# The Vibrational Spectra of the Boron Halides and their Molecular Complexes. Part 8. Ab initio Studies of the Complexes of Boron Trifluoride with Water and Hydrogen Sulphide 

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Received 25 January 2006; revised and accepted 17 October 2006.


#### Abstract

The structures, interaction energies and vibrational spectra of the van der Waals complexes formed between boron trifluoride, as Lewis acid, and water and hydrogen sulphide, as Lewis bases, have been determined by means of ab initio calculations at the second-order level of Møller-Plesset perturbation theory, using a number of basis sets, including double- and triple-zeta, with polarization and diffuse functions. Two conformers, an eclipsed and a staggered species, have been examined for each complex. In the case of the boron trifluoride-water complex, the spectra computed using the largest basis set have been compared with the spectra obtained experimentally in nitrogen, argon and neon matrices at cryogenic temperatures.


## KEYWORDS

$A b$ initio calculations, molecular complexes, boron trifluoride, water; hydrogen sulphide, molecular structures, interaction energies, vibrational spectra.

## 1. Introduction

Some years ago we reported the infrared spectrum of boron trifluoride and water co-condensed in nitrogen matrices at ca. 20 K , and interpreted the results in terms of a 1:1 molecular complex formed between $\mathrm{BF}_{3}$ and $\mathrm{H}_{2} \mathrm{O} .{ }^{1}$ A partial assignment of the spectrum of this complex in argon matrices had been reported by Hunt and Ault, ${ }^{2}$ but these authors were unable to locate all of the fundamentals of the aggregate. In order to assist with the assignment of our spectra, we supplemented our experimental measurements with an ab initio calculation, at the restricted Hartree-Fock (RHF) level and with a small (4-31G) basis set. ${ }^{1}$ This calculation enabled us to make tentative assignments of eight of the nine intramolecular modes of the complex, and of the two highest-frequency intermolecular modes. Experimental spectra of $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ in argon ${ }^{3}$ and neon ${ }^{4}$ matrices have subsequently been reported, but a full assignment remains elusive. Ab initio computations of the spectrum of $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$, at the RHF and second-order Møller-Plesset (MP2) levels of theory, using six different basis sets, ${ }^{5}$ and at the RHF, MP2, QCISD and $\operatorname{CCSD}(\mathrm{T})$ levels with the $6-311+\mathrm{G}(\mathrm{d}, \mathrm{p})$ basis set, ${ }^{4}$ have helped to clarify our understanding of the spectrum of this species, but several questions still remain. Our recent experience with some weakly-bound molecular complexes, e.g. $\left(\mathrm{NH}_{3}\right)_{2}$ and $\left(\mathrm{PH}_{3}\right)_{2},{ }^{6}$ and $\mathrm{H}_{2} \mathrm{O} \cdot \mathrm{CO}_{2}$ and $\mathrm{H}_{2} \mathrm{~S} \cdot \mathrm{CO}_{2}{ }^{7}{ }^{7}$ has taught us that for such aggregates the preferred structure may be a function of the basis set used, and the use of different basis sets sometimes leads to quite different optimized structures. Our original RHF/4-31G computation for $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ suggested that the $\mathrm{H}_{2} \mathrm{O}$ molecule was coordinated with $\mathrm{BF}_{3}$ with the $\mathrm{H}_{2} \mathrm{O}$ angle bisector presenting virtually perpendicularly to the plane of $\mathrm{BF}_{3} .{ }^{1}$ However, some trial calculations at the MP2 level with larger basis sets showed that in each case the $\mathrm{H}_{2} \mathrm{O}$

[^0]molecule adopted an eclipsed conformation relative to $\mathrm{BF}_{3}$, but in some cases a staggered conformation was also found to be a stationary point. In an attempt fully to characterize the true structure and vibrational spectrum of the $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ complex, we have undertaken a systematic reinvestigation of this adduct, at the correlated (MP2) level of theory. We employed a range of basis sets featuring both double- and triple-zeta bases, with and without polarization and diffuse functions, in order to explore the effect of these various features of the basis sets on the optimized geometry. We have also recalculated the vibrational spectrum of $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ using the largest basis set, in the expectation of removing the earlier ambiguities in the predicted ${ }^{1,4,5}$ and experimental ${ }^{1-4}$ vibrational assignments. These calculations form part of an ongoing theoretical study of the properties of the complexes of $\mathrm{BF}_{3}$ with other oxygen bases, e.g. $\mathrm{CO}_{2},{ }^{8} \mathrm{~N}_{2} \mathrm{O},{ }^{9} \mathrm{SO}_{2}{ }^{10}$ and $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{O} .{ }^{11}$
In view of the expected similarity between the complexes of $\mathrm{BF}_{3}$ with $\mathrm{H}_{2} \mathrm{O}$ and with its analogue $\mathrm{H}_{2} \mathrm{~S}$, we have included parallel studies of the $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{~S}$ complex, under the same computational conditions, in order to confirm their similarities and to reveal whatever differences may exist among their properties. This complex is the second adduct of $\mathrm{BF}_{3}$ with a sulphur base which we have examined in this way, following an earlier study of $\mathrm{BF}_{3} \cdot\left(\mathrm{CH}_{3}\right)_{2} \mathrm{~S} .{ }^{11}$

## 2. Computational Details

The calculations were carried out using the Gaussian-98 program, ${ }^{12}$ at the MP2 level of theory. ${ }^{13}$ Full geometry optimizations were carried out, using the VERYTIGHT convergence criterion, ${ }^{12}$ mainly with the Berny algorithm, ${ }^{14}$ but with the MurtaghSargent option ${ }^{15}$ in cases of slow convergence. Interaction energies were computed and corrected for basis set superposi-


Figure 1 The optimized structures of the $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{~S}$ complexes determined using the $6-311++\mathrm{G}(\mathrm{d}, \mathrm{p})$ basis set: (a) eclipsed $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ (energy minimum); (b) staggered $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ (saddle point); (c) staggered $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{~S}$ (energy minimum); (d) eclipsed $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{~S}$ (saddle point).
tion error (BSSE), ${ }^{16}$ using the Boys-Bernardi full counterpoise method, ${ }^{17}$ and for zero-point energy differences. We employed eight basis sets, $6-31 \mathrm{G}, 6-31++\mathrm{G}, 6-31 \mathrm{G}(\mathrm{d}, \mathrm{p}), 6-31++\mathrm{G}(\mathrm{d}, \mathrm{p})$, $6-311 \mathrm{G}, 6-311++\mathrm{G}, 6-311 \mathrm{G}(\mathrm{d}, \mathrm{p})$ and $6-311++\mathrm{G}(\mathrm{d}, \mathrm{p})$. This range of bases allowed us to examine the effect of adding first diffuse functions, then polarization functions, then both augmentations on all atoms, to the standard double-zeta 6-31G basis, and then repeating the stepwise augmentation strategy starting with the triple-zeta 6-311G basis set.

## 3. Results and Discussion

### 3.1. Molecular Structures

The effect of changing the basis set on the calculated properties of the various species is illustrated by reference to the minimized energies of the $\mathrm{BF}_{3}$ monomer. The energies are plotted as a function of the basis set in Supplementary Material, Fig. SM1. The greatest effect on the energy of improving the basis set is achieved by the addition of polarization functions, followed by substitution of double-zeta by triple-zeta, and the least significant influence is the addition of diffuse functions.
The effect of basis set on the optimized geometries is illustrated in the Supplementary Material, Table SM1, where the computed bond lengths and angles of the three monomers are listed for each basis set, along with the experimental structural parameters. ${ }^{18-20}$ The individual percentage errors are all within $5 \%$, with the exception of the HOH bond angle, which is overestimated by $6.19 \%(6-31+G)$ and $6.33 \%(6-311+G)$. The inclusion of polarization functions is found to have a strong positive influence in reducing the errors between the computed and experimental geometrical parameters.
In our earlier study of $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O},{ }^{1}$ at the RHF/4-31G level, we found that the angle, $\Theta$, between the $\mathrm{C}_{2}$ axis of $\mathrm{H}_{2} \mathrm{O}$ and the $\mathrm{C}_{3}$ axis of $\mathrm{BF}_{3}$ was close to $180^{\circ}$, indicating that coordination involved mainly the axial ( $3 a_{1}$ ) non-bonding orbital of $\mathrm{H}_{2} \mathrm{O}$. The direction of the deviation of the angle $\Theta$ from linearity determines whether the conformation of each complex is eclipsed or staggered; in either case the point group of the complex is expected to be $\mathrm{C}_{\mathrm{s}}$. Supplementary Material Table SM2 reports
the minimized energies and Hessian indices of the $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{~S}$ adducts for each basis set studied. For $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ the results obtained with the $6-31 \mathrm{G}, 6-31++\mathrm{G}, 6-311 \mathrm{G}$ and $6-311++G$ basis sets failed unambiguously to identify the preferred species. In these cases, optimization starting with either the eclipsed or the staggered conformation led to essentially the same structure, with coordination of the $\mathrm{H}_{2} \mathrm{O}$ molecule at the B atom virtually perpendicular to the $\mathrm{BF}_{3}$ pseudo-plane, as we found at the RHF/4-31G level. ${ }^{1}$
With the $6-31 \mathrm{G}$ and $6-31++\mathrm{G}$ basis sets, this converged structure turned out to be a first-order saddle point on the potential energy surface, while in the $6-311 \mathrm{G}$ and $6-311++\mathrm{G}$ cases it represented a true minimum. It was only on the introduction of polarization functions, in the $6-31 \mathrm{G}(\mathrm{d}, \mathrm{p}), 6-31++\mathrm{G}(\mathrm{d}, \mathrm{p})$, $6-311 \mathrm{G}(\mathrm{d}, \mathrm{p})$ and $6-311++\mathrm{G}(\mathrm{d}, \mathrm{p})$ bases, that the eclipsed and staggered conformations could be clearly distinguished. For all four of these bases the eclipsed structure was found to be the minimum and the staggered a first-order saddle point. The imaginary mode representing the reaction coordinate in these four cases was the torsional mode of the $\mathrm{H}_{2} \mathrm{O}$ molecule about the B...O axis. It appears, therefore, that only those basis sets which include polarization functions have sufficient directional properties to enable the two conformers of $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ to be separated reliably. The optimized structures of the eclipsed and staggered species of $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$, determined with the $6-311++\mathrm{G}(\mathrm{d}, \mathrm{p})$ basis set, are illustrated in Figs 1(a) and 1(b).
For the $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{~S}$ complex, the preferred structure determined using the double-zeta basis sets oscillated between eclipsed $[6-31++G$ and $6-31++G(d, p)]$ and staggered [ $6-31 G$ and $6-31 \mathrm{G}(\mathrm{d}, \mathrm{p})]$. For the four triple-zeta results the staggered conformer was consistently found to be a true minimum. For this complex even the four bases which did not include polarization functions were able to discriminate between the two structural possibilities. This is probably because, even though the differences between the optimized eclipsed and staggered energies for each basis set are quite similar in both complexes, in those cases where the two conformers are clearly distinguished, the angle B...OX, where $X$ is the centre of mass of the $\mathrm{H}_{2} \mathrm{O}$ molecule, has an average value of about $122^{\circ}$, while the corresponding angle

Table 1 Intermolecular structural parameters ${ }^{\text {a }}$ of some $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{~S}$ complexes, computed with a variety of basis sets.

| Basis set | $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ |  | $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{~S}$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Eclipsed |  | Eclipsed |  | Staggered |  |
|  | R/pm | @/deg | $\mathrm{R} / \mathrm{pm}$ | ©/deg | $\mathrm{R} / \mathrm{pm}$ | $\Theta / \mathrm{deg}$ |
| 6-31G | - | - | - | - | 300.33 | 119.20 |
| $6-31++\mathrm{G}$ | - | - | 282.54 | 113.16 | - | - |
| $6-31 \mathrm{G}(\mathrm{d}, \mathrm{p})$ | 180.25 | 117.35 | - | - | 304.46 | 115.60 |
| $6-31++G(d, p)$ | 177.76 | 125.37 | 292.84 | 107.30 | - | - |
| 6-311G | - | - | - | - | 312.94 | 122.39 |
| $6-311++G$ | - | - | - | - | 270.65 | 106.08 |
| 6-311G(d,p) | 183.61 | 120.71 | - | - | 310.28 | 115.97 |
| $6-311++G(d, p)$ | 181.57 | 125.71 | - | - | 290.87 | 100.94 |

${ }^{a} R$ is the B...O or B...S separation; $\Theta$ is the B...OX or B...SX angle, where $X$ is the centre of mass of the electron donor molecule.
in $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{~S}$ averages approximately $110^{\circ}$ (eclipsed) and $113^{\circ}$ (staggered). This results in the amplitude of the torsional motion which interconverts the two conformers in $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{~S}$ being larger than that in $\mathrm{BF}_{3} . \mathrm{H}_{2} \mathrm{O}$, enabling the conformers to be more clearly differentiated. Figures 1(c) and 1(d) show the optimized eclipsed and staggered structures of $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{~S}$, computed with the largest basis set.

The difference in the conformational preferences of the two complexes may be rationalized as follows. In the $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ complex, the eclipsed conformer is stabilized by an electrostatic attraction between the partially positively-charged hydrogen atoms and the fractionally negatively-charged fluorine atoms which straddle the symmetry plane. The closest approach of these two pairs of atoms is achieved when the complex adopts the eclipsed conformation. In the $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{~S}$ complex, on the other hand, the partial positive charge on the hydrogen atoms is reduced, due to the lower electronegativity of sulphur compared with oxygen, and the average distance between the hydrogens and the out-of-plane fluorines is substantially increased. This diminishes the electrostatic H...F attraction, and the steric effect becomes dominant. The repulsion of the H and $F$ atoms is maximized when the complex is in the staggered conformation.
The intermolecular structural parameters of the two complexes are collected in Table 1, for those species for which the eclipsed and staggered conformers could be distinguished, and which were found to be true minima. For the eclipsed $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ complex the smaller basis sets underestimate the van der Waals bond length, but have little effect on the angle $\Theta$. In the case of eclipsed $\mathrm{BF}_{3} . \mathrm{H}_{2} \mathrm{~S}$, a larger $\mathrm{B} \ldots \mathrm{S}$ separation is again found with the larger basis set, and the angle $\Theta$ is found to be smaller, implying a coordination angle closer to perpendicular, and therefore a greater involvement of the $2 b_{1}$ non-bonding orbital of $\mathrm{H}_{2} \mathrm{~S}$ in the interaction, relative to the $5 a_{1}$ orbital. For the staggered conformer, the triple-zeta bases predict a longer van der Waals bond length than the corresponding double-zeta, but the basis sets containing diffuse functions suggest substantially shorter B...S distances. The $6-311++G$ and $6-311++G(d, p)$ basis sets also yield noticeably smaller $\Theta$ angles.
Our calculations for the $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ complex may now be compared with those of Ball ${ }^{5}$ and Jacox et al. ${ }^{4}$ Ball's calculations were all carried out at the RHF level, except for one performed with the MP2/6-311+G(d,p) combination, in which he failed correctly to predict the $\mathrm{C}_{\mathrm{s}}$ symmetry of the complex, through not using a sufficiently stringent convergence criterion. Our $6-311++G(d, p)$ structural parameters are mostly in qualitative agreement with his results, after allowing for the slightly different basis set, and the lower symmetry of Ball's structure.

He also neglected to consider a staggered conformer as a possibility. ${ }^{5}$ Jacox and her co-workers employed, in addition to the RHF and MP2 theoretical models, the QCISD and CCSD(T) theories, also with the $6-311+G(d, p)$ basis. ${ }^{4}$ This set of calculations did converge in the correct point group, with comparable structural results to ours and Ball's, ${ }^{5}$ but again a staggered conformer was not included.

In summary, the complex of boron trifluoride with water adopts exclusively the eclipsed conformation, but the preferred conformation for the complex with hydrogen sulphide is the staggered. We are not aware of any gas phase microwave studies on either of these complexes with which to compare our structural results. However, Rao et al. have investigated $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}^{21-23}$ and $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{~S}^{22-24}$ by means of both electron energy loss and ultraviolet photoelectron spectroscopy, and the symmetries of the complex molecular orbitals derived from these studies are consistent with a $\mathrm{C}_{\mathrm{s}}$ structure.

### 3.2. Interaction Energies

The computed interaction energies of the $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{~S}$ complexes which were found to be energy minima are presented in Table 2. Those structures for which it was not possible to distinguish between the eclipsed and staggered species are excluded. Our binding energies are substantially larger than the $40 \mathrm{~kJ} \mathrm{~mol}^{-1}$ determined by Ball, ${ }^{5}$ even though Ball's interaction energies were not corrected for either BSSE or zero-point energy differences. Other estimates of the binding energy are -144 kJ $\mathrm{mol}^{-123}$ and $-71.7 \mathrm{~kJ} \mathrm{~mol}{ }^{-125}$ but these calculations were performed with much smaller basis sets. Jacox et al. did not report the interaction energies. ${ }^{4}$ For staggered $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{~S}$, addition of polarization functions, e.g. $6-31 \mathrm{G}(\mathrm{d}, \mathrm{p})$ versus $6-31 \mathrm{G}$, led to a reduction in the strength of binding. Where all four triple-zeta basis sets predicted the same (staggered) conformer, inclusion of diffuse functions caused an increase and polarization functions a decrease in the energy of interaction. The binding energy of $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{~S}$ has been reported previously as $-22 \mathrm{~kJ} \mathrm{~mol}^{-1}{ }^{23}$ and $+384.3 \mathrm{~kJ} \mathrm{~mol}^{-1} .{ }^{25}$ Clearly the energy of interaction is very sensitive to the basis set employed. Insofar as mean values of this property are meaningful, our results indicate that eclipsed $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ is bound by about $70 \mathrm{~kJ} \mathrm{~mol}{ }^{-1}\left(60 \mathrm{~kJ} \mathrm{~mol}^{-1}\right.$ with zero-point energy correction), eclipsed $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{~S}$ by $12 \mathrm{~kJ} \mathrm{~mol}{ }^{-1}$ $\left(8 \mathrm{~kJ} \mathrm{~mol}^{-1}\right)$ and staggered $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{~S}$ by $10 \mathrm{~kJ} \mathrm{~mol}^{-1}\left(5 \mathrm{~kJ} \mathrm{~mol}^{-1}\right)$. These relative values for interaction of $\mathrm{BF}_{3}$ with a hard $\left(\mathrm{H}_{2} \mathrm{O}\right)$ and a soft $\left(\mathrm{H}_{2} \mathrm{~S}\right)$ base are quite consistent with chemical intuition.

Comparison of our computed fully-corrected interaction energy of the $\mathrm{BF}_{3}$ complex with $\mathrm{H}_{2} \mathrm{O}$ with those with other oxygen donor bases, $\mathrm{CO}_{2},{ }^{8} \mathrm{~N}_{2} \mathrm{O},{ }^{9} \mathrm{SO}_{2}{ }^{10}$ and $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{O}^{11}$ recalculated under the same conditions ${ }^{26}(-4.556,-3.450,-8.844$ and

Table 2 Interaction energies of some $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{~S}$ complexes, corrected for BSSE and for zero-point energy differences, computed with a variety of basis sets.

| Basis set | $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ |  | $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{~S}$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Eclipsed |  | Eclipsed |  | Staggered |  |
|  | a | b | a | b | a | b |
| 6-31G | - | - | - | - | -10.561 | -5.596 |
| 6-31++G | - | - | -14.291 | -9.128 | - | - |
| 6-31G(d,p) | -71.100 | -60.732 | - | - | -6.990 | -2.759 |
| $6-31++G(d, p)$ | -79.577 | -69.215 | -10.443 | -6.253 | - | - |
| 6-311G | - | - | - | - | -7.821 | -3.661 |
| 6-311++G | - | - | - | - | -16.619 | -11.418 |
| 6-311G(d,p) | -62.385 | -53.192 | - | - | -5.350 | -1.656 |
| $6-311++G(d, p)$ | -66.333 | -56.699 | - | - | -10.593 | -6.878 |

a, Corrected for BSSE only.
b, Corrected for BSSE and zero-point energy differences.

Table 3 Computed wavenumbers of the eclipsed ${ }^{11} \mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ complex.
$\left.\begin{array}{cclccc}\hline \text { Symmetry species } & \text { Mode } & \begin{array}{l}\text { Approximate } \\ \text { description }\end{array} & \begin{array}{c}6-311++\mathrm{G}(\mathrm{d}, \mathrm{p}) \\ (\text { this work })\end{array} & 4-31 \mathrm{G}(\text { ref. } 1) & \begin{array}{c}6-311+\mathrm{G}(\mathrm{d}, \mathrm{p}) \\ (\text { ref. } 4)\end{array} \\ \hline \mathrm{a}^{\prime} & & v_{\mathrm{s}}\left(\mathrm{H}_{2} \mathrm{O}\right) & 3818.0 & 3-311+\mathrm{G}(\mathrm{d}, \mathrm{p}) \\ (\text { ref. } 5)\end{array}\right]$
$-130.554 \mathrm{~kJ} \mathrm{~mol}^{-1}$, respectively), reveals a general trend of increasing interaction energy with increasing gas phase basicity ${ }^{27}$ and decreasing ionization energy. ${ }^{28}$

### 3.3. Vibrational Spectra

Since the structural and energetic results reported above indicate that, among the eight basis sets which we have examined, it is the $6-311++G(d, p)$ basis which yields the most consistent and reliable data, we will confine our discussion of the vibrational spectra to those derived using that basis set only. The performance of this basis set in reproducing the experimental wavenumbers of the ${ }^{11} \mathrm{BF}_{3}, \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{~S}$ monomers ${ }^{19,29-33}$ is recorded in the Supplementary Material, Table SM3.
The computed wavenumbers of ${ }^{11} \mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ derived using the $6-311++G(d, p)$ basis set are listed in Table 3, along with those determined earlier ${ }^{1,4,5}$. Discounting our early effort at the RHF level with a small basis set, ${ }^{1}$ our present $6-311++G(d, p)$ results are in good agreement with those of Jacox et al. ${ }^{4}$ and Ball. ${ }^{5}$ The wavenumbers determined experimentally in nitrogen, ${ }^{1}$ argon ${ }^{2,3}$ and neon ${ }^{4}$ matrices are listed in Table 4. This table indicates a number of mis-assignments in our preliminary analysis. ${ }^{1}$ The band at $1725 \mathrm{~cm}^{-1}$ is clearly at too high a wavenumber to be the $\mathrm{H}_{2} \mathrm{O}$ bending mode, $v_{2}$, although we cannot suggest an alternative interpretation. The band at $460 \mathrm{~cm}^{-1}$ must be assigned to the

Table 4 Experimental wavenumbers of the ${ }^{11} \mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ complex.

| Symmetry species | Mode | Wavenumber/ $\mathrm{cm}^{-1}$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathrm{N}_{2}{ }^{\text {a }}$ | $\mathrm{Ar}^{\text {b }}$ | $\mathrm{Ar}^{\text {c }}$ | $\mathrm{Ne}{ }^{\text {d }}$ |
| $\mathrm{a}^{\prime}$ | $\nu_{1}$ | 3590 |  | 3555.1 | 3548.7 |
|  | $\nu_{2}$ | 1725 |  |  |  |
|  | $v_{3}$ | 1225 | 1241 | $1283.9{ }^{\text {e }}$ | 1303.8 |
|  |  |  |  | 1251.9 |  |
|  | $\nu_{4}$ | 863 |  | 874.5 | 875.9 |
|  | $\nu_{5}$ | 625 |  | 654.9 |  |
|  | $v_{6}$ | 460 |  | $691.5^{\text {e }}$ |  |
|  |  |  |  | 664.0 |  |
|  | $v_{7}$ | 385 |  |  | 455.3 |
|  | $\nu_{8}$ |  |  |  |  |
|  | $\nu_{9}$ |  |  |  |  |
| a" | $v_{10}$ | 3660 |  | 3730.0 | 3712.5 |
|  | $\nu_{11}$ | 1240 | $1313{ }^{\text {e }}$ | $1314.6{ }^{\text {e }}$ | 1323.0 |
|  |  |  | 1285 | 1264.7 |  |
|  | $v_{12}$ | 818 |  | 851.5 |  |
|  | $\nu_{13}$ | 460 |  |  |  |
|  | $v_{14}$ |  |  |  |  |
|  | $v_{15}$ |  |  |  |  |

[^1]Table 5 Computed (using the $6-311++G(d, p)$ basis set) and experimental intramolecular wavenumber shifts of the $\mathrm{BF}_{3}$ and $\mathrm{H}_{2} \mathrm{O}$ fragments of the eclipsed ${ }^{11} \mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ complex.

| Fragment | Monomer mode | Complex mode | Wavenumber shift/ $\mathrm{cm}^{-1}$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Computed | Experimental |  |  |
|  |  |  |  | $\mathrm{N}_{2}{ }^{\text {a }}$ | $\mathrm{Ar}^{\text {b }}$ | $\mathrm{Ne}^{\text {c }}$ |
| $\mathrm{BF}_{3}$ | $v_{1}$ | $v_{4}$ | -39.3 |  |  |  |
|  | $v_{2}$ | $v_{6}$ | -90.2 | -28 |  |  |
|  | $v_{3}\left(\mathrm{a}^{\prime}\right)$ | $v_{3}$ | -112.3 | -215 | -209 | -124.5 |
|  | $v_{3}\left(\mathrm{a}^{\prime \prime}\right)$ | $\nu_{11}$ | -139.1 | -200 | -165 | -143.7 |
|  | $v_{4}\left(\mathrm{a}^{\prime}\right)$ | $v_{7}$ | -18.5 | -19 |  | -23.6 |
|  | $v_{4}\left(\mathrm{a}^{\prime \prime}\right)$ | $v_{13}$ | -19.4 | -19 |  |  |
| $\mathrm{H}_{2} \mathrm{O}$ | $\nu_{1}$ | $\nu_{1}$ | -66.5 | -45 |  |  |
|  | $\nu_{2}$ | $\nu_{2}$ | 3.0 |  |  |  |
|  | $\nu_{3}$ | $\nu_{10}$ | -72.4 | -67 |  |  |

${ }^{\mathrm{a}}$ Ref. 1; ${ }^{\mathrm{b}}$ Ref. 2; ${ }^{\mathrm{c}}$ Ref. 4.
two components of the antisymmetric $\mathrm{BF}_{3}$ bending vibration, $v_{7}$ and $v_{13}$, heavily overlapped. The $625 \mathrm{~cm}^{-1}$ band must therefore be the out-of-plane $\mathrm{BF}_{3}$ bending mode, $v_{6}$, while the band observed at $385 \mathrm{~cm}^{-1}$ must be assigned to one of the intermolecular modes, although no predicted mode appears sufficiently close to this observed band to be a credible candidate. The remaining assignments are in reasonable agreement with those reported earlier. ${ }^{2-4}$
It is the shifts of the monomer modes on complexation which provide the most characteristic computational measure of the strength of interaction, for comparison with experimental data. These shifts, for the $6-311++G(d, p)$ basis set, are presented in Table 5, for both the $\mathrm{BF}_{3}$ and $\mathrm{H}_{2} \mathrm{O}$ molecules, while the corresponding experimental shifts are also included. ${ }^{1,2,4}$ The two antisymmetric $\mathrm{BF}_{3}$ stretching modes consistently undergo the largest perturbations on complexation. The computed shifts are substantially smaller than the experimental ones, except those in neon. ${ }^{4}$ However, it is well known that ab initio calculations for isolated 1:1 (gas phase) complexes do not account for the strong matrix effects experienced by molecules trapped in, e.g. $\mathrm{N}_{2}$ and Ar. In neon matrices the perturbations are smaller, and agreement between the calculated and the experimental shifts is much improved. On the other hand, our calculated shift of $-90.2 \mathrm{~cm}^{-1}$ for the symmetric bending mode of the $\mathrm{BF}_{3}$ fragment is considerably larger than the experimental value in $\mathrm{N}_{2}$. Inspection of the forms of the normal modes, however, reveals that $v_{6}$ of $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ is not a pure $\mathrm{BF}_{3}$ bending vibration. As a result of the proximity of the $v_{5}$ geared libration ( $\mathrm{H}_{2} \mathrm{O}$ wagging) mode at $608.4 \mathrm{~cm}^{-1}$ (see Table 3), these two vibrations are strongly coupled with one another, and the out-of-plane bending also involves a large amplitude displacement of the $\mathrm{H}_{2} \mathrm{O}$ fragment. This coupling has the effect of lowering the wavenumber of $v_{6}$ and raising that of $v_{5}$, so that the vibration nominally assigned to the out-of-plane $\mathrm{BF}_{3}$ bending mode is artificially low, and its shift is exaggerated. All the calculated shifts are to the red, with the exception of that of the $\mathrm{H}_{2} \mathrm{O}$ bending vibration, which is typical of water acting as a Lewis base.
The corresponding calculated wavenumbers of ${ }^{11} \mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{~S}$, along with the experimental values for the two antisymmetric $\mathrm{BF}_{3}$ stretching motions, ${ }^{2}$ are given in Table 6. These wavenumbers lead to the computed and experimental shifts reported in Table 7. All the wavenumber shifts are to lower values, including that of the $\mathrm{H}_{2} \mathrm{~S}$ bending mode, in contrast to the $\mathrm{H}_{2} \mathrm{O}$ bending vibration in $\mathrm{BF}_{3} . \mathrm{H}_{2} \mathrm{O}$. This finding serves to emphasize the difference in the ways in which the electron donors are bound to the $\mathrm{BF}_{3}$ fragment. Again, the computed antisymmetric $\mathrm{BF}_{3}$

Table 6 Computed (using the $6-311++G(d, p)$ basis set) and experimental wavenumbers of the staggered ${ }^{11} \mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{~S}$ complex.

| Symmetry <br> species | Mode | Approximate <br> description | Computed | Experimental ${ }^{\text {a }}$ |
| :---: | :---: | :--- | ---: | :---: |
| $\mathrm{a}^{\prime}$ | $v_{1}$ | $v_{\mathrm{s}}\left(\mathrm{H}_{2} \mathrm{~S}\right)$ | 2808.7 |  |
|  | $v_{2}$ | $v_{\mathrm{a}}\left(\mathrm{BF}_{3}\right)$ | 1407.2 | 1321 |
|  | $v_{3}$ | $\delta\left(\mathrm{H}_{2} \mathrm{~S}\right)$ | 1199.8 |  |
|  | $v_{4}$ | $v_{\mathrm{s}}\left(\mathrm{BF}_{3}\right)$ | 858.4 |  |
|  | $v_{5}$ | $\left.\delta_{\mathrm{s}} \mathrm{BF}_{3}\right)$ | 620.3 |  |
|  | $v_{6}$ | $\delta_{\mathrm{a}}\left(\mathrm{BF}_{3}\right)$ | 470.4 |  |
|  | $v_{7}$ | geared libration | 238.9 |  |
|  | $v_{8}$ | $v(\mathrm{~B} \ldots \mathrm{~S})$ | 92.0 |  |
|  | $v_{9}$ | antigeared libration | 81.2 |  |
|  | $v_{10}$ | $v_{\mathrm{a}}\left(\mathrm{H}_{2} \mathrm{~S}\right)$ | 2828.3 |  |
|  | $v_{11}$ | $v_{\mathrm{a}}\left(\mathrm{BF}_{3}\right)$ | 1417.3 | 1270 |
|  | $v_{12}$ | $\delta_{\mathrm{a}}\left(\mathrm{BF}_{3}\right)$ | 474.2 |  |
|  | $v_{13}$ | geared libration | 261.1 |  |
|  | $v_{14}$ | antigeared libration | 91.3 |  |
|  | $v_{15}$ | $\mathrm{~B} \ldots \mathrm{~S}$ torsion | 45.2 |  |

${ }^{\text {a }}$ In Ar; ref. 2.
stretching shifts substantially underestimate the experimental ones, ${ }^{2}$ but this is simply due to the neglect of the perturbing effect of the argon matrix in the theoretical calculations.

Table 7 Computed (using the $6-311++G(d, p)$ basis set) and experimental intramolecular wavenumber shifts of the $\mathrm{BF}_{3}$ and $\mathrm{H}_{2} \mathrm{~S}$ fragments of the staggered ${ }^{11} \mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{~S}$ complex.

| Fragment | Monomer mode | Complex mode | Wavenumber shift/ $\mathrm{cm}^{-1}$ |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  | Computed | Experimental ${ }^{\text {a }}$ |
| $\mathrm{BF}_{3}$ | $v_{1}$ | $\nu_{4}$ | -15.5 |  |
|  | $\nu_{2}$ | $\nu_{5}$ | -75.0 |  |
|  | $\nu_{3}\left(\mathrm{a}^{\prime}\right)$ | $\nu_{2}$ | -26.8 | -129 |
|  | $v_{3}\left(\mathrm{a}^{\prime \prime}\right)$ | $\nu_{11}$ | -16.7 | -180 |
|  | $v_{4}\left(\mathrm{a}^{\prime}\right)$ | $v_{6}$ | -4.4 |  |
|  | $v_{4}\left(\mathrm{a}^{\prime \prime}\right)$ | $v_{12}$ | -0.6 |  |
| $\mathrm{H}_{2} \mathrm{~S}$ | $\nu_{1}$ | $v_{1}$ | -8.2 |  |
|  | $v_{2}$ | $v_{3}$ | -33.5 |  |
|  | $v_{3}$ | $\nu_{10}$ | -7.8 |  |

[^2]
## 4. Conclusions

The preferred conformation calculated for the $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ complex is the eclipsed, while that for the $\mathrm{H}_{2} \mathrm{~S}$ analogue is the staggered. The order of the energies of interaction of the complexes of $\mathrm{BF}_{3}$ with the hard oxygen base $\mathrm{H}_{2} \mathrm{O}$ and the soft sulphur base $\mathrm{H}_{2} \mathrm{~S}$ is in accordance with predictions based on conventional wisdom. The computed vibrational spectrum of $\mathrm{BF}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ correlates, with the reservations noted above, with those observed in nitrogen, argon and neon matrices, and the computations have assisted in the re-assignment of a number of the observed bands.

## Acknowledgements

This material is based upon work supported by the National Research Foundation under Grant Number 2053648. Any opinion, findings and conclusions or recommendations expressed in this material are those of the authors and do not necessarily reflect the views of the National Research Foundation. The authors also acknowledge the financial assistance of the University of KwaZulu-Natal Research Fund, through its support of the Centre for Theoretical and Computational Chemistry, and the expert technical assistance of Mr Kishore Singh.

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[^1]:    ${ }^{\mathrm{a}}$ Ref. 1; ${ }^{\mathrm{b}}$ Ref. 2; ${ }^{\mathrm{c}}$ Ref. 3; ${ }^{\mathrm{d}}$ Ref. 4; ${ }^{\mathrm{e}}$ Bands due to ${ }^{10} \mathrm{BF}_{3} . \mathrm{H}_{2} \mathrm{O}$.

[^2]:    ${ }^{\mathrm{a}}$ In Ar; ref. 2.

