Astrophysical Journal (ApJ)*, 583, 192
- Murgia, M., et al. (1999). Synchrotron spectra and ages of compact steep spectrum radio sources, *Astronomy & Astrophysics (A&A)*, 345, 769
- Myers, S. & Spangler, S., (1985). Synchrotron Aging in the Lobes of Luminous Radio Galaxies. *Astrophysical Journal (ApJ)*, 291, 52.
- Norman, M. L., (1996). Structure and Dynamics of the 3D Supersonic Jet, in Energy transport in radio galaxies and quasars. *Astronomical Society of the Pacific Conference Series, Volume 100, Proceedings of a workshop held in Tuscaloosa, Alabama, 19-23 September 1995, San Francisco: Astronomical Society of the Pacific (ASP), |c1996, edited by Hardee, Philip E.; Bridle, Alan H.; Zensus, J. Anton, p.319*O'Dea, C. P. 1998, *Publication of the Astronomical Society of the Pacific (PASP)*, 110, 493

- Onuchukwu, C.C., & Ubachukwu, A.A., (2013). Structural Asymmetries, Relativistic Beaming And Orientation Effects in Lobe-Dominated Quasars. *Astrophysics & Space Science (Ap&SS)*, 344, 211
- Orienti, M., & Dallacasa, D., (2010). Proper motion and apparent contraction in J0650+6001. *Monthly Notices of the Royal Astronomical Society (MNRAS)*, 406, 5290
- Parma, P., et al. (1999). Radiative ages in a representative sample of low luminosity radio galaxies. *Astronomy & Astrophysics (A&A)*, 344, 7
- Pearson, T.J., & Readhead, A. C. S., (1988), The milliarcsecond structure of a complete sample of radio sources. II - First-epoch maps at 5 GHz. *Astrophysical Journal (ApJ)*, 328, 114
- Perucho, M., & Mart, J. M. (2002). Physical Parameters in the Hot Spots and Jets of Compact Symmetric Objects, *Astrophysical Journal (ApJ)*, 568, 639
- Piner B.G., et al. (2007), Relativistic Jets in the Radio Reference Frame Image Database. I. Apparent Speeds From the First 5 Years Of Data. *Astrophysical Journal (ApJ)*, 133, 2357
- Polatidis, A.G. & Conway, J.E., (2003). Proper Motion in Compact Symmetric Objects. *Proceedings of the Astronomical Society of Australia, (PASA)*, 20, 69
- Ryle, M., & Longair, M.S., (1967). A Possible Method For Investigating The Evolution Of Radio Galaxies. *Monthly Notices of the Royal Astronomical Society (MNRAS)*, 136, 123
- Ryś, S., (2000), The Asymmetries in Radio Source Structures. II Generalized Kinematical Model. *Astronomy & Astrophysics (A&A)*, 355, 79
- Saikia, D. J., et al. (1995), *Monthly Notices of the Royal Astronomical Society (MNRAS)*, 276, 1215
- Scheuer, P.A.G., (1995). Lobe Asymmetry and Expansion Speed of Radio Source. *Monthly Notices of the Royal Astronomical Society (MNRAS)*, (277) 331-340.

Scheuer, P.A.G., (1974). Models of Extragalactic Radio Sources with a Continuous Energy Supply from A Central Object. *Monthly Notices of the Royal Astronomical Society (MNRAS)*, 166, 513.

Schoenmakers, A. P., et al. (2000). Radio galaxies with a 'double-double' morphology - III. The case of B1834+620. *Monthly Notices of the Royal Astronomical Society (MNRAS)*, 315, 395