SIMULATION AND COMPARISON OF EQUILIBRIUM AND NONEQUILIBRIUM STAGE MODELS OF REACTIVE DISTILLATION

Nurelegne Tefera Department of Chemical Engineering Addis Ababa University

ABSTRACT

In the present study, two distinctly different approaches are followed for modeling of reactive distillation column, the equilibrium stage model and the nonequilibrium stage model. These models are simulated with a computer code developed in the present study using MATLAB programming. In the equilibrium stage models, the vapor and liquid phases are assumed to be in equilibrium and allowance is made for finite reaction rates, where as in the nonequilibrium stage models simultaneous mass transfer and reaction rates are considered. These simulated model results are validated from the experimental data reported in the literature [Jacob and Krishna, 1993]. The simulated results of equilibrium and nonequilibrium models are compared for concentration, temperature and reaction rate profiles in a reactive distillation column for Methyl Tert Butyle Ether (MTBE) production. Both the models show similar trend for the concentration, temperature and reaction rate profiles but the nonequilibrium model predictions are higher and closer to the experimental values reported in the literature [Jacob and Krishna, 1993].

INTRODUCTION

The reactive distillation columns are gaining importance for the synthesis of reversible or consecutive chemical reactions for exceeding the equilibrium conversion and reducing the rate of formation of byproducts. Both the reaction and separation steps are carried out in a single unit, where as in a conventional process the reaction and separation steps are carried out separately. A typical reactive distillation column is divided in to reactive and non-reactive sections. The reactive section is located in the middle of the two non-reactive sections namely rectifying and stripping sections. In a reactive section, the reactants are converted in to products and in the non-reactive sections, the products are separated by means of distillation.

The recent works on reactive distillation involve synthesis of reversible reactions exceeding more than equilibrium conversion and the analysis of the reactive distillation process using different modeling approaches namely equilibrium and nonequilibrium models [1-8]. Reactive distillation process involving reactive separation or multicomponent heterogeneously catalyzed processes are further modeled using nonequilibrium cell models [4] or dusty fluid model [5]. Hence, the design and operation issues for reactive distillation systems are considerably more complex than those involved for conventional reactors or distillation columns. The introduction of an on-line separation function within the reaction zone leads to complex interactions between vapor-liquid equilibrium, vapor-liquid mass transfer, intra-catalyst diffusion and chemical kinetics.

In the present study, an attempt has been made to understand the complex system and to simulate equilibrium and nonequilibrium models for the production of Methyl Tert Butyl Ether (MTBE) in a reactive distillation column, developing a computer code using MATLAB programming. It is also aimed to use simultaneous correction method based on Naphtali-Sandholm together with *Newton's* method for the simulation of nonequilibrium model equations, and the Newton's method alone for those set of nonequilibrium equations, where there is a singularity problem using the Naphtali-Sandholm procedure.

NON-EQUILIBRIUM MODEL

A typical setup considered for Reactive distillation column [6] and the schematic representation of the nonequilibrium model are shown in Fig. 1 &2 respectively. The nonequilibrium model used in the present study for reactive distillation considers both reaction rates and mass transfer fluxes. It is assumed that bulk phase of vapor and liquid are well mixed and the mass transfer resistances are located in films near the interface. A penetration model description is used for predicting mass transfer rates. A chemical

reaction term is incorporated in the model equations for generic stage k (tray or packing) and component i. The model uses the height of packing and treats the column as a continuous element.





distillation column for ether



Figure 2 Nonequilibrium stage model for pseudo homogeneous reaction in the liquid phase

The model formulation can deal with any number of reactions and the component molar balance for vapor (V) and liquid phases (L) are:

$$\begin{pmatrix} \left(1 + r_{j}^{\nu}\right) V_{j} y_{j,i} - V_{j+1} y_{j+1,i} - f_{j,i}^{\nu} + \mathbf{N}_{j,i}^{\nu} = 0 \quad (1) \\ \left(1 + r_{j}^{L}\right) L_{j} x_{j,i} - L_{j-1} x_{j-1,i} - f_{j,i}^{L} \\ - \mathbf{N}_{j,i}^{L} - \varepsilon_{j} \sum_{m=1}^{n} v_{m,i} R_{m,j} = 0$$

$$(2)$$

Overall phase material balances are obtained by adding the above equations over i=1 to i=C, where C is the number of components, x is the mole fraction in liquid phase and y is the mole fraction in vapor phase, N is the mass transfer rate and R is the reaction rate and j represents the stage number.

Journal of EEA, Vol. 23, 2006

In the material balance equations given above r_j is the ratio of side stream flow rate (S) to inter stage flow rate as

$$r_j^{\nu} = \frac{S_j^{\nu}}{V_i} \quad and \quad r_j^{L} = \frac{S_j^{L}}{L_i} \quad (3)$$

Summations of the component molar balance equations are also expressed for both control volumes.

$$V_{j+1} - V_j + F_j^{\nu} - \sum_{i=1}^{C} N_{j,i} = 0$$

$$L_{j-1} - L_j + F_j^{L} + \sum_{i=1}^{C} N_{j,i}$$

$$+ \sum_{i=1}^{C} \sum_{m=1}^{r} v_{m,i} R_{m,j} \varepsilon_j = 0$$
(5)

The feed entering the column at any inlet is treated as follows: the vapor portion of this feed enters the stage above and the liquid portion of the feed enters the tray below. The feed flow rate of component *i* in the vapor phase to stage *j* is $Z_{j,i}^{\nu}F_{j,i}^{\nu}$ and the feed flow rate of component *i* in the liquid phase to stage *j* is $Z_{j,i}^{L}F_{j,i}^{L}$, where $Z_{j,i}^{\nu}$ and $Z_{j,i}^{L}$ are the corresponding mole fraction of the feed streams. The Non equilibrium model uses two sets of rate equations (*R*) for each stage

$$\mathbf{R}_{j,i}^{\nu} = \mathbf{N}_{j,i} - \mathbf{N}_{j,i}^{\nu} = 0 \tag{6}$$

$$\mathbf{R}_{j,i}^{L} = \mathbf{N}_{j,i} - \mathbf{N}_{j,j}^{L} = 0 \tag{7}$$

Where N_{ij} is the mass transfer rate of component *i* on stage *j*.

The general forms for component mass transfer rates across the vapor and liquid films is computed from a diffusive and a convective (bulk- flow) contribution with

$$N_{j,i}^{\nu} = a_j^{\prime} J_{j,i}^{\nu} + \gamma_{j,i} N$$
(8)

$$\mathbf{N}_{j,i}^{L} = a_{j}^{I} \mathbf{J}_{j,i}^{L} + x_{j,i} \mathbf{N}_{T,j}$$
(9)

Where a_j^I : total interfacial area for the stage j and $N_{T,j}$ is the total rate on stage $j \left(N_{T_j} = \sum_{i=1}^{C} N_{ij}\right)$. The diffusive molar fluxes J are given by (in matrix form):

$$\left(\mathbf{J}^{\nu}\right) = C_{\iota}^{\nu} \left[\boldsymbol{\kappa}^{\nu}\right] (\overline{\boldsymbol{y}^{\nu} - \boldsymbol{y}^{\ell}})$$
 (10)

$$\left(\mathbf{J}^{L}\right) = C_{t}^{L}\left[\mathbf{\kappa}^{L}\right]\left(\overline{\mathbf{x}^{T} - \mathbf{x}^{L}}\right)$$
(11)

Simulation and Comparison of Equilibrium and Nonequilibrium

Where the $(y^{\nu} - y^{\tau})$ and $(x^{\tau} - x^{\tau})$ are the average mole fraction differences between the bulk and the interface mole fractions. The calculation of the average mole fraction differences depends on the selected flow model. The matrices of Maxwell-Stefan mass transfer coefficients, $[\kappa]$, are calculated for the vapor phase as

$$\begin{bmatrix} \mathbf{\kappa}^{t'} \end{bmatrix} = \begin{bmatrix} \mathfrak{R}^{t'} \end{bmatrix}^{-1} \tag{12}$$

for a the non-ideal liquid solution as

$$\left[\mathbf{\kappa}^{L}\right] = \left[\mathfrak{R}^{L}\right]^{-1} \left[\mathbf{\Gamma}^{L}\right]$$
(13)

Where $[\Gamma^2]$ is a $(C-1)\times(C-1)$ matrix of thermodynamic factors that corrects for non-ideality, which often is a necessary correction for the liquid phase. The thermodynamic factor is required because it is generally accepted that the fundamental driving force for diffusion is the gradient of the Chemical potential rather than the mole fraction or concentration gradient. The $(C-1)\times(C-1)$ Rate Matrix [\Re] is a matrix of mass transfer resistances

calculated from the following formulae:

$$\Re_{i,i}^{\nu} = \frac{y_i}{k_{i,C}^{\nu}} + \sum_{k=1,k\neq i}^{C} \frac{y_k}{k_{i,k}^{\nu}}$$
(14)

$$\Re_{i,j}^{\nu} = -y_i \left(\frac{1}{k_{i,j}^{\nu}} - \frac{1}{k_{i,c}^{\nu}} \right)$$
(15)

$$\Re_{i,i}^{L} = \frac{x_{i}}{k_{i,C}^{L}} + \sum_{k=1,k\neq i}^{C} \frac{x_{k}}{k_{i,k}^{L}}$$
(16)

$$\Re_{i,j}^{L} = -x_i \left(\frac{1}{k_{i,j}^{L}} - \frac{1}{k_{i,C}^{L}} \right)$$
(17)

Where $k_{i,j}^{\nu}$ and $k_{i,j}^{L}$ are binary pair mass transfer coefficient for each phases. Eqs. (14) to (17) are the Maxwell-Stefan equations for mass transfer in multicomponent systems. Mass transfer coefficient is calculated first calculating the matrix function inverted binary diffusion coefficients, *B*.

$$B_{i,i}^{\nu} = \frac{\hat{y}_i}{\mathbf{D}_{i,C}^{\nu}} + \sum_{k=1,k=i}^{C} \frac{\hat{y}_k}{\mathbf{D}_{i,k}^{\nu}}$$
(18)

$$B_{i,j}^{\nu} = -y_i \left(\frac{1}{\mathbf{D}_{i,j}^{\nu}} - \frac{1}{\mathbf{D}_{i,c}^{\nu}} \right)$$
(19)

$$B_{i,l}^{L} = \frac{x_i}{\mathbf{D}_{i,c}^{L}} + \sum_{k=1,k=l}^{C} \frac{x_k}{\mathbf{D}_{i,k}^{L}}$$
(20)

$$\mathsf{B}_{i,j}^{L} = -x_i \left(\frac{1}{\mathbf{D}_{i,j}^{L}} - \frac{1}{\mathbf{D}_{i,C}^{L}} \right)$$
(21)

Where $\mathbf{p}_{i,j}$ is the binary Maxwell-Stefan diffusion coefficient. The Fickian diffusion coefficient matrix [D] is the inverse of the inverted binary diffusion coefficient [B], $\{D\} = [B]^{-1}\}$. Matrices [D] and [B] are square matrices of size (C-1), where C is the number of components. Therefore, the required correlations for mass transfer coefficients for components1 to C-1 are expressed using the penetration theory.

The Energy balance equations on stage *j* are written for each phase as follows:

$$E_{j}^{\nu} = (1 + r_{j}^{\nu})V_{j}H_{j}^{\nu} - V_{j+1}H_{j+1}^{\nu}$$

$$-F_{j}^{\nu}H_{j}^{\nu \mu} + Q_{j}^{\nu} + e_{j}^{\nu} = 0$$

$$E_{j}^{\perp} = (1 + r_{j}^{\perp})L_{j}H_{j}^{\perp} - L_{j-1}H_{j-1}^{\perp}$$

$$-F_{j}^{\perp}H_{j}^{\perp \mu} + Q_{j}^{\perp} - e_{j}^{\perp} = 0$$
(23)

The last term in Eqs. (22) and (23), H is the enthalpy, Q is the amount of heat added or removed from the system and e_j represents the energy transfer rates for the vapor and liquid phase which are defined by:

$$e_{j}^{\nu} = a_{j}^{I} \alpha^{\nu} (T^{\nu} - T^{I}) + \sum_{i=1}^{C} \mathbf{N}_{i,j}^{\nu} \overline{H}_{i,j}^{\nu}$$
(24)

$$e_j^L = a_j^I \alpha^L (T^I - \tau^L) + \sum_{i=1}^C \mathbf{N}_{i,j}^L \overline{H}_{i,j}^L$$
(25)

Where $\overline{H}_{i,j}$ are the partial molar enthalpies of component *i* on stage *j*. There is also a continuity of the energy fluxes across the vapor-liquid interface that gives the interface energy balance:

$$E_{j}^{L} = e_{j}^{V} - e_{j}^{L} = 0 (26)$$

Where α^{v} and α^{L} are the vapor and liquid heat transfer coefficients respectively, and T^{V} , T^{I} , and T^{L} are the bulk vapor, interface and bulk liquid temperatures. For the calculation of the vapor heat transfer coefficients the Chilton-Colburn analogy between mass and heat transfer is used [9].

Journal of EEA, Vol. 23, 2006

9

Phase equilibrium is assumed to exist only at the interface with the mole fractions in both phases related by:

$$Q_{j,i}^{I} = \mathbf{K}_{j,i} \mathbf{x}_{j,i}^{I} - \mathbf{y}_{j,i}^{I} = 0$$
 (27)

Where $K_{i,j}$ is the vapor liquid equilibrium ratio for component i, on stage j.

The mole fractions must sum to unity in each phase:

$$S_{j}^{\nu} = \sum_{i=1}^{c} y_{j,i} - 1 = S_{j}^{L} = \sum_{i=1}^{c} x_{j,i} - 1 = 0$$
(28)

as well as at the interface:

$$S_{j}^{LI} = S_{j}^{VI} = \sum_{i=1}^{C} y_{j,i}^{l} - 1 = \sum_{i=1}^{C} x_{j,i}^{l} - 1 = 0$$
(29)

For each stage, the establishment of a liquid hold up on the stage is considered through use of the hvdraulic equation for stage pressure drop:

$$\Delta P_i = P_{i+1} - P_i \tag{30}$$

Where $P_j = P_j^{\nu} = P_j^{\perp}$ and ΔP_j is the vapor pressure drop from stage *j*+1 to stage *j*.

The vapor and liquid phases in reactive distillation column are highly nonideal system due to the complex interactions between reaction and distillation. The Poynting correlation is used to calculate the vapor-liquid equilibrium constant. The vapor-liquid equilibrium constant \mathbf{K}_i for component *i*, in the nonideal solution of systems, is expressed as [8,9]

$$K_{i} = \gamma_{i} \frac{\phi_{i}^{\circ}}{\phi_{i}^{\circ}} \frac{p_{i}^{\circ}}{P} \exp\left[\frac{\upsilon_{i}(P - P_{i}^{\circ})}{RT}\right]$$
(31)

Where γ_i is the liquid activity coefficient, ϕ_i° and ϕ_i° the vapor fugacity in pure and mixture state respectively, P_i° the Antoine vapor pressure, D_i the molar volume and P is the total pressure of the system [4]. For the description of liquid phase and gas phase interactions, the Wilson equation model [1] is used while gas phase interactions are modeled using the well known Peng-Robinson equation [10]. These models are used to calculate liquid activity coefficient γ_i and the vapor fugacity ϕ_i° (and ϕ_i°) respectively.

These set of nonequilibrium model equations are solved using simultaneous correction method based on Naphtali-Sandholm together with *Newton's* method.

Journal of EEA, Vol. 23, 2006

RESULT AND DISCUSSION

The column configuration chosen for the simulations is shown in Fig. 3. This configuration is reported by Jacobs and Krishna [6] for reactive distillation column and many authors have used the same configuration for the standardize of the simulation results. The same configuration is also used in the present study to standardize the computer code developed using MATLAB programming for simulation of equilibrium and nonequilibrium models. In the present study, we have considered the reactive distillation process for Methyl tert-butyl (MTBE) production. Thermodynamic ether parameters, transport parameters and reaction kinetics for MTBE production are taken from the literature[6,9,10 and11].

The synthesis of MTBE is selected because it is an exothermic and thermodynamically equilibrium limited process. The difficulties are the existence of minimum boiling azeotropes between MTBEmethanol, isobutene-methanol and n-butanemethanol and the separation between n-butane and isobutene, which have close boiling points. The either (MTBE) is derived from isobutene and methanol is blended in gasoline, to increase the octane number and to decrease carbon monoxide emission. The synthesis of MTBE from methanol and isobutene is a reversible exothermic reaction and is catalyzed by Amberlyst 15 or similar ion exchange resin catalyst. The forward reaction is first order with respect to the isobutene concentration and zero order with respect to the methanol concentration. The main side reaction is the dimerization of isobutene to diisobutene and the hydration of isobutene to TBA (tert butyl alcohol). Molar ratio of methanol to isobutene should be higher than 0.8 at each stage to avoid the side reactions.

The Reactive Distillation column considered for simulation consists of 17 stages including a total condenser and partial reboiler. The stages are numbered 1 to 17 from the condenser down to the reboiler Reactive stages are located in the middle of the column from stage 4 down to stage 11 with Amberlyst 15 ion exchange resin catalyst. The column has also nonreactive sections, a rectification zone (stage 2 to 3) where the inerts are separated, and a stripping zone (stage 12 to16) where the MTBE product is purified. The column has two feed streams: a methanol feed and a mixed butene feed (n-butane and isobutene). A small stoichiometric excess of

10

methanol is used. The methanol feed stage location is varied between stage 2 and stage 16 to study the effect of feed location on MTBE production. The mixed butene feed contains a mixture of isobutene. which is reactive, and *n*-butane, which is nonreactive or inerts are fed at a stage 11. For standardization the bottom products flow rate is taken as 197 mol/sec, reflux ratio is fixed at 7 and Amberlyst 15 ion exchange resin catalyst loading is taken as 1000kgs/stage from the literature [6]. The reactive distillation column simulation is carried out allowing the variation in feed flow rate, feed location using a user friendly computer code developed with MATLAB programming. The standard values reported in the literature [6] for the production of MTBE in a reactive distillation using number of stages, catalyst loading, flow rates of the phase and reflux ratio are considered for simulation validation as well as model comparison purpose.



Figure 3 Configuration of the MTBE synthesis column

THORE I THREADER OF STREAMEROFF FOREIG	Table	1	1	Va	lidation	of	simu	lation	results
--	-------	---	---	----	----------	----	------	--------	---------

Validation of Simulation Results

Computer code developed in the present study using MATLAB programming for the simulation of equilibrium and nonequilibrium models are validated using experimental data reported in literature [6] for the reactive distillation column. Table 1 shows the comparison between experimental data and the simulation results in the present study for equilibrium and nonequilibrium models. It is seen from the table 1 that the simulation results are in good agreement with the literature data.

Simulation of Concentration Profiles

The simulated concentration profiles of the reactive distillation column using the equilibrium and nonequilibrium modelss are shown in Figs. 4,5 and 6. The vapor phase concentration profile using equilibrium model is shown in figure 4a. The inert component n-butane is observed to be -the predominant component in the vapor phase in the rectifying section and reactive section of the column. High mole fractions of methanol and isobutene are achieved at the bottom part of the reactive section of the column. The liquid phase concentration profile of the components isobutene, thanol, MTBE and the inert n-butane are shown in figure 4b for equilibrium model. In the reaction zone from stages 4 to 11 isobutene and methanol are consumed, and maximum

	Jacobs and	Krishna [1]	Present study simulation results							
Component			Equilibriu	m model	Nonequilibrium model					
	Flow rate [mol/s]									
	Distillate	Bottoms	Distillate	Bottoms	Distillate	Bottoms				
isobutene	7.27	1,31	6.0344	0.2157	7.05556	0.2756				
methanol	28.32	0.31	24.6476	0.0006	25.8858	0.0365				
MTBE	0.12	186.74	0.2594	190.919	0.21747	190.677				
n-butane	344.92	8,64	349,688	5,8647	347.471	6.01125				
Total	380.63	197	380.63	197	380.63	197				

mole fractions of methanol and isobutene are observed at the feed locations. The liquid composition profiles show that the liquid is dominated by n-butane from top stage 1 to stage 12, thus drastically reducing the rate of reaction. In the stripping section, the liquid quickly becomes richer in MTBE as the mole fraction of the other components decrease because of increasing temperature. In the rectifying section of the reactive , distillation column the concentration of MTBE decreases. In the stripping zone, methanol, isobutene and the inert are being separated, resulting in a high concentration of MTBE in the bottoms and high mole fraction of MTBE is obtained in the liquid phase.



Figure 4 Concentration profiles using equilibrium model for (a) Vapor Phase (b) Liquid Phase

Figure 5 a shows the component mole fraction profiles for the bulk vapor phase obtained using the nonequilibrium model. The predominant component in bulk vapor phase is n-butane. The unreacted methanol is observed in the vapor phase. This is due to its nonideality that, it imposes to the system. Methanol is found more concentrated on the upper part of the reactive distillation column and less in the lower part of the column. High concentrations of isobutene are observed at the reaction and separation section of the column in the vapor phase and the Isobutene concentration decreases outside the reaction section of the reactive distillation column in the liquid phase. The drop in isobutene concentration outside the reaction section in the liquid phase is due to equilibrium limitation between the liquid and vapor phase, and bottom of the section is more predominant with MTBE and the top section is with methanol. The higher concentrations of isobutene in both the reactive and non reactive sections in the vapor phases may need further study to explain this behavior. A sharp increase of MTBE concentration is observed in the stripping section reaching maximum at the last stage (reboiler). Similar trend is observed for liquid phase concentration profiles shown in Fig. 5b. The concentration of MTBE decreases in the rectifying section and increases in the stripping section.



Figure 5 Concentration profiles using nonequilibrium model for (a) Vapor Phase (b) Liquid Phase

Comparison of Concentration Profiles

Figure 6 shows the comparison between equilibrium and nonequilbrium models for the mole fraction of MTBE in the liquid phase. Both the model simulation results give similar trends. In the reactive and stripping section higher mole fraction of MTBE is obtained by nonequilibrium model than by equilibrium model. The observed differences among the profiles are due to direct account of interface heat and mass transfer in nonequilibrium model for more MTBE production.



Figure 6 Comparison of concentration profile of MTBE for equilibrium and non-equilibrium model simulations.

Figure 7 shows the composition profile for isobutene (IB), methanol (MeOH), in the liquid phase of both equilibrium and nonequilibrium models. The concentration profile of these reactants resulted from

equilibrium model shows a maximum concentration at their respective feed stage and then decrease as we go away either up or down from that stage. Whereas the profiles obtained by nonequilibrium model shows that concentrations are high in reactive section of the column



Figure 7 Comparison of concentration profile of reactants for equilibrium and nonequilibrium model simulations for IBand MeOH.

Simulation of Temperature Profiles

The simulated temperature profiles of the reactive distillation column obtained from both the models are shown in Figs. (8a) and (8b). A smooth temperature profile is observed with equilibrium model Fig. (8a) for vapor phase showing lower temperature in the rectifying section and gradually increasing to a maximum value in the stripping section. As the reaction equilibrium constant increases exponentially

with decreasing temperature, the equilibrium is shifted toward MTBE in the reaction zone, located at the middle of the column from stages 4 to 11. The larger temperatures in the bottom are due to the presence of MTBE, which has a significantly higher molecular weight and higher boiling temperature. Simulated temperature profiles obtained using nonequilibrium model are shown in Fig. 8b for bulk liquid temperature, bulk vapor temperature and for vapor-liquid interphase. It is seen from the figure that the bulk vapor temperatures are higher than the bulk liquid temperatures, and interphase temperatures are in between approaching the theoretical behavior.

Simulation of Reaction Rate Profiles

The simulated results for the rate of formation of MTBE in the reaction zone is shown in figure 10 for both the models. The actants methanol and isobutene and n-butane mixture are introduced on stage 10 and stage 11 respectively. It is seen from the figure that there is no formation of MTBE in the non-reactive sections. It is also observed that the reaction rate increases starting from stage 4 to stage 10 and reaches maximum at stage 11 and shows that the forward reaction dominates on every stage of the reactive section.



Figure 8 Temperature profiles with (a) equilibrium model and (b) nonequilibrium model

Comparison of Temperature Profiles

A comparison between the equilibrium and nonequilibrium models for the prediction of temperature profile is show in Fig. 9 for the bulk vapor and bulk liquid pha. It is observed that the stage temperature profile of equilibrium model is identical with the bulk liquid temperative of the nonequilibrium model. It is also seen from the figure that the bulk vapor temperatures of the nonequilibrium model is higher than the equilibrium model stage temperature. This is because therma¹ equilibrium assumption of the equilibrium model forces the liquid and vapor leaving a stage to have the same temperature but in reality heat transfer between the two phases is limited [6].





nonequilibrium

Comparison of Reaction Rate Profiles

The rate of reaction profiles obtained for the models are compared in Fig. 11. The reaction rate profile for equilibrium model is smooth compared to the nonequilibrium model simulation. The instability of the reaction rate profile is mainly due to the complex



Figure 10 Reaction rate of formation of MTBE with (a) EQ and (b) NEQ Models



Figure 11 Comparison of reaction rate profiles of formation of MTBE using equilibrium and nonequilibrium models.

Sensitivity Analysis

The sensitivity analysis have been conducted for the influences of methanol feed stage location and reflux ratio on the isobutene conversion. The feed ratios and concentrations are not considered because if the molar ratio of methanol to isobutene is lower than 0.8 at each stage, the main side reactions are the

dimerization of isobutene to diisobutene and the hydration of isobutene to tert-butyl-alcohol(TBA). The molar ratios of the feed methanol to isobutene was maintained above 0.8 taking a small excess of stoichiometric concentrations of methanol.

interaction of reaction and separation process together with the nonideality of the system that are

directly considered on developing the nonequilibrium

stage model [6]. The higher reaction rate for

higher temperature of the bulk phase with the

relaxation of the thermal equilibrium

model may be attributed to the

Comparison of Isobutene Conversion: Effect of Methanol Feed Location

A series of simulation runs were carried out with varying methanol feed stage location from stage 2 to 16. First the column temperature and concentration profile were calculated with the methanol feed point located at stage 2. Then the values obtained from this simulation were used as initial values for the calculations with the methanol feed point located at stage 3 using the same operating and feed conditions as in the previous simulation. The concentration and temperature profile thus obtained were used for the simulation with the methanol feed point at stage 4 and so on until stage 16.

The simulation results for isobutene conversion using the equilibrium and nonequilibrium models are shown in Fig. 12. The difference in isobutene conversion between the models with methanol feed location is small in the rectifying and reactive sections. Moving the methanol feed from stage 11 to

stage 12 in the stripping section, the isobutene conversion drops to a lower value with the equilibrium model where as the drop with nonequilibrium model is much smaller. This is due to introduction of mass transfer resistance in the nonequilibrium model and also the existence of methanol in the vapor form in the stripping section.



Figure 12 Comparison of Isobutene conversion with methanol feed location with the equilibrium and nonequilibrium models.

Comparison of Isobutene Conversion: Effect of Reflux Ratio

The effect of the reflux ratio, R on the isobutene conversion in the reactive distillation column was determined by varying the reflux ratio from 1 to 10. This ratio is chosen because no significant variation in the conversion of isobutene is observed beyond 10 and the conversion lowers below 1. For each value of reflux ratio the steady-state column concentration and temperature profiles were calculated. The simulated results of isobutene conversion with reflux ratio is shown in Fig. 13 for both the models. It is observed from the figure that the conversions of isobutene increases with increase in reflux ratio up to 4.5 and becomes independent for further rise in reflux ratio.



Figure 13 Comparison of isobutene conversion with reflux ratio for equilibrium and nonequilibrium models.

CONCLUSIONS

Reactive Distillation is an attractive alternative to the classical combination of reactors and separators. The simulation studies are carried out using the equilibrium and nonequilibrium models for the MTBE system using the computer code developed in the present study with MATLAB programming. Both the equilibrium and nonequilibrium models show similar trend for concentration, temperature and reaction rate profiles in the reactive and separation sections. The MTBE concentration, the bulk vapor temperatures and reaction rates are higher with nonequilibrium model compared to equilibrium model. This is due to incorporation of reaction rates and mass transfer flux in the nonequilibrium models. The column operating performance depends on feed location, and reflux ratio. The drop in isobutene conversion with nonequilibrium model prediction is much smaller than the equilibrium model in the stripping section. Introduction of methanol feed in the stripping section is supposed to give higher conversion because of the nature of the feed, which is well predicted by the nonequilibrium model demonstrating the superiority over equilibrium modeling approach closer to the experimental data reported in the literature [6].

REFERENCES

- Eldarsi.H. and Douglas.P.L., Methyl-Tert-Butyl-Ether catalytic distillation column, part I: multiple steady states, *Trans IChemE*, Vol 76, Part A, 509-516, 1998.
- [2] Gani.R, Jepsen.T.S. and Pérez-Cisneros.E.S., A generalized reactive separation unit model. modelling and simulation aspects, *Computers Chem. Engng*, Vol.22, S363-S370, 1998.
- [3] Higler, A., Krishna.R., Ellenberger, J. and Taylor R., Counter-current operation of of a structured catalytically packed bed reactor: liquid phase mixing and mass transfer. *Chem. Eng. Sci.*, Vol54,5145-5152, 1999.
- [4] Higler, A., Krishna, R. and Taylor R., A nonequilibrium cell model for multicomponent(reactive) separation processes *AIChE.J*, Vol45,2357-2363, 1999.
- [5] Higler, A., Krishna R. and Taylor R., Nonequilibrium modeling of reactive distillation: A dusty fluid model for heterogeneously catalyzed processes. *Ind. Eng. Chem. Res.* Vol39, 1596-1607, 2000.

- [6] Jacobs.R. and Krishna.R., Multiple solutions in reactive distillation for methyl tert-butyl ether synthesis, *Ind. Eng. Chem. Res.*, Vol32, 1706-1709, 1993.
- [7] Kreul, L,U., Gorak, A. and Barton, P, I., Modelling of homogeneous reactive separation processes in packed columns., *Chem. Eng. Sci.*, Vol54, 19-25, 1999.
- [8] Xu, X., Zheng, Y. and Zeng, G., Kinetics and effectiveness of catalyst for synthesis of Methyl-Tert-Butyl-Ether in catalytic distillation. *Ind. Eng. Chem. Res.*, Vol34, 2232-2231, 1995.
- [9] Reid.R.C., Prausnitz J M., and Poling, B.M., The properties of gases and liquids, New York ,McGraw-Hill, 1999.
- [10] Smith.J.M., Van Ness.H.C., Abbot.M.M., Introduction to chemical engineering thermodynamics, McGraw-Hill Book Company, Inc, 1996
- [11] Sinnott.R.K., Coulson and Richrdsons, Chemical Engineering Design, Vol.6, Butterworth, 1996.