

Some Factors Influencing Distribution Coefficients of Trace Amounts of M²⁺ Ions During the Crystallization of Mn(CH₃COO)₂·4H₂O

Marek Smolik* and Łukasz Siepietowski

Department of Chemistry, Inorganic Technology and Fuel, Silesian University of Technology, Gliwice, Poland.

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ABSTRACT

Distribution coefficients, D_{2/1} (Henderson – Kraček, Khlopin) of trace amounts of Ni²⁺, Mg²⁺, Cu²⁺, Co²⁺, Zn²⁺, Cd²⁺, Ca²⁺, and Sr²⁺ have been determined during the crystallization of Mn(CH₃COO)₂·4H₂O. Their dependencies on several properties of co-crystallizing acetate hydrates M(CH₃COO)₂·nH₂O as well as co-crystallizing M²⁺ ions have been analyzed. The D_{2/1} values fall in the range from 0.011 (D_{Cu}) to 0.28 (D_{Co}) and indicate the possibility of effective removal of trace amounts of most investigated ions during the crystallization of Mn(CH₃COO)₂·4H₂O at 25 °C. They generally do not depend directly on most investigated factors, but those of Mg²⁺, Ni²⁺ and Co²⁺ ions, which form acetate tetrahydrates like Mn(CH₃COO)₂·4H₂O, closely depend on electronegativity of the elements as well as solubility and η parameter and may be estimated on the basis of the mentioned properties using simple formulae.

KEYWORDS

Crystallization, manganese(II) acetate tetrahydrate, Henderson-Kraček, Khlopin distribution coefficients, D.

1. Introduction

Co-crystallization coefficients D_{2/1} (Henderson – Kraček, Khlopin) are important indicators of the effectiveness of crystallization as a method of purification. Therefore they are needed in preparation of high-purity salts. However, their calculation using the general thermodynamic equation relating D_{2/1} to the solubility of co-crystallizing salts Mn(CH₃COO)₂·4H₂O and M(CH₃COO)₂·nH₂O[±]:

$$D_{2,II/I,I} = \left(\frac{\gamma_{01} \cdot \gamma_{m01}}{\gamma_{02} \cdot \gamma_{m02}} \right)^3 \cdot \left(\frac{\gamma_{m2}}{\gamma_{m1}} \right)^3 \cdot \frac{f_1}{f_2} \cdot \exp\left(-\frac{\Delta\mu_{II \rightarrow I}^0}{RT} \right) \quad (1)$$

is not possible because of a lack of the suitable data (mainly $\Delta\mu_{II \rightarrow I}$ as well as f₁(f₂)). Hence the effect of chemical, physicochemical and crystal-chemical factors on D_{2/1} values is sought. Such dependences have already been established¹ in sulfate (MSO₄·nH₂O), nitrate (M(NO₃)₂·nH₂O), chloride (MCl₂·nH₂O) and formate (M(HCOO)₂·nH₂O) crystallization systems.

However acetate crystallization systems (M(CH₃COO)₂·nH₂O) have been less well studied and D_{2/1} coefficients of trace amounts of M²⁺ ions have only been determined in the case of Ni(CH₃COO)₂·4H₂O,² Co(CH₃COO)₂·4H₂O,³ as well as Mg(CH₃COO)₂·4H₂O and Cu(CH₃COO)₂·H₂O crystallization.⁴

In the case of Mn(CH₃COO)₂·4H₂O only four co-crystallization

coefficients D_{2/1} for comparable amounts of other acetates are available: for Mg²⁺ (D_{2/1} = 0.07), for Zn²⁺ (D_{2/1} = 0.30), for Co²⁺ (D_{2/1} = 0.28) and for Ni²⁺ (D_{2/1} = 1.3).⁵

The purpose of this work was to determine the co-crystallization coefficients D_{M/Mn(CH₃COO)₂·4H₂O} of trace amounts (10⁻³–10⁻¹ %) of M²⁺ ions (M²⁺ = {Mg²⁺, Cu²⁺, Co²⁺, Zn²⁺, Ni²⁺, Cd²⁺, Ca²⁺, Sr²⁺}) with Mn(CH₃COO)₂·4H₂O as well as to analyze the influence of some physicochemical and crystal-chemical properties of Mn(CH₃COO)₂·4H₂O and M(CH₃COO)₂·nH₂O as well as Mn²⁺ and M²⁺ ions on D_{M/Mn(CH₃COO)₂·nH₂O} (D_{2/1}) coefficients.

2. Experimental

2.1. Reagents and Solutions

Solutions of Ni(II), Co(II), Cu(II), Cd(II), Zn(II), Mg(II), Ca(II) and Sr(II) acetates were prepared by dissolution of the acetate salt (POCh-Gliwice) in water. Ammonia solution (14 mole L⁻¹) was obtained by saturating distilled water with ammonia gas. Sodium versenate p.a. (POCh-Gliwice) – 0.1 mole L⁻¹ water solution, ascorbic acid p.a. (POCh-Gliwice), NH₃–NH₄Cl buffer solution of pH 10 and eriochrome black T ind. (POCh-Gliwice) were used.

2.2. Analytical Methods

The *macrocomponent*: manganese was determined (after addition of ascorbic acid) by complexometric titration with sodium versenate in NH₃–NH₄Cl buffer solution (pH 10) in the presence of eriochrome black T ind.⁶ From the manganese(II) content of the mother solution and solution containing dissolved crystal the degree of Mn(CH₃COO)₂·4H₂O crystallization, α , was found, as well as the volumes of these solutions (containing 0.300 g of Mn(CH₃COO)₂·4H₂O) calculated.

The *microcomponents* (Cu, Zn, Ni, Co, Mg, Cd, Ca and Sr) were determined by means of direct atomic absorption spectrometry (Perkin Elmer 3300) from solutions containing 0.300 g of

¹Where m₀₁(m₀₂), γ_{m01} (γ_{m02}) = solubility/mol kg⁻¹ of Mn(CH₃COO)₂·4H₂O(M(CH₃COO)₂·nH₂O) and mean molal activity coefficient of Mn(CH₃COO)₂·4H₂O(M(CH₃COO)₂·nH₂O) in its binary saturated solution; m₁(m₂), γ_{m1} (γ_{m2}) = solubility/mol kg⁻¹ and mean molal activity coefficient of Mn(CH₃COO)₂·4H₂O (M(CH₃COO)₂·nH₂O) in the ternary solution being in equilibrium with (Mn,M)(CH₃COO)₂·nH₂O solid solution; x₁(x₂) = mole fraction of Mn²⁺(M²⁺) ion, and f₁(f₂) = activity coefficient of ion Mn²⁺(M²⁺) in this solid solution; $\Delta\mu_{II \rightarrow I}^0$ = the molar partial Gibbs free energy of the phase transition of (M(CH₃COO)₂·nH₂O) from its structure (II) into the structure (I) of Mn(CH₃COO)₂·4H₂O; R = gas constant, T = temperature /K.

* To whom correspondence should be addressed. E-mail: marek.smolik@polsl.pl

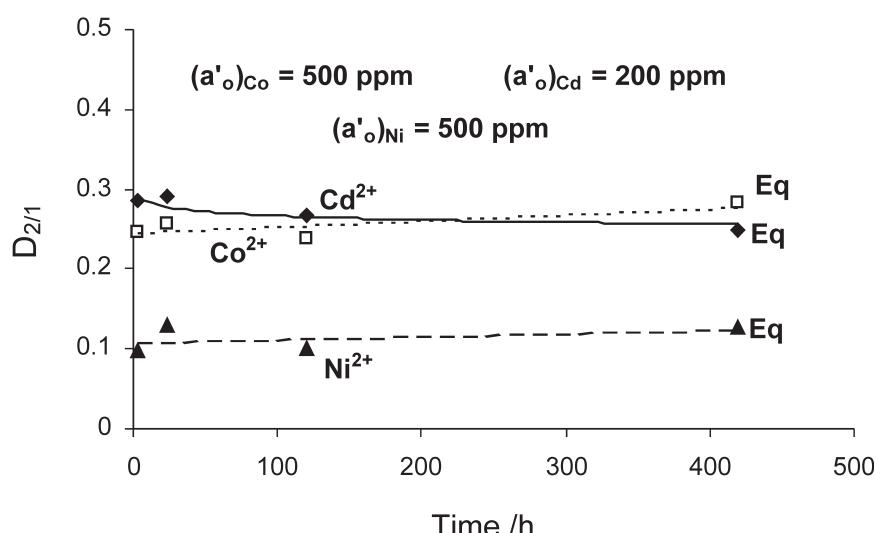


Figure 1 The dependence of co-crystallization coefficients $D_{2/1}$ of Co^{2+} , Cd^{2+} , Ni^{2+} on time of crystallization of $\text{Mn}(\text{CH}_3\text{COO})_2 \cdot 4\text{H}_2\text{O}$ at 25°C ; a'_o = initial concentration of M^{2+} in relation to $\text{Mn}(\text{CH}_3\text{COO})_2 \cdot 4\text{H}_2\text{O}$; Eq = equilibrium values of $D_{2/1}$ obtained by the second method.

$\text{Mn}(\text{CH}_3\text{COO})_2 \cdot 4\text{H}_2\text{O}$ in 25 mL of solution. Absorbances of the samples and of the sets of standards having the same concentrations of the matrix (manganese(II) acetate), were measured under the same conditions.

2.3. Methods of Determination of Distribution Coefficients

Distribution coefficients, $D_{\text{M}/\text{Mn}(\text{CH}_3\text{COO})_2 \cdot 4\text{H}_2\text{O}}$ were determined at $25 \pm 1^\circ\text{C}$ using the following two methods:

- 1) the method of isothermal leveling of supersaturation of manganese(II) acetate solutions by stirring its supersaturated solutions for 4–120 hours;
- 2) the method of long-time stirring of crushed $\text{Mn}(\text{CH}_3\text{COO})_2 \cdot 4\text{H}_2\text{O}$ crystals in their saturated solution – achieving the equilibrium ‘from above’ (D°_{MAX}) and ‘from below’ (D°_{min}).

Details of both methods as well as preparation of samples of crystals and mother solutions before analysis are described earlier.^{3,7} Determined by the above mentioned AAS method relative concentrations of microcomponents: $-a'_k$ ($\mu\text{g M}/1\text{g } \text{Mn}(\text{CH}_3\text{COO})_2 \cdot 4\text{H}_2\text{O}$ in the washed crystal in ppm) and $-a'_r$ ($\mu\text{g M}/1\text{g } \text{Mn}(\text{CH}_3\text{COO})_2 \cdot 4\text{H}_2\text{O}$ in the mother solution in ppm) were applied to calculate the homogeneous distribution coefficients –

$D_{2/1}$ (Henderson-Kraček, Khlopin) by means of the following equation:

$$D_{2/1} = D_{\text{M}/\text{Mn}(\text{CH}_3\text{COO})_2 \cdot 4\text{H}_2\text{O}} = \frac{a'_k}{a'_r}. \quad (2)$$

The results are given in Figs 1 and 2 (the first method) and in Table 1 (the equilibrium values).

3. Results and Discussion

Co-crystallization coefficients, $D_{2/1}$, of microcomponents with $\text{Mn}(\text{CH}_3\text{COO})_2 \cdot 4\text{H}_2\text{O}$ determined by the first method generally change with increasing time of stirring, and generally tend to the equilibrium $D_{2/1}$ values, obtained by the second method (Figs 1 & 2, Table 1). They had diverse values ranging from $D_{\text{Cu}/\text{Mn}(\text{CH}_3\text{COO})_2 \cdot 4\text{H}_2\text{O}} = 0.011$ to $D_{\text{Co}/\text{Mn}(\text{CH}_3\text{COO})_2 \cdot 4\text{H}_2\text{O}} = 0.28$.

These values indicate, that effective removal of trace amounts of most investigated ions (excepting Co^{2+} , Cd^{2+} , Ni^{2+}) is possible by means of crystallization of $\text{Mn}(\text{CH}_3\text{COO})_2 \cdot 4\text{H}_2\text{O}$ at 25°C , and so may be used in the preparation of high purity manganese salts.

The dependences of the coefficients $D_{2/1}$ on various properties of the co-crystallizing salts ($\text{Mn}(\text{CH}_3\text{COO})_2 \cdot 4\text{H}_2\text{O}$ and

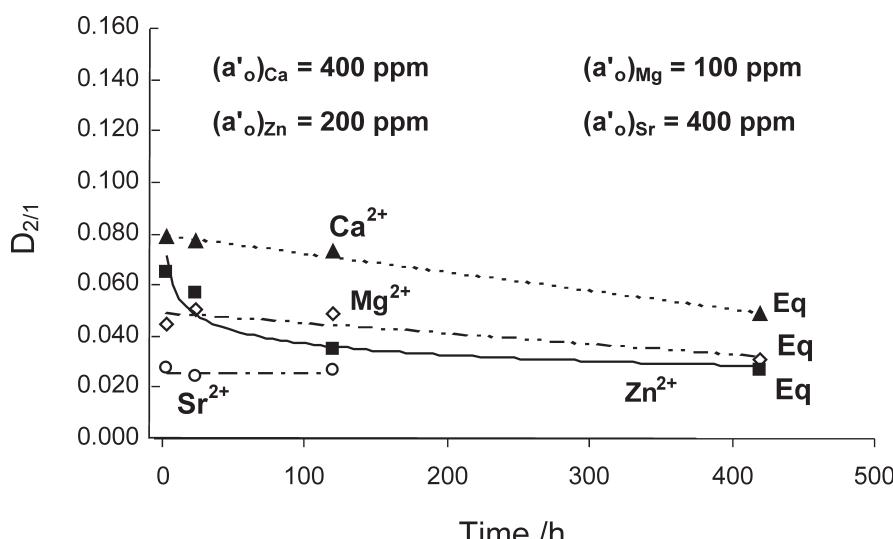


Figure 2 The dependence of co-crystallization coefficients $D_{2/1}$ of Ca^{2+} , Sr^{2+} , Mg^{2+} , Zn^{2+} on time of crystallization of $\text{Mn}(\text{CH}_3\text{COO})_2 \cdot 4\text{H}_2\text{O}$ at 25°C ; a'_o = initial concentration of M^{2+} in relation to $\text{Mn}(\text{CH}_3\text{COO})_2 \cdot 4\text{H}_2\text{O}$; Eq = equilibrium values of $D_{2/1}$, obtained by the second method.

Table 1 Equilibrium co-crystallization coefficients $D_{2/1}$ of trace amounts of M^{2+} ions with $Mn(CH_3COO)_2 \cdot 4H_2O$ at 25 °C.

Microcomponent M^{2+}	Initial distribution coefficient after long-time stirring		Average distribution coefficient		Average equilibrium distribution coefficient $\bar{D} \pm t_\alpha \frac{s}{\sqrt{n}}$
			for D^0_{\min}	for D^0_{\max}	
	$D^0_{\min} = \frac{a'_{k_0}}{a'_{r_0}}$	$D^0_{\max} = \frac{a'_{k_0}}{a'_{r_0}}$	$\bar{D} \pm t_\alpha \frac{s}{\sqrt{n}}$	$\bar{D} \pm t_\alpha \frac{s}{\sqrt{n}}$	
Ni^{2+}	0.040	0.40	0.113 ± 0.007	0.141 ± 0.036	0.127 ± 0.009
Mg^{2+}	0.025	0.30	0.028 ± 0.004	0.034 ± 0.006	0.031 ± 0.004
Cu^{2+}	0.005	1.00	0.012 ± 0.005	0.010 ± 0.004	0.011 ± 0.003
Co^{2+}	0.120	0.50	0.28 ± 0.02	0.28 ± 0.02	0.28 ± 0.01
Zn^{2+}	0.020	0.20	0.023 ± 0.008	0.031 ± 0.007	0.027 ± 0.005
Cd^{2+}	0.080	0.80	0.25 ± 0.01	0.26 ± 0.01	0.25 ± 0.01
Ca^{2+}	0.030	0.30	0.043 ± 0.004	0.054 ± 0.013	0.049 ± 0.007

\bar{D} = mean value of $D_{M/Mn(CH_3COO)_2 \cdot 4H_2O}$; t_α = value of Student's t-test for $(n-1)$ degrees of freedom and for the confidence level of $(1-\alpha) = 0.95$; n = number of determinations; s = standard deviation; D^0_{\min} , D^0_{\max} = initial minimum and maximum values of $D_{M/Mn(CH_3COO)_2 \cdot 4H_2O}$ respectively.

$M(CH_3COO)_2 \cdot nH_2O$ as well as the metal ions Mn^{2+} and M^{2+} have been analyzed. These properties are presented in Table 2.

3.1. Effect of Solubility of Co-crystallizing Salts

The dependence of $\log D_{2/1}$ on $\log (m_{01}/m_{02})$ for all determined co-crystallization coefficients is not significant (correlation coefficient $\rho_{xy} = -0.3552$). Analogous correlation for coefficients $D_{Ni/Mn(CH_3COO)_2 \cdot 4H_2O}$, $D_{Mg/Mn(CH_3COO)_2 \cdot 4H_2O}$, $D_{Co/Mn(CH_3COO)_2 \cdot 4H_2O}$, that is, for monodentate-bonded acetates¹⁵ that form monoclinic acetate tetrahydrates of similar structure to $Mn(CH_3COO)_2 \cdot 4H_2O$, is higher, but not significant as well ($\rho_{xy} = 0.7421$).

3.2. Effect of Ionic Radius

The effect of ionic radius on coefficients $D_{2/1}$ is presented in Fig. 3. They change irregularly as ionic radius increases and achieve the lowest values for Ca^{2+} and Sr^{2+} ($D_{2/1} < 0.06$), for which $r_{Mn^{2+}} - r_{Ca(Sr)^{2+}}/r_{Mn^{2+}} > 0.22$.

3.3. Effect of Some Other Factors

Correlation coefficients (ρ_{xy}) of $y = \ln D_{2/1}$ or (where $\pi = \ln D_{2/1} - \ln(m_{01}/m_{02})^3$) and $x = \{\Delta\epsilon, \Delta s, \Delta h$ and $\Delta n\}$ (where Δ are differences of: electronegativity, crystal field stabilization energy, hardness and number of molecules of crystallization water respectively) are presented in Table 3.

As can be seen, values of $\ln D_{2/1}$ for all investigated ions ($k = 8$) do not depend directly on crystal field stabilization energy (Δs), electronegativity ($\Delta\epsilon$), hardness of cation (Δh) as well as on the

number of molecules of crystallization water (Δn). Corresponding correlation coefficients are insignificant.

However, in the case of acetate tetrahydrates of $Ni(II)$, $Mg(II)$, $Co(II)$ (with monodentate acetate ligands) $\ln D_{2/1}$ is correlated to $|\Delta\epsilon|$ ($\rho_{xy} = 0.9820$) and π depends on $(\Delta n/\eta_M)^2$ ($\rho_{xy} = -0.9987$). Hence it is possible to estimate coefficients $D_{Ni/Mn(CH_3COO)_2 \cdot 4H_2O}$, $D_{Co/Mn(CH_3COO)_2 \cdot 4H_2O}$ and $D_{Mg/Mn(CH_3COO)_2 \cdot 4H_2O}$ by means of the two following empirical equations:

$$D_{2/1} = \left(\frac{m_{01}}{m_{02}} \right)^3 \cdot e^{-8272 \left(\frac{\eta_1 - \eta_2}{\eta_1} \right)^2 + 0.698} \quad (3)$$

(at an average relative error not exceeding 7.8 %); or

$$D_{2/1} = e^{-7.644|\epsilon_1 - \epsilon_2| - 0.687} \quad (4)$$

(at an average relative error not exceeding 15.6 %); where $m_{01}(m_{02})$ = solubility of $Mn(CH_3COO)_2 \cdot 4H_2O(M'$ ($CH_3COO)_2 \cdot nH_2O$), $M' = \{Co, Ni, Mg\}$; $\eta_1(\eta_2) = \eta_{Mn(CH_3COO)_2 \cdot 4H_2O}(\eta_{M'(CH_3COO)_2 \cdot nH_2O})$; $\epsilon_1(\epsilon_2) = \epsilon_{Mn}(\epsilon_{M'})$.

The average coefficient, $D_{2/1}$ for open shell ions (Cu^{2+} , Ni^{2+} , Co^{2+}) is almost twice as great as that for closed shell ions (Mg^{2+} , Zn^{2+} , Cd^{2+} , Ca^{2+} , Sr^{2+}).

4. Conclusion

Co-crystallization coefficients, $D_{2/1}$ of trace amounts of M^{2+} ions with $Mn(CH_3COO)_2 \cdot 4H_2O$ range from 0.011 ($D_{Cu/Mn(CH_3COO)_2 \cdot 4H_2O}$) to 0.282 ($D_{Co/Mn(CH_3COO)_2 \cdot 4H_2O}$). Their values indicate the possibility

Table 2 Some properties of co-crystallizing salts ($M(CH_3COO)_2 \cdot nH_2O$) and ions (M^{2+}) where CS is the crystal system; m = solubility in water at 25 °C; EC = electronic configuration of M^{2+} ion; r = radius of M^{2+} ion¹²; h = cation M^{2+} hardness¹³; ε = electronegativity¹⁴; η = $10^3 \cdot \sqrt[3]{\frac{M_x}{d \cdot N}}$, M_x = molar mass of $M(CH_3COO)_2 \cdot nH_2O/g \cdot mole^{-1}$; d = density/g cm⁻³; N = Avogadro number; and s = crystal field stabilization energy of M^{2+} ion.

Salt	CS	$m/mol kg^{-1}$	M^{2+}	EC	r/Å	ε	h/eV	$\eta/\text{\AA}$	s/Dq^e
$Ni(CH_3COO)_2 \cdot 4H_2O$	monoclinic	0.747 ^a	Ni^{2+}	[Ar]3d ⁸	0.70	1.75	0.29	6.191	1.2
$Mg(CH_3COO)_2 \cdot 4H_2O$	monoclinic	4.608 ^a	Mg^{2+}	[Ne]	0.72	1.23	2.53	6.261	0.0
$Cu(CH_3COO)_2 \cdot H_2O$	monoclinic	0.284 ^b	Cu^{2+}	[Ar]3d ⁹	0.73	1.75	-0.55	5.583	0.6
$Co(CH_3COO)_2 \cdot 4H_2O$	monoclinic	1.453 ^b	Co^{2+}	[Ar]3d ⁷	0.735	1.70	0.44	6.232	0.8
$Zn(CH_3COO)_2 \cdot 2H_2O$	orthorhombic	1.688 ^b	Zn^{2+}	[Ar]3d ¹⁰	0.745	1.66	-1.02	5.929	0.0
$Mn(CH_3COO)_2 \cdot 4H_2O$	monoclinic	2.570 ^c	Mn^{2+}	[Ar]3d ⁵	0.82	1.60	0.69	6.369	0.0
$Cd(CH_3COO)_2 \cdot 2H_2O$	monoclinic	4.314 ^c	Cd^{2+}	[Kr]3d ¹⁰	0.95	1.46	-2.04	5.936	0.0
$Ca(CH_3COO)_2 \cdot H_2O$	monoclinic	2.172 ^c	Ca^{2+}	[Ar]	1.00	1.04	2.33	5.574	0.0
$Sr(CH_3COO)_2 \cdot 0.5H_2O$	hexagonal	1.954 ^d	Sr^{2+}	[Kr]	1.16	0.99	2.15	5.659	0.0

^a From ref. 8; ^b From ref. 9; ^c From ref. 10; ^d From ref. 11; ^e Dq = natural theoretical unit for crystal-field splitting energies.

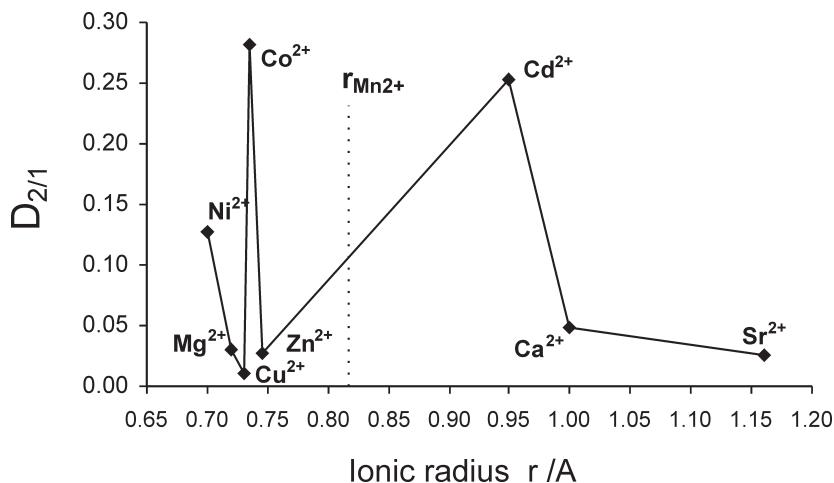


Figure 3 The effect of ionic radius of M^{2+} on co-crystallization coefficients $D_{2/1}$.

Table 3 Correlation coefficients (ρ_{xy}) of $y = \{\ln D_{2/1}; \pi\}$ and $x = \{r, \Delta\varepsilon; \Delta\mu, \Delta n, \Delta h\}$ for co-crystallizing salts $(Mn(CH_3COO)_2 \cdot 4H_2O)$ and $M(CH_3COO)_2 \cdot nH_2O$ and ions (Mn^{2+} and M^{2+}).

y	x	Correlation coefficient ρ_{xy}	Number of investigated ions k
$\ln D_{2/1}$	r	-0.0479	8
$\ln D_{2/1}$	$\Delta\varepsilon$	-0.3243	8
$\ln D_{2/1}$	Δh	0.2845	8
$\ln D_{2/1}$	Δn	-0.5379	8
$\ln D_{2/1}$	Δs	-0.3242	8
$\ln D_{2/1}$	$ \Delta\varepsilon $	0.9820	3 ($Mg^{2+}, Co^{2+}, Ni^{2+}$)
$\pi = \ln D_{2/1} - \ln(m_{01}/m_{02})^3$	$(\Delta\eta/\eta_M)^2$	-0.9987^t	3 ($Mg^{2+}, Co^{2+}, Ni^{2+}$)

^tSignificant correlation coefficient ρ_{xy} is indicated in bold.

of effective removal of trace amounts of most investigated ions during the crystallization of $Mn(CH_3COO)_2 \cdot 4H_2O$ at 25 °C. This may find application in preparation of high-purity manganese(II) salts.

Coefficients $D_{2/1}$ for Mg^{2+} , Ni^{2+} and Co^{2+} ions, which form (like $Mn(CH_3COO)_2 \cdot 4H_2O$) acetate tetrahydrates, closely depend on electronegativity of the elements as well as η and may be calculated using simple empirical formula.

M^{2+} ions, whose radii $r_{M^{2+}}$ fulfill the following condition: $|r_{Mn^{2+}} - r_{M^{2+}}|/r_{Mn^{2+}} > 0.22$ have very low values of their

co-crystallization coefficients ($D_{M^{2+}/Mn(CH_3COO)_2 \cdot 4H_2O} < 0.06$).

Open shell ions ($Cu^{2+}, Ni^{2+}, Co^{2+}$) generally co-crystallize with $Mn(CH_3COO)_2 \cdot 4H_2O$ to a greater degree than closed shell ones ($Mg^{2+}, Zn^{2+}, Cd^{2+}, Ca^{2+}, Sr^{2+}$).

References

1. M. Smolik, *Zesz. Nauk. Pol. Sl. s. Chem.*, 2004, **1617**, 1–186.
2. M. Smolik, *Ann. Polish Chem. Soc.*, 2005, 297–299.
3. M. Smolik, A. Jakóbik-Kolon and J. Trojanowska, *Sepm. Purif. Techn.*, 2007, **54**, 272–276.
4. M. Smolik, *Chemik*, 2008, **10**, 526–529.
5. Chr. Balarew, *Massovaya Kristallizatsya*, 1977, **3**, 151–154.
6. W.J. Welcher, *The Analytical Uses of EDTA*, Van Nostrand Comp. Inc., New Jersey, London, Toronto, 1958, pp. 217.
7. V.G. Khlopin, *Izbr. trudy*, vol. 6, Izd. AN SSSR, Moskva, 1957, pp. 173.
8. Chr. Balarew and D. Stoilova, *Dokl. Bolg. Akad. Nauk*, 1974, **27**, 803–805.
9. D. Stoilova, Chr. Balarew, *Dokl. Bolg. Akad. Nauk*, 1981, **34**, 1397–1400.
10. Chr. Balarew, D. Stoilova, *Zh. Neorg. Khim.*, 1976, **21**, 555–565.
11. A. Seidel, W.F. Linke, *Solubilities of Inorganic and Metal Organic Compounds*, Van Nostrand, New York, USA, 1958, pp. 1499.
12. R.D. Shannon, C.T. Prewitt, *Acta Cryst.*, 1969, **B25**, 925–946.
13. Chr. Balarew, R. Duhlev, D. Spassov, *Crystal Res. Technol.*, 1984, **19**(11), 1469–1475.
14. A.L. Allred, E.G. Rochow, *J. Inorg. Nucl. Chem.* 1958, **5**, 264–268.
15. Chr. Balarew, *Z. Kristallogr.* 1987, **181**, 35–82.